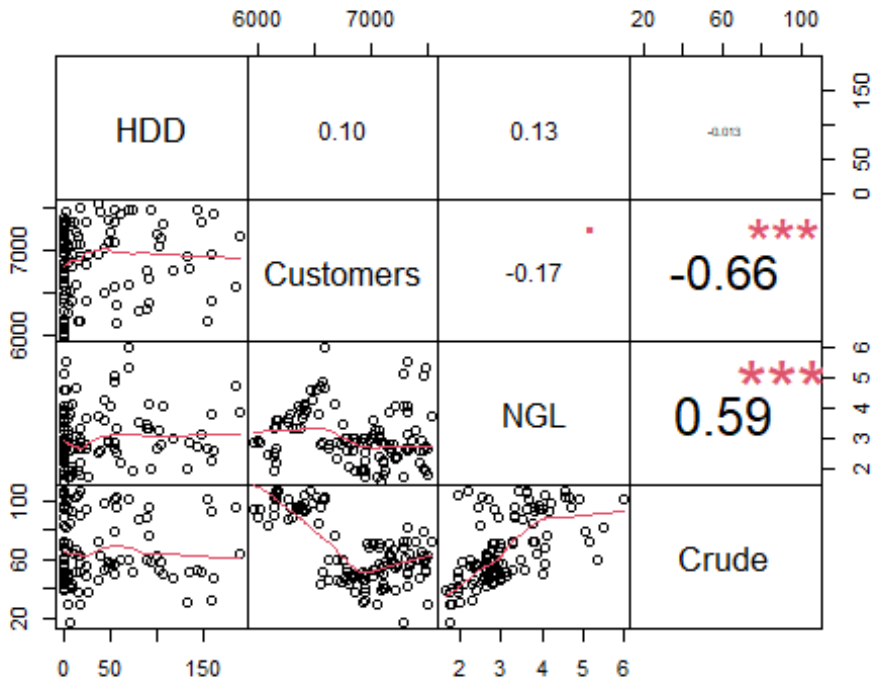
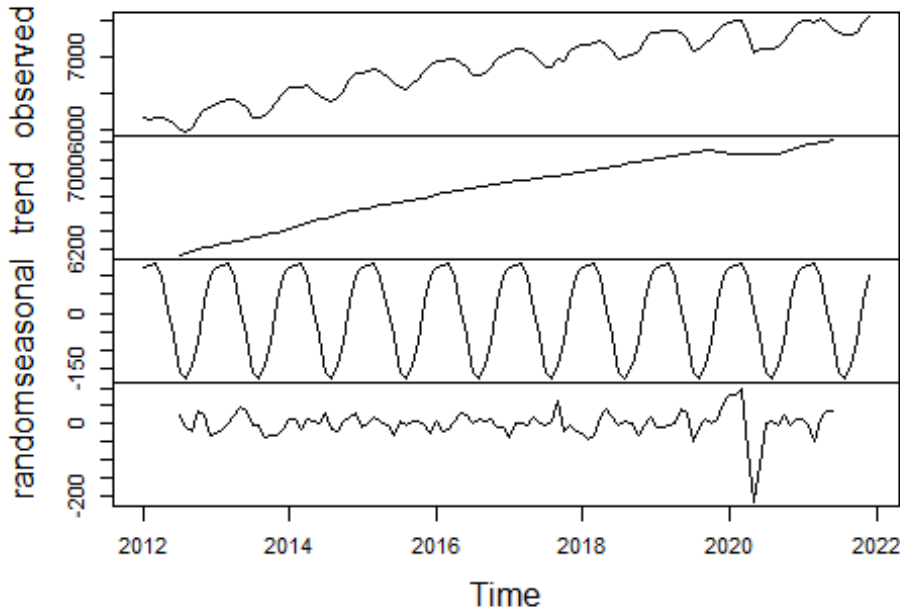


Commercial Customer Count Forecast

Overall Commercial Customers Forecast Analysis

Customer Time-Series Decomposition

Decomposition of additive time series



ARIMA Model: Expected Accuracy

		ME	RMSE	MAE
Forecast Horizon	1	-2	26	20
Forecast Horizon	2	0	28	22
Forecast Horizon	3	-1	28	23
Forecast Horizon	4	-7	44	30
Forecast Horizon	5	-17	76	41
Forecast Horizon	6	-24	87	48
Forecast Horizon	7	-27	89	51
Forecast Horizon	8	-31	94	56
Forecast Horizon	9	-37	100	60
Forecast Horizon	10	-43	103	66
Forecast Horizon	11	-45	106	69
Forecast Horizon	12	-48	110	73
Forecast Horizon	13	-52	114	79
Forecast Horizon	14	-54	115	80
Forecast Horizon	15	-58	119	84
Forecast Horizon	16	-59	121	89
Forecast Horizon	17	-62	121	91
Forecast Horizon	18	-66	119	91
Forecast Horizon	19	-67	115	89
Forecast Horizon	20	-68	115	89
Forecast Horizon	21	-73	120	95
Forecast Horizon	22	-77	122	99
Forecast Horizon	23	-79	122	99
Forecast Horizon	24	-84	124	101

ARIMA Model: Diagnostics

Series: x

ARIMA(0,1,3)(1,1,1)[12]

Coefficients:

	ma1	ma2	ma3	sar1	sma1
	0.0742	-0.3654	-0.1624	-0.1281	-0.8283
s.e.	0.1053	0.0841	0.1085	0.1572	0.2179

sigma^2 estimated as 1500: log likelihood=-548.66

AIC=1109.33 AICc=1110.17 BIC=1125.36

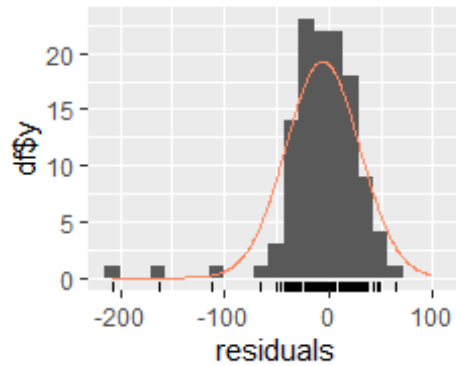
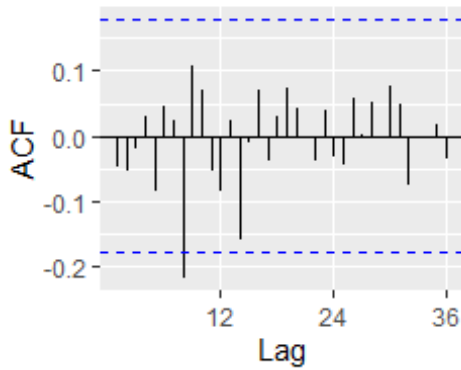
Training set error measures:

