

**BEFORE THE
FLORIDA PUBLIC SERVICE COMMISSION**

REBUTTAL TESTIMONY OF

ROBERT M. BELL, PH.D.

ON BEHALF OF

**AT&T COMMUNICATIONS OF THE SOUTHERN STATES, INC.
WORLDCOM, INC.
DIECA COMMUNICATIONS COMPANY D/B/A COVAD COMMUNICATIONS
COMPANY
NEW SOUTH COMMUNICATIONS CORP.
MPOWER COMMUNICATIONS CORP.
E.SPIRE COMMUNICATIONS, INC.
ITC^DELTACOM COMMUNICATIONS, INC.
RHYTHMS LINKS INC.**

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FPSC-RECORDS/REPORTING

1 **Q. PLEASE STATE YOUR NAME AND BUSINESS ADDRESS.**

2 **A.** My name is Robert M. Bell. My business address is AT&T Labs-
3 Research, 180 Park Avenue, Florham Park, New Jersey 07932.

4

5 **Q. WHAT IS THE PURPOSE OF YOUR TESTIMONY?**

6 **A.** My testimony responds to certain portions of the direct testimony of Dr.
7 Edward Mulrow and describes errors in Exhibit DAC-6 filed by Mr. David
8 Coon. The greatest part of my testimony discusses problems with an
9 example that Dr. Mulrow uses to illustrate how the parameter delta should
10 be specified.

11

12 **Q. HOW SHOULD THE COMMISSION EVALUATE ALTERNATIVE**
13 **VALUES FOR THE PARAMETER DELTA REQUIRED TO SET A**
14 **BALANCING CRITICAL VALUE?**

15 **A.** Any particular value of the parameter delta implies a specific degree of
16 departure from parity between the service received by ALEC customers
17 and BellSouth's retail customers. Deciding on the appropriateness of a
18 particular value of delta for a measure should be based on a judgment
19 about the impact that the corresponding disparity of service would have on
20 the competitive environment. Delta should define the minimum degree of
21 disparity that causes a material impact on competition. Thinking about
22 real measures is the best way to make these judgments.

23

1 Q. ON PAGES 18-19 OF HIS DIRECT TESTIMONY, DR. MULROW
2 PRESENTED AN EXAMPLE TO ILLUSTRATE THE EFFECTS OF TWO
3 DIFFERENT VALUES OF DELTA FOR A SPECIFIC MEASURE.

4 PLEASE SUMMARIZE THIS EXAMPLE?

5 A. Dr. Mulrow performs calculations for a measure, time to provision a
6 dispatched retail order, which he assumes has a mean of 5.0 days and
7 standard deviation of 0.5 days for BellSouth's customers. He states that a
8 delta of 1.0 implies that the minimum difference between the ALEC and
9 BellSouth means that would be material equals one-half the BellSouth
10 standard deviation (0.25 days or 6 hours). He writes that a delta of 1
11 "means that as long as the average time taken to provide the relevant
12 service to the ALECs did not exceed the BellSouth mean (5 days) plus
13 one-half of the standard deviation I mentioned (half a day), the difference
14 would not be material. That is, if the mean for the ALECs for this period
15 were 5.25 days or less, the difference would not be material." (p. 18, lines
16 15-19). This leads to the question, "Is it material that BellSouth took 6
17 hours longer over a five-day period on average to provide service to the
18 ALEC than to its own retail services?" (p. 19, lines 6-8). A corresponding
19 calculation for delta equals 0.5 led to the question "Is it material that
20 BellSouth took 3 hours longer, on average?" (p. 19, lines 8-9).

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1 **Q. IS DR. MULROW'S EXAMPLE USEFUL?**

2 **A.** No. There are two problems with the example that result in the statement
3 of misleading questions about material impact. First, Dr. Mulrow
4 incorrectly includes a factor of one half in his calculation of the difference
5 implied by any value of delta. Second, he assumes an implausibly small
6 value for BellSouth's standard deviation for the time-to-provision measure.
7 Consequently, he understates the resulting disparity by a factor of 20 or
8 more.

