THE RELATIONSHIP BETWEEN RETURN AND MARKET VALUE OF COMMON STOCKS*

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This study examines the empirical relationship between the return and the total market value of NYSE common stocks. It is found that smaller firms have had higher risk adjusted returns on average, than larger firms. This 'size effect' has been in existence for at least forty years and is evidence that the capital asset pricing model is reisspecified. The size effect is not linear in the market value; the main effect occurs for very small firms while there is little difference in return between average sized and large firms. It is not known whether size per se is responsible for the effect or whether size is just a proxy for one or more true unknown factors correlated with size.

1. Introduction

The single-period capital asset pricing model (henceforth CAPM) postulates a simple linear relationship between the expected return and the market risk of a security. While the results of direct tests have been inconclusive, recent evidence suggests the existence of additional factors which are relevant for asset pricing. Litzenberger and Ramaswamy (1979) show a significant positive relationship between dividend yield and return of common stocks for the 1936-1977 period. Basu (1977) finds that price-earnings ratios and risk adjusted returns are related. He chooses to interpret his findings as evidence of market inefficiency but as Ball (1978) points out, market efficiency tests are often joint tests of the efficient market hypothesis and a particular equilibrium relationship. Thus, some of the anomalies that have been attributed to a lack of market efficiency might well be the result of a misspecification of the pricing model.

This study contributes another piece to the emerging puzzle. It examines the relationship between the total market value of the common stock of a firm and its return. The results show that, in the 1936-1975 period, the common stock of small firms had, on average, higher risk-adjusted returns

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than the common stock of large firms. This result will henceforth be referred to as the 'size effect'. Since the results of the study are not based on a particular theoretical equilibrium model, it is not possible to determine conclusively whether market value per se matters or whether it is only a proxy for unknown true additional factors correlated with market value. The last section of this paper will address this question in greater detail.

The various methods currently available for the type of empirical research presented in this study are discussed in section 2. Since there is a considerable amount of confusion about their relative merit, more than one technique is used. Section 3 discusses the data. The empirical results are presented in section 4. A discussion of the relationship between the size effect and other factors, as well as some speculative comments on possible explanations of the results, constitute section 5.

2. Methodologies

The empirical tests are based on a generalized asset pricing model which allows the expected return of a common stock to be a function of risk β and an additional factor ϕ , the market value of the equity. A simple linear relationship of the form

$$E(R_i) = \gamma_0 + \gamma_1 \beta_i + \gamma_2 [(\phi_i - \phi_m)/\phi_m], \qquad (1)$$

is assumed, where

 $E(R_i)$ = expected return on security i,

= expected return on a zero-beta portfolio,

= expected market risk premium,

= market value of security i,

φ_m = average market value, and

= constant measuring the contribution of ϕ_i to the expected return of a security.

If there is no relationship between ϕ_i and the expected return, i.e., $\gamma_2 = 0$, (1) reduces to the Black (1972) version of the CAPM.

Since expectations are not observable, the parameters in (1) must be estimated from historical data. Several methods are available for this purpose. They all involve the use of pooled cross-sectional and time series regressions to estimate γ_0 , γ_1 , and γ_2 . They differ primarily in (a) the assumption concerning the residual variance of the stock returns (homoscedastic or heteroscedastic in the cross-sectional), and (b) the treatment of the

In the empirical tests, Φ_i and Φ_m are defined as the market proportion of security i and average market proportion, respectively. The two specifications are, of course, equivalent.