	ME	RMSE	MAE	MPE	MAPE	MASE
Training set	-6.049582	35.70541	23.40443	-0.08616574	0.336943	0.1517032

ACF1

Training set -0.04888767

Residuals from ARIMA(0,1,3)(1,1,1)[12]

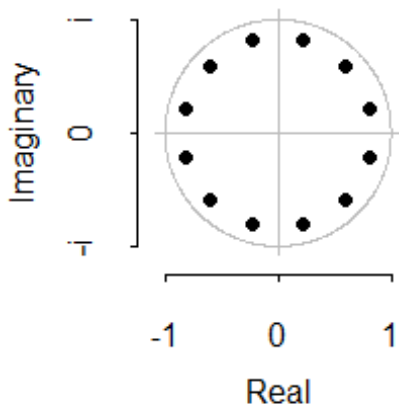


Ljung-Box test

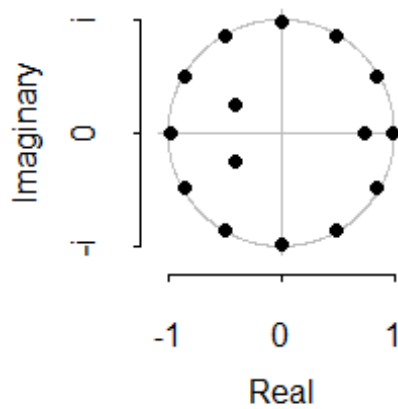
data: Residuals from ARIMA(0,1,3)(1,1,1)[12]
 $Q^* = 18.359$, $df = 19$, $p\text{-value} = 0.4986$

Model df: 5. Total lags used: 24

Inverse AR roots

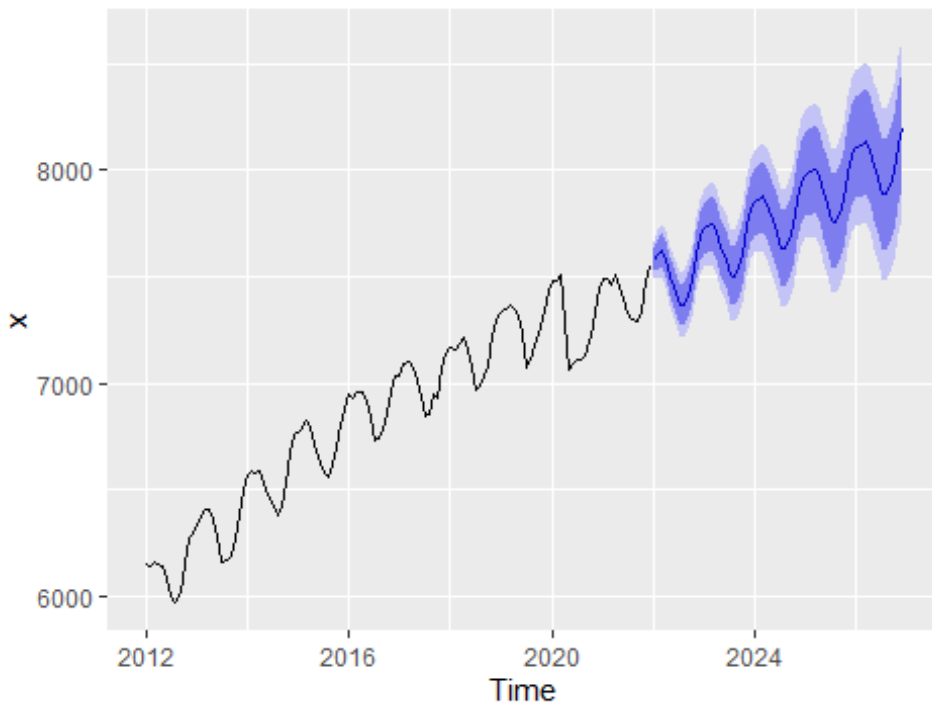


Inverse MA roots



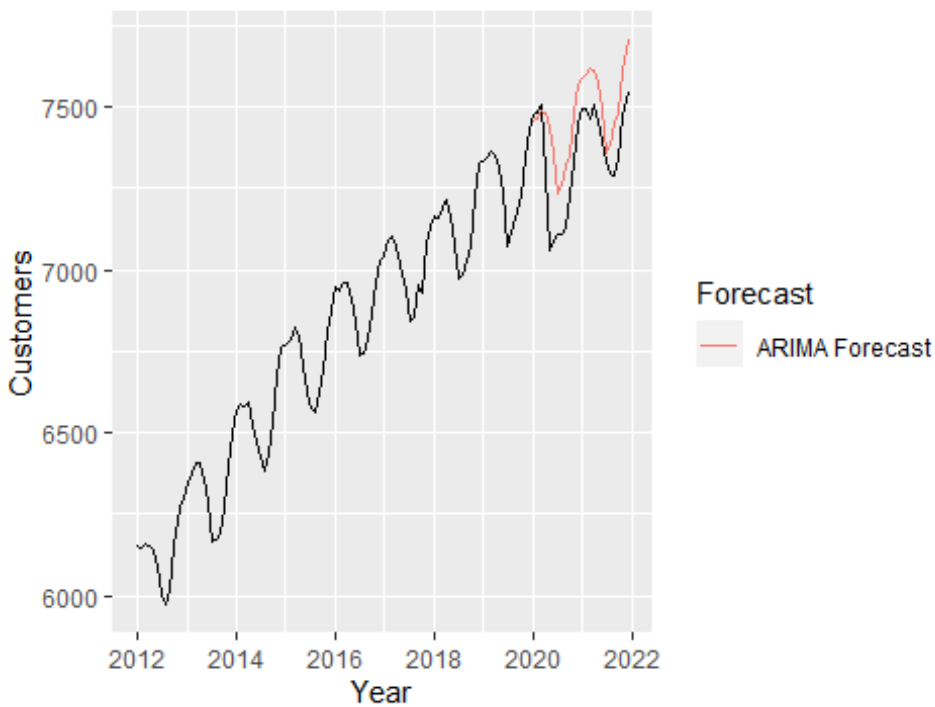
ARIMA Model: 5 Year Forecast

Forecasts from ARIMA(0,1,3)(1,1,1)[12]



Back-Testing

Commercial Client Backtesting: 2020-2021



Test Results

Below we see that the model performs roughly as expected for a “normal” year of 2019, and continues to have a high degree of accuracy in 2020 and 2021.