9

10 **Q. WHAT WAS THE FIRST PROBLEM WITH THE EXAMPLE AND WHY IS**
11 **IT IMPORTANT?**

12 **A.** Dr. Mulrow argues that the parameter delta should be set so that the
13 minimum material difference equals $0.5 \times \text{delta} \times \text{BellSouth's standard}$
14 deviation . Including the factor of one-half violates the balancing principle
15 because balancing occurs when the true difference in means equals delta
16 $\times \text{BellSouth's standard deviation}$. The Louisiana joint statistician's report
17 implicitly defines materiality in terms of the alternative hypothesis, "If a
18 standard of materiality is set by stating a specific alternative hypothesis for
19 the test, ...then a critical value can be determined so that the two error
20 probabilities are equal." (Exhibit EJM-1, page 9 of 39). That is, a material
21 difference must be defined as $\text{delta} \times \text{BellSouth's standard deviation}$ (the
22 difference between the BellSouth mean and the ALEC mean under the
23 alternative hypothesis). If delta is set incorrectly, so that a difference of

1 one-half that size is material, then proper balancing does not occur. The
2 probability of a Type II error when there is a difference corresponding to
3 one-half delta remains at 50 percent, no matter how low the Type I error
4 falls.

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6 **Q. WHAT WAS THE SECOND PROBLEM WITH THE EXAMPLE AND WHY**
7 **IS IT IMPORTANT?**

8 **A.** Dr. Mulrow's example assumed that BellSouth's standard deviation was
9 0.5 days—only one-tenth the average time to provision. Because
10 distributions for waiting times tend to have long tails (i.e., some customers
11 may take 30 days or more to provision), these measures would be
12 expected to have standard deviations that exceed their means. For
13 example, in a later example, Dr. Mulrow assumes that the standard
14 deviation of the interval for providing service to BellSouth's retail analog is
15 4 days, compared with a mean of only 3 days. Real data demonstrate the
16 same relationship (see "Qwest Performance Results (ROC 271 PID 2.0,"
17 December 21, 2000). Page 54 of the report shows monthly summary data
18 for the measure OP-4A, "Installation Interval (Average Days) – Dispatches
19 within MSAs" for residences. For nine of the ten reported months
20 (January to October 2000), the CLEC standard deviation exceeds the
21 CLEC mean (the report does not report standard deviations for Qwest
22 customers). The ratios of the standard deviations to the means range

1 from 0.91 to 1.66 with a median of 1.19. Similar results hold for
2 dispatches outside MSAs (measure OP-4B).

3 Consider the consequence of using a more realistic, but still conservative,
4 standard deviation of 5 days in Dr. Mulrow's example. In that cases, a
5 delta of 1.0 would imply a difference of 5 days between the ALEC and
6 BellSouth means—20 times larger than the 6 hours calculated by Dr.
7 Mulrow. Based on the improved calculation, delta equal to 1.0 implies that
8 as long as the average time taken to provide the relevant service to the
9 ALECs did not exceed 10 days, the difference would not be material.

10 The following table shows the correct degree of disparity associated with
11 various values of delta (assuming BellSouth's standard deviation equals 5
12 days). For example, delta = 0.50 (second row from bottom) implies a
13 difference of 2.5 days, so that balancing occurs with for an alternative
14 hypothesis that the ALEC mean equals 7.50 days. Note that the
15 disparities stated in Dr. Mulrow's testimony actually correspond to delta
16 values of 0.025 and 0.05.

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Degree of Disparity Associated with
Selected Values of Delta

Delta	Disparity (in days)	ALEC Mean (in days)
0.025	0.125	5.125
0.05	0.25	5.25
0.10	0.50	5.50
0.25	1.25	6.25
0.50	2.50	7.50
1.00	5.00	10.00

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Disparity = difference in means implied
by Delta (Delta x 5 days)
ALEC Mean = ALEC Mean under alternative
hypothesis (BellSouth mean + Disparity)