errors-in-variables problem introduced by the use of estimated betas in (1). All methods use a constrained optimization procedure, described in Fama (1976, ch. 9), to generate minimum variance (m.v.) portfolios with mean returns γ_i , i=0,...,2. This imposes certain constraints on the portfolio weights, since from (1)

$$E(R_p) = \gamma_i = \gamma_0 \sum_j w_j + \gamma_1 \sum_j w_j \beta_j + \gamma_1 \left[\left(\sum_j w_j \phi_j - \phi_m \sum_j w_j \right) \middle/ \phi_m \right], \quad i = 0, \dots, 2,$$
 (2)

where the w_j are the portfolio proportions of each asset j, j=1,...,N. An examination of (2) shows that $\hat{\gamma}_0$ is the mean return of a standard m.v. portfolio $(\sum_j w_j = 1)$ with zero beta and $\phi_p \equiv \sum_j w_j \phi_j = \phi_m$ [to make the second and third terms of the right-hand side of (2) vanish]. Similarly, $\hat{\gamma}_1$ is the mean return on a zero-investment m.v. portfolio with beta of one and $\phi_p = 0$, and $\hat{\gamma}_2$ is the mean return on a m.x. zero-investment, zero-beta portfolio with $\phi_p = \phi_m$. As shown by Fama (1976, ch. 9), this constrained optimization can be performed by running a cross-sectional regression of the form

$$R_{it} = \gamma_{0t} + \gamma_{1t}\beta_{it} + \gamma_{2t} [(\phi_{it} - \phi_{mt})/\phi_{mt}] + \varepsilon_{it}, \qquad i = 1, ..., N,$$
 (3)

on a period-by-period basis, using estimated betas β_u and allowing for either homoscedastic or heteroscedastic error terms. Invoking the usual stationarity arguments the final estimates of the gammas are calculated as the averages of the Testimates.

One basic approach involves grouping individual securities into portfolios on the basis of market value and security beta, reestimating the relevant parameters (beta, residual variance) of the portfolios in a subsequent period, and finally performing either an ordinary least squares (OLS) regression [Fama and MacBeth (1973)] which assumes homoscedastic errors, or a generalized least squares (GLS) regression [Black and Scholes (1974)] which allows for heteroscedastic errors, on the portfolios in each time period. 2 Grouping reduces the errors-in-variables problem, but is not very efficient because it does not make use of all information. The errors-in-variables problem should not be a factor as long as the portfolios contain a reasonable number of securities. 3

Litzenberger and Ramaswamy (1979) have suggested an alternative method which avoids grouping. They allow for heteroscedastic errors in the cross-section and use the estimates of the standard errors of the security

²Black and Scholes (1974) do not take account of heteroscedasticity, even though their method was designed to do so.

Black, Jensen and Scholes (1972, p. 116).

betas as estimates of the measurement errors. As Theil (1971, p. 610) has pointed out, this method leads to unbiased maximum likelihood estimators for the gammas as long as the error in the standard error of beta is small and the standard assumptions of the simple errors-in-variables model are met. Thus, it is very important that the diagonal model is the correct specification of the return-generating process, since the residual variance assumes a critical position in this procedure. The Litzenberger-Ramaswamy method is superior from a theoretical viewpoint; however, preliminary work has shown that it leads to serious problems when applied to the model of this study and is not pursued any further.

Instead of estimating equation (3) with data for all securities, it is also possible to construct arbitrage portfolios containing stocks of very large and very small firms by combining long positions in small firms with short positions in large firms. A simple time series regression is run to determine the difference in risk-adjusted returns between small and large firms. This approach, long familiar in the efficient markets and option pricing literature, has the advantage that no assumptions about the exact functional relationships between market value and expected return need to be made, and it will therefore be used in this study.

3. Data

The sample includes all common stocks quoted on the NYSE for at least five years between 1926 and 1975. Monthly price and return data and the number of shares outstanding at the end of each month are available in the monthly returns file of the Center for Research in Security Prices (CRSP) of the University of Chicago. Three different market indices are used; this is in response to Roll's (1977) critique of empirical tests of the CAPM. Two of the three are pure common stock indices—the CRSP equally—and value-weighted indices. The third is more comprehensive: a value-weighted combination of the CRSP value-weighted index and return data on corporate and government bonds from Ibbotson and Sinquefield (1977) (henceforth market index'). The weights of the components of this index are derived from information on the total market value of corporate and government bonds, in various issues of the Survey of Current Business (updated annually) and from the market value of common stocks in the CRSP monthly index file. The stock indices, made up of riskier assets, have both higher returns

No pretense is made that this index is complete; thus, the use of quotation marks. It ignores real estate, foreign assets, etc.; it should be considered a first step toward a comprehensive index. See [bbotson and Fall (1979).