FPUC-Rate 0625437

[1] "Overall MAE: 131.69"

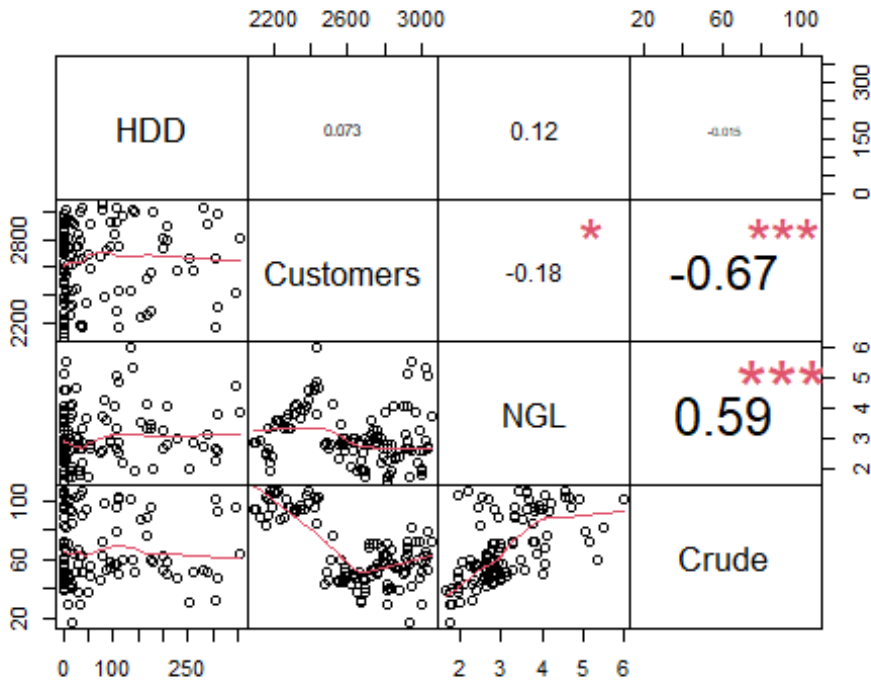
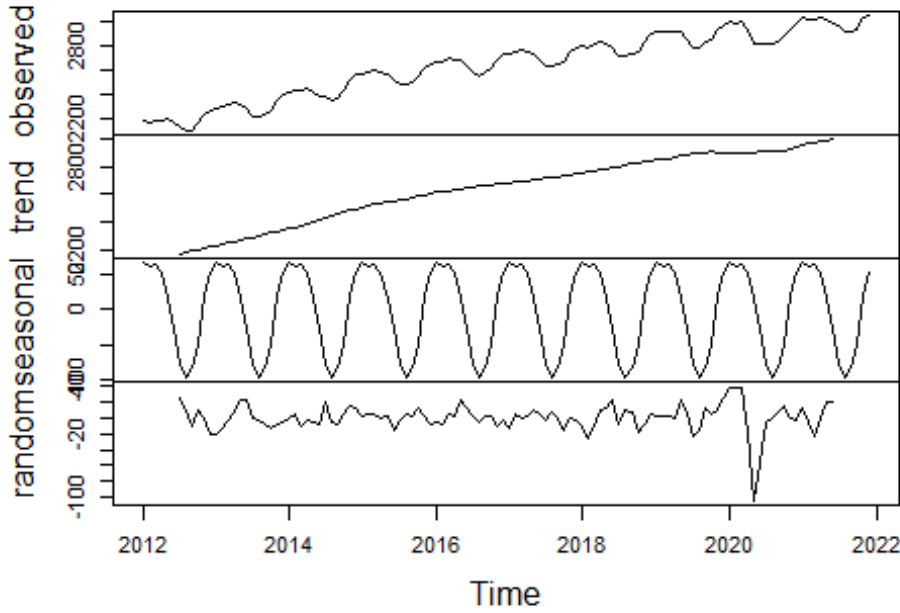
[1] "Overall Accuracy: 98.19"

	Actual	Forecast	Absolute_Error	Accuracy
Jan 2020	7478	7455	23.39	99.7
Feb 2020	7482	7462	19.91	99.7
Mar 2020	7505	7485	19.65	99.7
Apr 2020	7293	7482	189.10	97.4
May 2020	7061	7436	375.23	94.7
Jun 2020	7092	7358	265.68	96.3
Jul 2020	7112	7234	121.93	98.3
Aug 2020	7108	7255	147.46	97.9
Sep 2020	7130	7319	188.97	97.3
Oct 2020	7225	7349	123.76	98.3
Nov 2020	7332	7484	152.40	97.9
Dec 2020	7444	7571	127.13	98.3
Jan 2021	7492	7589	97.01	98.7
Feb 2021	7492	7597	105.06	98.6
Mar 2021	7466	7620	154.26	97.9
Apr 2021	7508	7615	107.31	98.6
May 2021	7456	7574	117.64	98.4
Jun 2021	7392	7495	102.65	98.6
Jul 2021	7332	7358	26.22	99.6
Aug 2021	7298	7386	87.55	98.8
Sep 2021	7287	7449	161.79	97.8
Oct 2021	7336	7484	148.01	98.0
Nov 2021	7478	7615	137.16	98.2
Dec 2021	7544	7705	161.32	97.9

FPUC General Service 2 (FPU-GS2 & FPU-GST2)

Customer Time-Series Decomposition

Decomposition of additive time series



ARIMA Model: Expected Accuracy

	ME	RMSE	MAE
Forecast Horizon 1	1	15	13
Forecast Horizon 2	2	16	12
Forecast Horizon 3	1	17	14