8 **Q. DR. MULROW REJECTS A FLOOR FOR THE BALANCING CRITICAL**
9 **VALUE CONCLUDING, "BELLSOUTH WOULD BE PAYING A**
10 **PENALTY EVEN THOUGH THE FOUR-DAY THRESHOLD THAT**
11 **ACTUALLY REPRESENTS A MATERIAL DIFFERENCE HAS NOT**
12 **BEEN MET IN THE FOURTH SET OF OBSERVATIONS." (PP. 21-22).**
13 **DO YOU AGREE WITH HIS CONCLUSION?**

1 **A.** No. In the line that Dr. Mulrow cites, the balancing critical value is -12.35 .
2 Consequently, unequivocal evidence of non-parity with z scores of -8, -10,
3 or even -12 would fail to trigger a remedy. This decision would only be
4 justified if we could be assured that the observed difference did not hinder
5 competition. However, setting delta is not an exact science. There is no
6 magic point at which disparities suddenly become material. Even if there
7 were, we could not identify that point with any certainty. Consequently, a
8 floor on the balancing critical value provides some protection against
9 failing to trigger a remedy in the face of unequivocal, material disparity for
10 measures with large samples, when delta has been set too high. If delta
11 is set at 0.50 or higher, this risk is clear enough that a floor on the
12 balancing critical value should be used. Although the same danger
13 theoretically exists for $\delta = 0.25$, the value used in the joint ALEC plan,
14 the danger is sufficiently small, at current samples sizes, so that I do not
15 anticipate a floor would be necessary. Even at current sample sizes,
16 however, a delta of 0.50 or 1.00 would be problematic.

17

18 **Q. DOES TRUNCATED Z PREVENT PARITY SERVICE IN SOME CELLS**
19 **FROM CONCEALING DISCRIMINATION IN OTHER CELLS?**

20 **A.** No. The truncation step, setting $Z_j^* = \min(0, Z_j)$, is designed to keep a
21 single cell where the ALEC's customers receive much better than parity
22 service from canceling out poor service in other cells. However, it does
23 not prevent parity, or better, service in a large number of cells from

1 concealing very poor service in other cells. Suppose that BellSouth
2 provides very poor service in a few cells (e.g., modified z scores extreme
3 enough to rule out random variation as the explanation) and parity service
4 in other cells being aggregated. The more parity cells that are included
5 the greater the chance is that truncated z will not be significant. The
6 reason is that each cell that is in parity tends to increase the expected
7 value of the truncated z statistic (high values are take as evidence of
8 parity). In addition, each cell that is in parity decreases the balancing
9 critical value that truncated z must fall below to be judged significant.
10 Similarly, parity service in just a few large cells can conceal very poor
11 service in much smaller cells because the truncated z statistics weights
12 the modified z scores according to sample sizes in the cells. This feature
13 of truncated z is not a flaw in the procedure, but it can result in unintended
14 consequences if very heterogeneous cells are aggregated.

15

16 **Q. ARE THE CALCULATIONS ILLUSTRATING THE SEEM REMEDY**
17 **PROCEDURE, ON PAGES 4-6 OF EXHIBIT DAC-6, CORRECT?**

18 **A.** No. The ILEC sample sizes for cells 1-10, which are not provided, would
19 be required to validate exactly the modified z, truncated z and balancing
20 critical values. However, there is enough information available to prove
21 that the balancing critical values shown in the tables are wrong by as
22 much as a factor of 70. The tables all report balancing critical values of –
23 0.21. However, for Order Completion Interval (p. 5), if the total ILEC

1 sample size of 50,000 is divided equally among the ten cells, the correct
2 balancing critical value (BCV) is -14.58. If, instead, the ILEC sample is
3 divided in proportion to the CLEC sample, the correct BCV is -14.67.
4 Even if each ILEC cell size were only 10 (for a total of ILEC sample of
5 100), the correct BCV would be -4.75. Under any of these three scenarios
6 for the correct BCV, a truncated z of -1.92 would not even approach the
7 BCV, and no payout would be made. Consequently, all three tables give a
8 distorted impression of the SEEM remedy procedure.

9

10 **Q. DOES THAT CONCLUDE YOUR TESTIMONY?**

11 **A. Yes.**