⁴If the diagonal model (or market model) is an incomplete specification of the return generating process, the estimate of the standard error of beta is likely to have an upward bias, since the residual variance estimate is too large. The error in the residual variance estimate appears to be related to the second factor. Therefore, the resulting gamma estimates are biased.

and higher risk than the bond indices and the 'market index'.6 A time series of commercial paper returns is used as the risk-free rate. While not actually constant through time, its variation is very small when compared to that of the other series, and it is not significantly correlated with any of the three indices used as market proxies.

4. Empirical results

4.1. Results for methods based on grouped data

The portfolio selection procedure used in this study is identical to the one described at length in Black and Scholes (1974). The securities are assigned to one of twenty-five portfolios containing similar numbers of securities, first to one of five on the basis of the market value of the stock, then the securities in each of those five are in turn assigned to one of five portfolios on the basis of their beta. Five years of data are used for the estimation of the security beta; the next five years' data are used for the reestimation of the portfolio betas. Stock price and number of shares outstanding at the end of the five year periods are used for the calculation of the market proportions. The portfolios are updated every year. The cross-sectional regression (3) is then performed in each month and the means of the resulting time series of the gammas could be (and have been in the past) interpreted as the final estimators. However, having used estimated parameters, it is not certain that the series have the theoretical properties, in particular, the hypothesized beta. Black and Scholes (1974, p. 17) suggest that the time series of the gammas be regressed once more on the excess return of the market index. This correction involves running the time series regression (for $\hat{\gamma}_2$)

$$\hat{\gamma}_{2t} - R_{Ft} = \hat{\alpha}_2 + \hat{\beta}_2 (R_{mt} - R_{Ft}) + \hat{\varepsilon}_{2t}. \tag{4}$$

It has been shows earlier that the theoretical β_2 is zero. (4) removes the effects of a non-zero β_2 on the return estimate $\hat{\gamma}_2$ and $\hat{\alpha}_2$ is used as the final estimator for $\hat{\gamma}_2 - R_F$. Similar corrections are performed for γ_0 and γ_1 . The

Mean monthly returns and standard deviations for the 1926-1975 period are:

/	. Mean return	Standard deviation		
Market index' CRSP value-weighted index CRSP equally-weighted index Government bond index Corporate bond index	0.0046 0.0085 0.0120 0.0027 0.0032	0.0178 0.0588 0.0830 0.0157 0.0142		

⁷I am grateful to Myron Scholes for making this series available. The mean monthly return for the 1926-1975 period is 0.0026 and the standard deviation is 0.0021.

derivations of the β_i , i=0,...,2, in (4) from their theoretical values also allow us to check whether the grouping procedure is an effective means to eliminate the errors-in-beta problem.

The results are essentially identical for both OLS and GLS and for all three indices. Thus, only one set of results, those for the 'market index' with GLS, is presented in table 1. For each of the gammas, three numbers are reported: the mean of that time series of returns which is relevant for the test of the hypothesis of interest (i.e., whether or not $\hat{\gamma}_0$ and $\hat{\gamma}_1$ are different from the risk-free rate and the risk premium, respectively), the associated t-statistic, and finally, the estimated beta of the time series of the gamma from (4). Note that the means are corrected for the deviation from the theoretical beta as discussed above.

The table shows a significantly negative estimate for γ_2 for the overall time period. Thus, shares of firms with large market values have had smaller returns, on average, than similar small firms. The CAPM appears to be misspecified. The table also shows that γ_0 is different from the risk-free rate. As both Fama (1976, ch. 9) and Roll (1977) have pointed out, if a test does not use the true market portfolio, the Sharpe-Lintner model might be wrongly rejected. The estimates for γ_0 are of the same magnitude as those reported by Fama and MacBeth (1973) and others. The choice of a market index and the econometric method does not affect the results. Thus, at least within the context of this study, the choice of a proxy for the market portfolio does not seem to affect the results and allowing for heteroscedastic disturbances does not lead to significantly more efficient estimators.