Forecast Horizon	4	0	20	16
Forecast Horizon	5	-5	35	21
Forecast Horizon	6	-8	41	26
Forecast Horizon	7	-10	42	28
Forecast Horizon	8	-11	43	27
Forecast Horizon	9	-13	44	31
Forecast Horizon	10	-14	47	33
Forecast Horizon	11	-15	49	34
Forecast Horizon	12	-16	51	35
Forecast Horizon	13	-17	53	39
Forecast Horizon	14	-17	56	41
Forecast Horizon	15	-18	60	42
Forecast Horizon	16	-19	62	44
Forecast Horizon	17	-20	63	48
Forecast Horizon	18	-20	63	48
Forecast Horizon	19	-20	64	49
Forecast Horizon	20	-21	65	51
Forecast Horizon	21	-23	65	52
Forecast Horizon	22	-25	66	55
Forecast Horizon	23	-25	69	56
Forecast Horizon	24	-27	68	56

ARIMA Model: Diagnostics

Series: x

ARIMA(0,1,2)(0,1,1)[12]

Coefficients:

	ma1	ma2	sma1
	0.0754	-0.3622	-0.8704
s.e.	0.0969	0.1025	0.1547

sigma² estimated as 354.3: log likelihood=-472.54

AIC=953.08 AICc=953.48 BIC=963.78

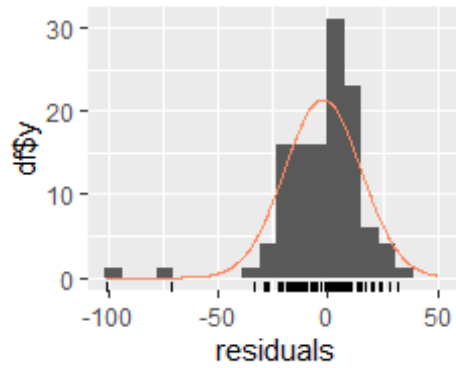
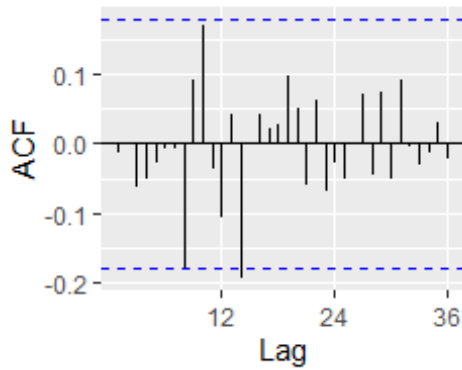
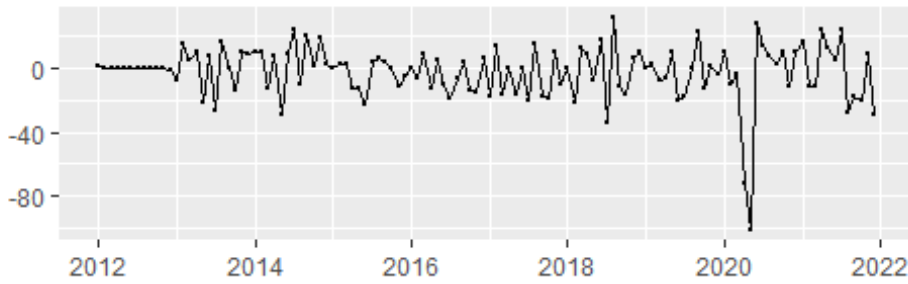
Training set error measures:

	ME	RMSE	MAE	MPE	MAPE	MASE
Training set	-2.472999	17.524	11.89993	-0.08808673	0.4423596	0.1253357

ACF1

Training set -0.01260262

Residuals from ARIMA(0,1,2)(0,1,1)[12]

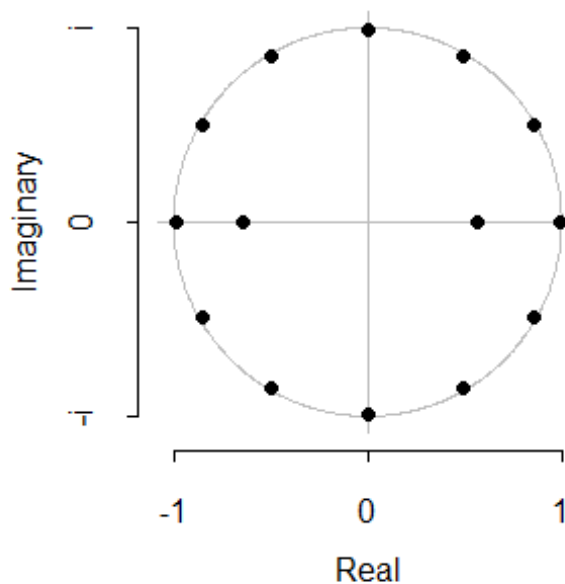


Ljung-Box test

data: Residuals from ARIMA(0,1,2)(0,1,1)[12]
 $Q^* = 21.503$, $df = 21$, $p\text{-value} = 0.4286$