Before looking at the results in more detail, some comments on econometric problems are in order. The results in table 1 are based on the 'market index' which is likely to be superior to pure stock indices from a theoretical viewpoint since it includes more assets [Roll (1977)]. This superiority has its price. The actual betas of the time series of the gammas are reported in table 1 in the columns labeled, β_1 . Recall that the theoretical values of β_0 and β_1 are zero and one, respectively. The standard zero-beta portfolio with return $\hat{\gamma}_0$ contains high beta stocks in short positions and low beta stocks in long positions, while the opposite is the case for the zero-investment portfolio with return $\hat{\gamma}_1$. The actual betas are all significantly different from the theoretical values. This suggests a regression effect, i.e., the past betas of high beta securities are overestimated and the betas of low beta-securities are underestimated. Past beta is not completely uncorrelated with the error of the current beta and the instrumental variable approach to the error-in-variables problem is not entirely successful.

There is no such effect for β_2 because that portfolio has both zero beta and zero investment; i.e., net holdings of both high and low beta securities are, on average, zero.

This result is first documented in Brenner (1976) who examines the original Fama-McBeth (1973) time series of $\hat{\gamma}_{00}$.

Table 1

Portfolio estimators for γ_0 , γ_1 and γ_2 based on the 'market index' with generalized least squares estimation.' $R_0 = \hat{\gamma}_0 + \hat{\gamma}_1 \beta_0 + \hat{\gamma}_2 [(\phi_0 - \phi_{m_0}) \phi_{m_0}]$

										200
Period	$\hat{\gamma}_0 - R_F$	$I(\hat{\gamma}_0 - R_F^-)^+$	$\hat{\beta}_{o}$	$\dot{\gamma}_s - (R_M - R_F)$	$t(\hat{\gamma}_1 - (R_M - R_I))$	β ₁	† ₂ –	$t(\hat{\gamma}_2)$	β2	
1936-1975	0.00450	2.76	0.45	-0.00092	- 1.00 00.1	0.75	-0.00052	- 2.92	0.01 -	
1936-1955	0.00377 .	1.66	0.43	-0.00060	-0.80	0.80	-0.00043	-2.12	0.01	
1956-1975	0.00531	2.22	0.46	-0.00138	-0.82	0.73	-0.00062	- 2.09	0.01	-
1936-1945	0.00121	0.30	0.63	-0.00098	- 0.77	0.82	-0.00075	-2.32	-0.01	
1946-1955	0.00650-	- 2.89	0.03	-0.00021	-0.26	0.75	-0.00015	-0.65	. 0.06	
1956-1965	0.00494	2.02	0.34	~ 0.00098	-0.56	0.96	-0.00039	-1.27	-0.01	
1966-1975	0.00596	1.43	0.497	-0.00232	-0.80	0.69	-0.00080	-1.55	0.01	
		-								-

 $[\]hat{r}_{i0} - R_F =$ mean difference between return on zero beta portfolio and risk-free rate, $\hat{r}_{i1} - (R_M - R_E) =$ mean difference between actual risk premium (\hat{r}_{i1}) and risk premium stipulated by Sharpe-Lintner model $(R_M - R_F)$, $\hat{r}_{i1} =$ size premium, $\hat{\beta}_i =$ actual estimated market risk of \hat{r}_{i1} (theoretical values: $\beta_0 = 0$, $\beta_1 = 1$, $\beta_2 = 0$); all β_0 , β_1 are significantly different from the theoretical values. $t(\cdot) = t$ -statistic.

The deviations from the theoretical betas are largest for the 'market index', smaller, for the CRSP value-weighted index, and smallest for the CRSP equally-weighted index. This is due to two factors: first, even if the true covariance structure is stationary, betas with respect to a value-weighted index change whenever the weights change, since the weighted average of the betas is constrained to be equal to one. Second, the betas and their standard errors with respect to the 'market index' are much larger than for the stock indices (a typical stock beta is between two and three), which leads to larger deviations — a kind of 'leverage' effect. Thus, the results in table 1 show that the final correction for the deviation of β_0 and β_1 from their theoretical values is of crucial importance for maket proxies with changing weights.