Model df: 3. Total lags used: 24

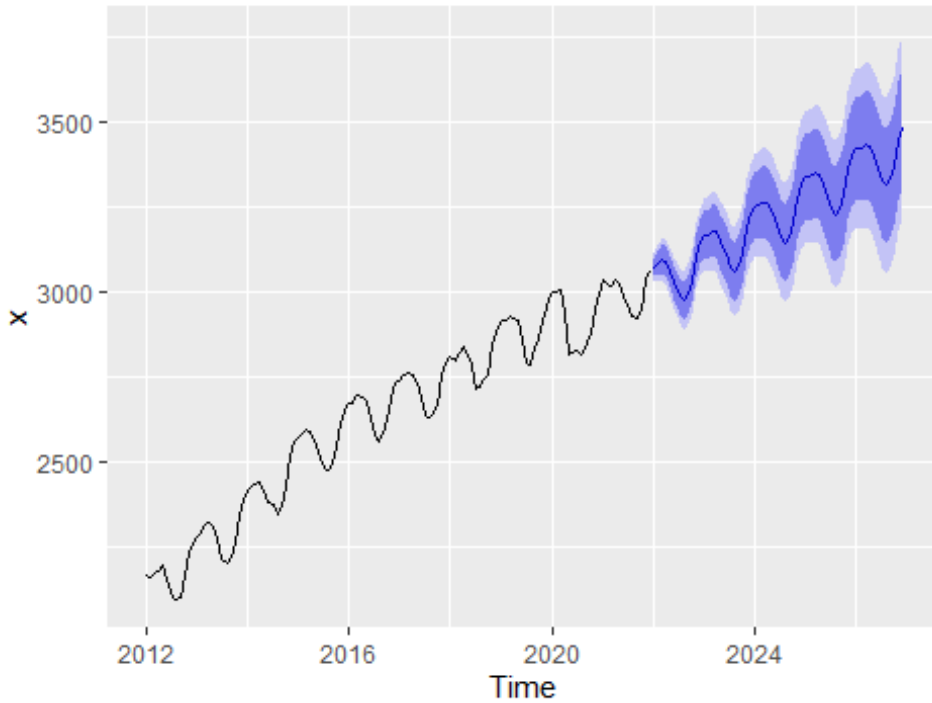
Inverse MA roots



ARIMA Model: 5 Year Forecast

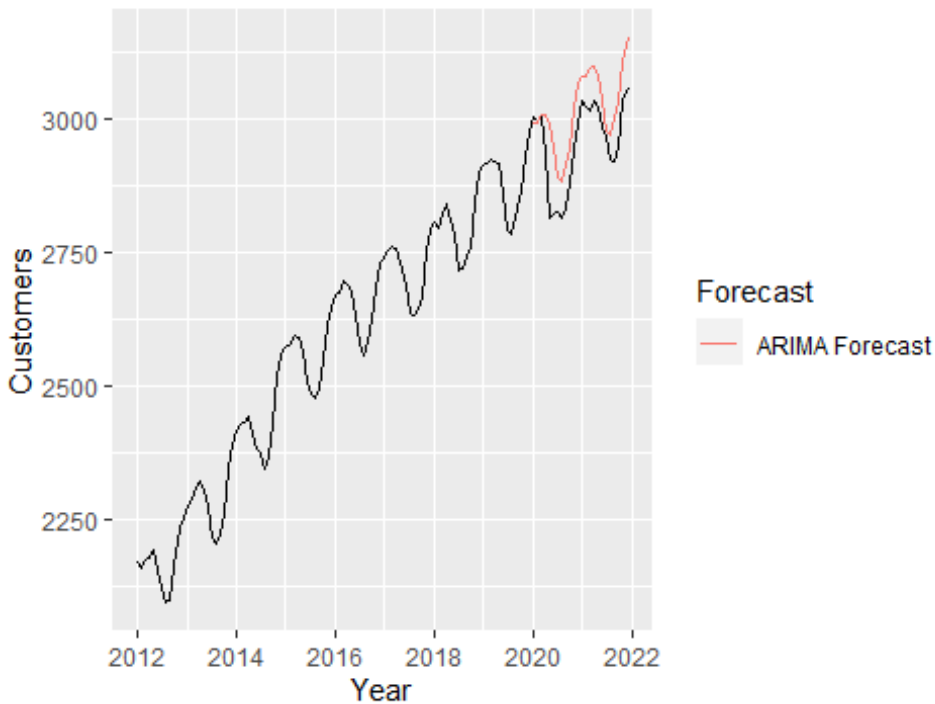
Below we fit & forecast 60 months into the future using an ARIMA (0,1,2)(0,1,1) model. This model only uses 1 difference, 1 Seasonal Moving Average, 1 Seasonal Difference, and is expected to be extremely accurate as previously shown. In the graph below we see the 80% and 95% Prediction Intervals bounding our forecast.

Forecasts from ARIMA(0,1,2)(0,1,1)[12]



Back-Testing

Commercial Client Backtesting: 2020-2021



Test Results

Below we see that the model performs roughly as expected for a “normal” year of 2019, and continues to have a high degree of accuracy in 2020 and 2021.

```
[1] "24Month Mean Absolute Error (MAE): 65.17"
```

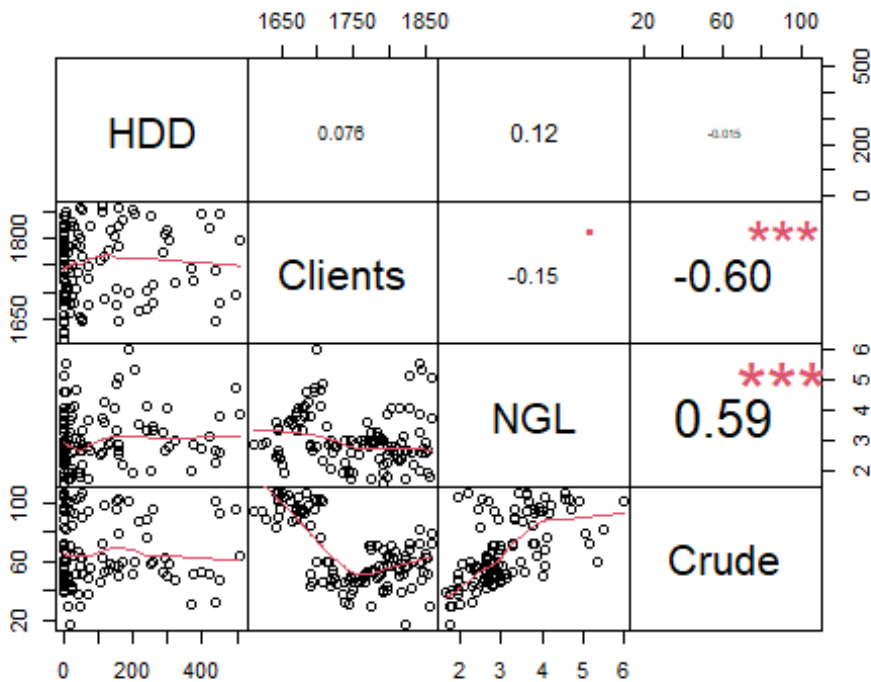
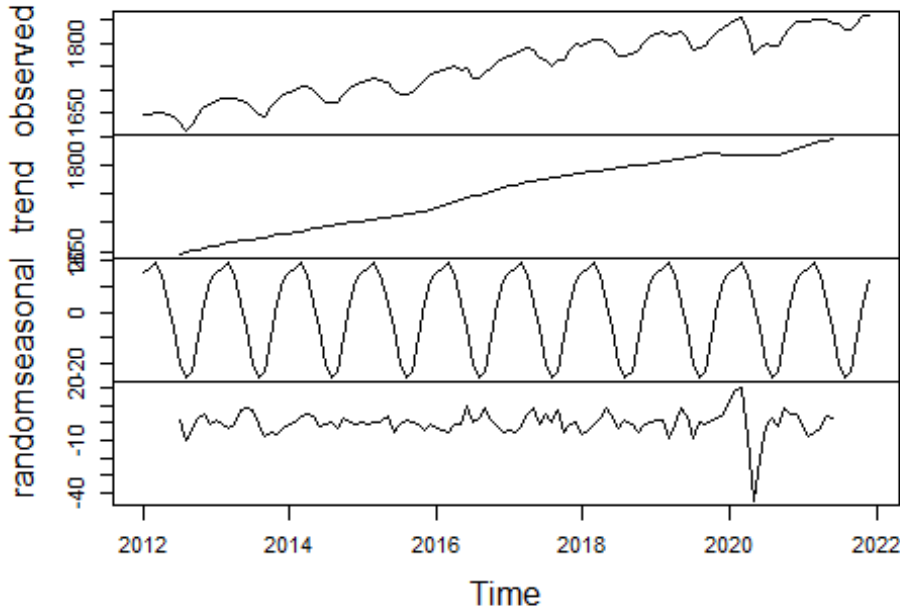
```
[1] "24Month Mean Accuracy: 97.77"
```