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Estimated portfolio betas and portfolio market proportions are (negatively) correlated. It is therefore possible that the errors in beta induce an error in the coefficient of the market proportion. According to Levi (1973), the probability limit of \hat{y}_1 in the standard errors in the variables model is

plim
$$\gamma_1 = \gamma_1/(1 + (\sigma_u^2 \cdot \sigma_2^2)/D) < \gamma_1$$

with

$$D = (\sigma_1^2 + \sigma_u^2) \cdot \sigma_2^2 - \sigma_{12}^2 > 0,$$

where σ_1^2 , σ_2^2 are the variances of the true factors β and ϕ , respectively, σ_u^2 is the variance of the error in beta and σ_{12} is the covariance of β and ϕ . Thus, the bias in $\hat{\gamma}_1$ is unambiguously towards zero for positive γ_1 . The probability limit of $\hat{\gamma}_2 + \gamma_2$ is [Levi (1973)]

plim
$$(\hat{\gamma}_2 \leftarrow \gamma_2)' = (\sigma_u^2 \cdot \sigma_{12} \cdot \gamma_1)/D$$
.

We find that the bias in $\hat{\gamma}_2$ depends on the covariance between β and ϕ and the sign of γ_1 . If σ_{12} has the same sign as the covariance between β and ϕ , i.e., $\sigma_{12} < 0$, and if $\gamma_1 > 0$, then plim $(\hat{\gamma}_2 - \gamma_2) < 0$, i.e., plim $\hat{\gamma}_2 < \gamma_2$. If the grouping procedure is not successful in removing the error in beta, then it is likely that the reported $\hat{\gamma}_2$ overstates the true magnitude of the size effect. If this was a serious problem in this study, the results for the different market indices should reflect the problem. In particular, using the equally-weighted stock index should then lead to the smallest size effect since, as was pointed out earlier, the error in beta problem is apparently less serious for that kind of index. In fact, we find that there is little difference between the estimates. 10

¹⁰For the overall time period, $\hat{\gamma}_2$ with the equally-weighted CRSP index is -0.00044, with the value weighted CRSP index -0.00044 as well as opposed to the -0.00052 for the 'market index' reported in table 1. The estimated betas of $\hat{\gamma}_0$ and $\hat{\gamma}_1$ which reflect the degree of the error in beta problems are 0.07 and 0.91, respectively, for the equally-weighted CRSP index and 0.13 and 0.87 for the value-weighted CRSP index.

Thus, it does not appear that the size effect is just a proxy for the unobservable true beta even though the market proportion and the beta of securities are negatively correlated.

The correlation coefficient between the mean market values of the twentyelive portfolios and their betas is significantly negative, which might have
introduced a multicollinearity problem. One of its possible consequences is
coefficients that are very sensitive to addition or deletion of data. This effect
does not appear to occur in this case: the results do not change significantly
when five portfolios are dropped from the sample. Revising the grouping
procedure — ranking on the basis of beta first, then ranking on the basis of
market proportion — also does not lead to substantially different results.

4.2. A closer look at the results

An additional factor relevant for asset pricing—the market value of the equity of a firm—has been found. The results are based on a linear model. Linearity was assumed only for convenience and there is no theoretical reason (since there is no model) why the relationship should be linear. If it is nonlinear, the particular form of the relationship might give us a starting point for the discussion of possible causes of the size effect in the next section. An analysis of the residuals of the twenty-five portfolios is the easiest way to look at the linearity question. For each month t, the estimated residual return

$$\hat{\epsilon}_{it} = R_{it} - \hat{\gamma}_{0t} - \hat{\gamma}_{1t} \hat{\beta}_{it} - \hat{\gamma}_{2t} [(\phi_{it} - \phi_{mt})/\phi_{mt}], \qquad i = 1, ..., 25,$$
 (5)

is calculated for all portfolios. The mean residuals over the forty-five year sample period are plotted as a function of the mean market proportion in fig. 1. Since the distribution of the market proportions is very skewed, a logarithmic scale is used. The solid line connects the mean residual returns of each size group. The numbers identify the individual portfolios within each group according to beta, '1' being the one with the largest beta, '5' being the one with the smallest beta.