	Actual	Forecast	Absolute_Error	Accuracy
Jan 2020	3002	2991	11.04	99.6
Feb 2020	2997	2992	4.79	99.8
Mar 2020	3004	3007	2.82	99.9
Apr 2020	2937	3009	71.79	97.6
May 2020	2815	2993	178.46	93.7
Jun 2020	2820	2948	128.31	95.4
Jul 2020	2825	2889	63.66	97.7
Aug 2020	2813	2883	70.14	97.5
Sep 2020	2834	2913	79.30	97.2
Oct 2020	2880	2943	62.77	97.8
Nov 2020	2945	3019	73.88	97.5
Dec 2020	2992	3063	71.20	97.6
Jan 2021	3033	3079	46.16	98.5
Feb 2021	3021	3080	59.41	98.0
Mar 2021	3016	3095	79.02	97.4
Apr 2021	3036	3097	60.99	98.0
May 2021	3024	3082	57.67	98.1
Jun 2021	2986	3037	50.51	98.3
Jul 2021	2965	2977	11.86	99.6
Aug 2021	2925	2971	46.34	98.4
Sep 2021	2919	3002	82.51	97.2
Oct 2021	2947	3031	83.98	97.2
Nov 2021	3035	3107	72.08	97.6
Dec 2021	3056	3151	95.41	96.9

FPUC Large Volume Services (LVS, LVTS, LVTS2)

Customer Time-Series Decomposition

Decomposition of additive time series



ARIMA Model: Expected Accuracy

		ME	RMSE	MAE
Forecast Horizon	1	-1	6	4
Forecast Horizon	2	-1	6	5
Forecast Horizon	3	-1	7	5

Forecast Horizon	4	-2	7	6
Forecast Horizon	5	-4	14	8
Forecast Horizon	6	-6	16	10
Forecast Horizon	7	-6	16	10
Forecast Horizon	8	-7	15	10
Forecast Horizon	9	-8	16	10
Forecast Horizon	10	-10	17	12
Forecast Horizon	11	-10	18	12
Forecast Horizon	12	-11	18	12
Forecast Horizon	13	-12	17	13
Forecast Horizon	14	-13	18	13
Forecast Horizon	15	-13	20	15
Forecast Horizon	16	-14	20	15
Forecast Horizon	17	-15	20	16
Forecast Horizon	18	-16	21	17
Forecast Horizon	19	-16	21	17
Forecast Horizon	20	-16	22	18
Forecast Horizon	21	-17	22	17
Forecast Horizon	22	-18	22	18
Forecast Horizon	23	-18	23	18
Forecast Horizon	24	-19	24	19

ARIMA Model: Diagnostics

Series: x

ARIMA(1,0,0)(2,1,0)[12] with drift

Coefficients:

	ar1	sar1	sar2	drift
	0.7700	-0.6788	-0.2845	1.8258
s.e.	0.0637	0.0994	0.1264	0.1568

sigma² estimated as 74.61: log likelihood=-387.25

AIC=784.49 AICc=785.08 BIC=797.9

Training set error measures:

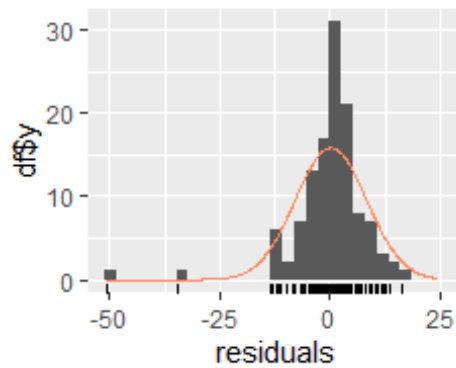
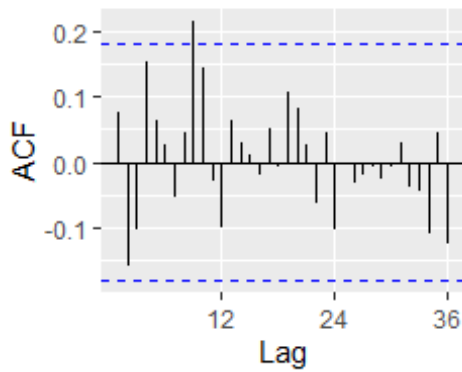
	ME	RMSE	MAE	MPE	MAPE	MASE
Training set	0.1976991	8.041368	5.113355	0.01287257	0.2889195	0.2148803

ACF1

Training set 0.07471428

FPUC-Rate 0625445

Residuals from ARIMA(1,0,0)(2,1,0)[12] with drift

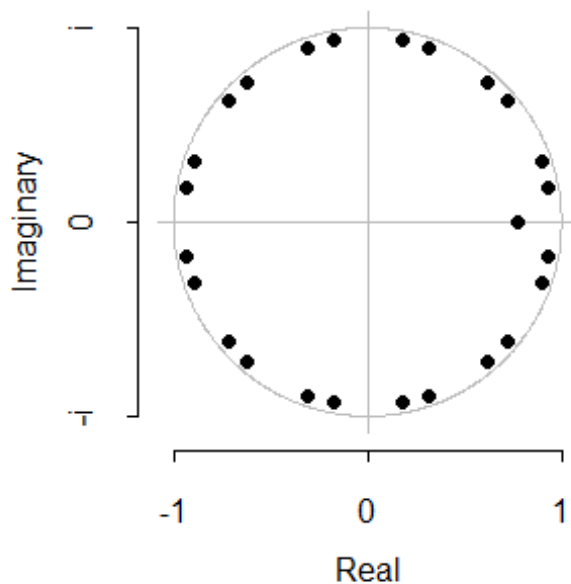


Ljung-Box test

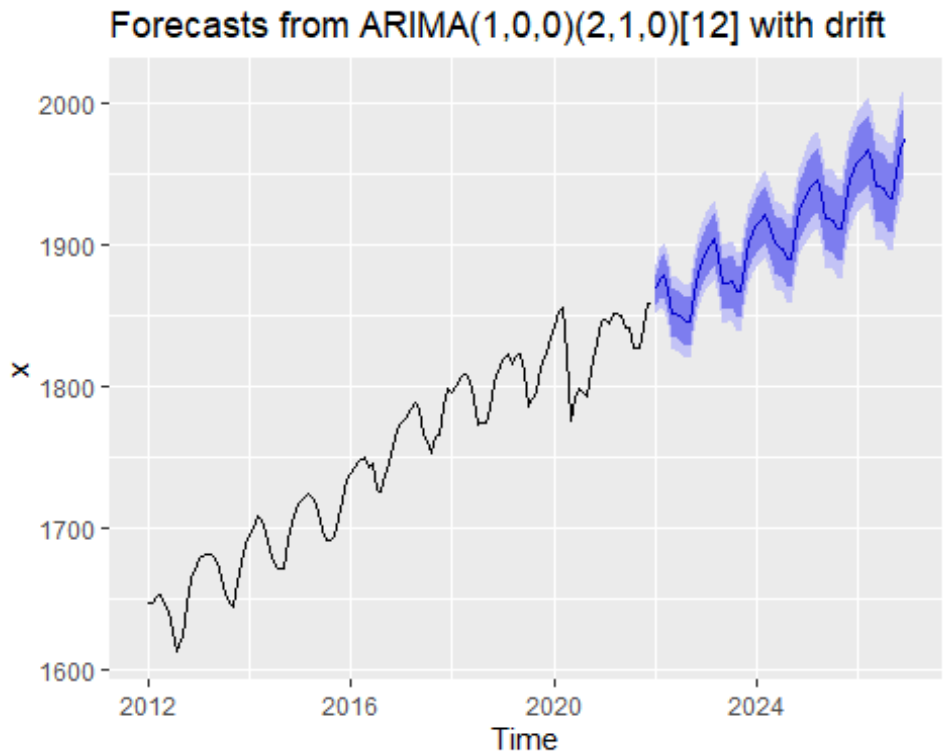
data: Residuals from ARIMA(1,0,0)(2,1,0)[12] with drift
 $Q^* = 25.879$, $df = 20$, $p\text{-value} = 0.1699$

Model df: 4. Total lags used: 24

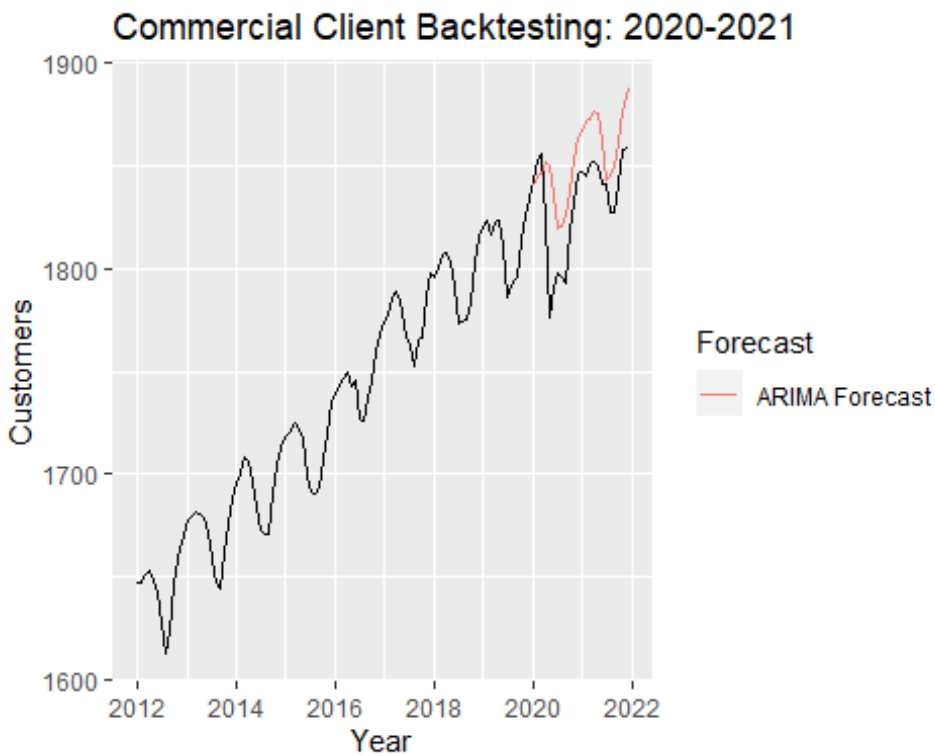
Inverse AR roots



ARIMA Model: 5 Year Forecast



Back-Testing



Test Results

Below we see that the model performs roughly as expected for a “normal” year of 2019, and continues to have a high degree of accuracy in 2020 and 2021.