The figure shows clearly that the linear model is misspecified.¹¹ The residuals are not randomly distributed around zero. The residuals of the portfolios containing the smallest firms are all positive; the remaining ones are close to zero. As a consequence, it is impossible to use $\hat{\gamma}_2$ as a simple size premium in the cross-section. The plot also shows, however, that the misspecification is not responsible for the significance of $\hat{\gamma}_2$ since the linear model underestimates the true size effect present for very small firms. To illustrate this point, the five portfolios containing the smaller firms are

¹¹The nonlinearity cannot be eliminated by defining ϕ_i as the log of the market proportion.

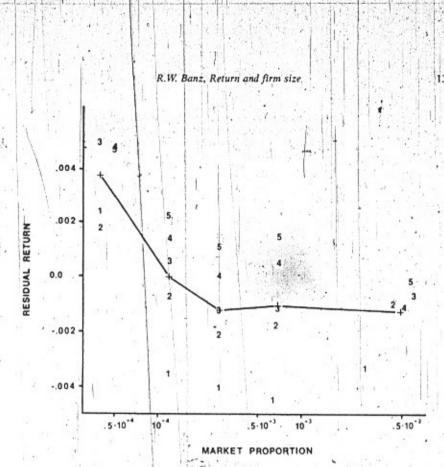


Fig. 2. Mean residual returns of portfolios (1936–1975) with equally-weighted CRSP index as market proxy. The residual is calculated with the two-factor model $(\hat{\epsilon}_n = R_n - \hat{\gamma}_0 - \hat{\gamma}_1 \hat{\beta}_n)$. The symbols are as defined for fig. 1.

4.3. 'Arbitrage' portfolio returns

One important empirical question still remains: How important is the size effect from a practical point of view? Fig. 2 suggests that the difference in returns between the smallest firms and the remaining ones is, on average, about 0.4 percent per month. A more dramatic result can be obtained when the securities are chosen solely on the basis of their market value.

As an illustration, consider putting equal dollar amounts into portfolios containing the smallest, largest and median-sized firms at the beginning of a year. These portfolios are to be equally weighted and contain, say, ten, twenty or fifty securities. They are to be held for five years and are rebalanced every month. They are levered or unlevered to have the same beta. We are then interested in the differences in their returns,

$$R_{1t} = R_{st} - R_{tr},$$
 $R_{2t} = R_{sr} - R_{at},$ $R_{3t} = R_{at} - R_{tt},$ (6)

Table 3 Mean monthly returns on 'arbitrage' portfolios." $R_j - R_k = \hat{\pi}_i + \hat{\beta}_i (R_m - R_F)$

	ā ₁ ^b			x2°			\hat{x}_3^d			
	n = 10	n = 20	n = 50	n = 10 .	n = 20	n = 50	n = 10	n = 20	n = 50	
Overall period 1931-1975	0.0152 (2.99)	0.0148 (3.53)	0.0101	0.0130 (2.90)	0.0124 (3.56)	0.0089	0.0021		0.0012 (0.85)	
Fire-year subper 1931-1935	(2.25)	0.0597 (2.81)	(2.35)	0.0462 (1.92)	0.0462	0.0326	0.0127 (1.09)	0.0134	0.0101	
1936-1940	(0.82)	(0.97)	(0.67)	(0.55)	0.0145 (0.90)	(0.65)	(1.20)	0.0037	0.0025	3
1941-1945	0.0430 (2.29)	0.0408 (2.46)	0.02 69 (2.17)	(2.29)	0.0367 · (2.54)	0.0228	0.0049	0.0038	0.0041	Danz, N
1946–1950	-0.0060 (-1.17)	-0.0046, (-0.97)	- 0.0036 (-0.97)	- 0.0058 (-1.03)	- 0.0059 - (-1,29)	-0.0029 (-0.83)	-0.0002 (-0.07)	(-0.50)	-0.0007 (-0.38)	1077
1951-1955	-0.0067 (-0.89)	-0.0011 (-0.21)	0.0013	-0.0004 (-0.07)	0.0026	0.0010 (0.39)	-0.0062 (-1.29)	-0.0037 (-0.99)	0.0003	na jirn
1956-1960	0.0039 (0.67)	0.0008	(0.89)	(0.14)	-0.0027 (-0.64)	(0.45)	(0.88)	(1.16)	0.0026_	3218
1961-1965	0.0131	0.0060 (0.67)	0.0024,	0.0096 (1.11)	(0.72)	0.0036	0.0035	(0.24)	-0.0012 (-0.24)	
1966-1970	0.0121 ^t (1.64)	0.0117	0.0077	(1.93)	0.0110 (2.71)	0.0071 (2.43)	(0.23)	0.0007	(0.27)	
1971–1975	0.0063	0.0108	0.0098	(0.39)	0.0077	0.0083	(0.64)	0.0031	0.0015	

^{*}Equally-weighted portfolios with n securities, adjusted for differences in market risk-with respect to CRSP value-weighted index, t-statistics in parentheses.

*Small firms held long, large firms held short.

*Small firms held long, median-size firms held short.

*Median-size firms held long, large firms held short.

per month or 19.8 percent on an annualized basis. This strategy, which suggests very large 'profit opportunities', leaves the investor with a poorly diversified portfolio. A portfolio of small firms has typically much larger residual risk with respect to a value-weighted index than a portfolio of very large firms with the same number of securities [Banz (1978, ch. 3)]. Since the fifty largest firms make up more than 25 percent of the total market value of NYSE stocks, it is not surprising that a larger part of the variation of the return of a portfolio of those large firms can be explained by its relation with the value-weighted market index. Table 3 also shows that the strategy would not have been successful in every five year subperiod. Nevertheless, the magnitude of the size effect during the past forty-five years is such that it is of more than just academic interest.

5. Conclusions

The evidence presented in this study suggests that the CAPM is misspecified. On average, small NYSE firms have had significantly larger risk adjusted returns than large NYSE firms over a forty year period. This size effect is not linear in the market proportion (or the log of the market proportion) but is most pronounced for the smallest firms in the sample. The effect is also not very stable through time. An analysis of the ten year subperiods show substantial differences in the magnitude of the coefficient of the size factor (table 1).

There is no theoretical foundation for such an effect. We do not even know whether the factor is size itself or whether size is just a proxy for one or more true but unknown factors correlated with size. It is possible, however, to offer some conjectures and even discuss some factors for which size is suspected to proxy. Recent work by Reinganum (1980) has eliminated, one obvious candidate: the price-earnings (P/E) ratio.13 He finds that the P/E-effect, as reported by Basu (1977), disappears for both NYSE and AMEX stocks when he controls for size but that there is a significant size effect even when he controls for the P/E-ratio, i.e., the P/E-ratio effect is a proxy for the size effect and not vice versa. Stattman (1980), who found a significant negative relationship between the ratio of book value and market value of equity and its return, also reports that this relationship is just a proxy for the size effect. Naturally, a large number of possible factors remain to be tested.14 But the Reinganum results point out a potential problem with some of the existing negative evidence of the efficient market hypothesis. Basu believed to have identified a market inefficiency but his FE-effect is

14E.g., debt-equity ratios, skewness of the return distribution [Kraus and Litzenberger 1976)].

 $^{^{13}}$ The average correlation coefficient between P/E-ratio and market value is only 0.16 for individual stocks for thirty-eight quarters ending in 1978. But for the portfolios formed on the basis of P/E-ratio, it rises to 0.82. Recall that Basu (1977) used ten portfolios in his study.