FPUC-Rate 0625447

[1] "24Month Mean Absolute Error (MAE): 22.88"

[1] "24Month Mean Accuracy: 98.75"

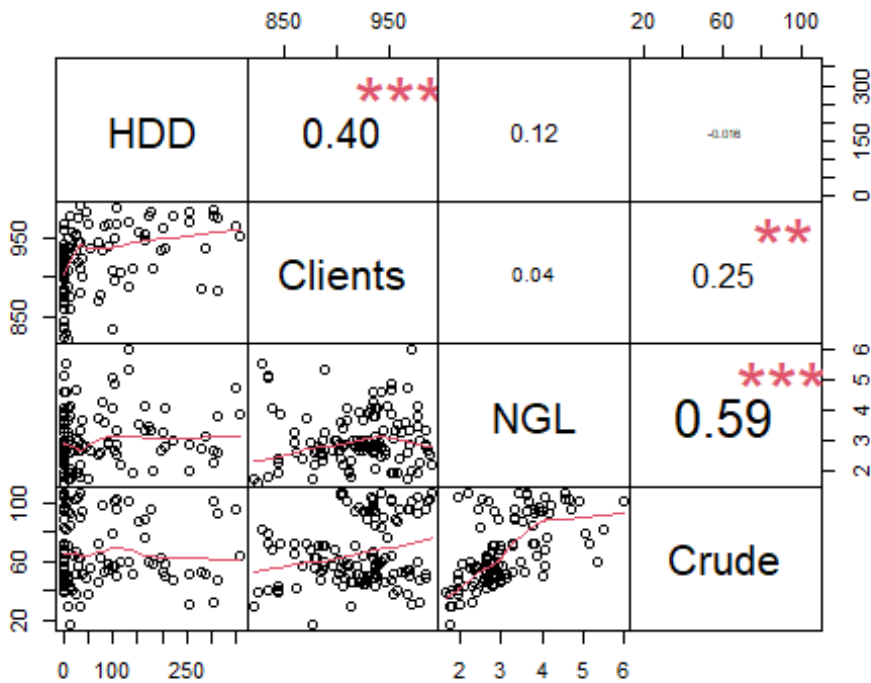
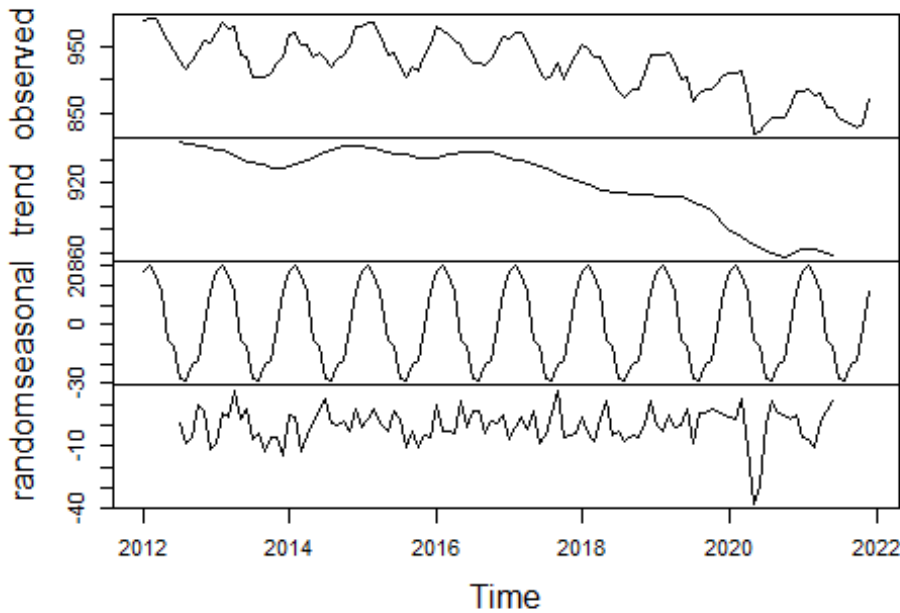
	Actual	Forecast	Absolute_Error	Accuracy
Jan 2020	1843	1840	2.77	99.8
Feb 2020	1853	1845	7.87	99.6
Mar 2020	1856	1846	9.98	99.5
Apr 2020	1823	1851	28.29	98.4
May 2020	1776	1850	74.14	95.8
Jun 2020	1791	1836	45.33	97.5
Jul 2020	1798	1819	21.33	98.8
Aug 2020	1796	1820	24.15	98.7
Sep 2020	1793	1826	33.13	98.2
Oct 2020	1818	1837	19.02	99.0
Nov 2020	1832	1853	20.72	98.9
Dec 2020	1846	1863	17.20	99.1
Jan 2021	1847	1867	19.79	98.9
Feb 2021	1845	1871	26.40	98.6
Mar 2021	1851	1872	21.42	98.8
Apr 2021	1852	1877	24.56	98.7
May 2021	1850	1875	24.95	98.7
Jun 2021	1841	1862	20.53	98.9
Jul 2021	1841	1843	1.99	99.9
Aug 2021	1827	1845	17.79	99.0
Sep 2021	1827	1849	21.93	98.8
Oct 2021	1841	1860	19.35	98.9
Nov 2021	1858	1876	18.38	99.0
Dec 2021	1859	1887	28.05	98.5

FPUC General Services1 (GS-1 & GSTS1)

Fort Meade customers excluded.

Customer Time-Series Decomposition

Decomposition of additive time series



ARIMA Model: Expected Accuracy

		ME	RMSE	MAE
Forecast Horizon	1	-2	10	8
Forecast Horizon	2	-3	11	9
Forecast Horizon	3	-4	12	10
Forecast Horizon	4	-5	13	11
Forecast Horizon	5	-8	18	14
Forecast Horizon	6	-10	22	17
Forecast Horizon	7	-11	23	17
Forecast Horizon	8	-11	23	18
Forecast Horizon	9	-12	24	19
Forecast Horizon	10	-14	25	20
Forecast Horizon	11	-15	26	21
Forecast Horizon	12	-16	26	22
Forecast Horizon	13	-17	27	23
Forecast Horizon	14	-18	27	23
Forecast Horizon	15	-19	28	24
Forecast Horizon	16	-19	28	24
Forecast Horizon	17	-20	28	24
Forecast Horizon	18	-20	27	24
Forecast Horizon	19	-20	26	23
Forecast Horizon	20	-20	25	22
Forecast Horizon	21	-20	25	21
Forecast Horizon	22	-21	25	22
Forecast Horizon	23	-22	26	22
Forecast Horizon	24	-22	26	23

ARIMA Model: Diagnostics

In this section we evaluate the diagnostics of the ARIMA Model. Below we see that the model fails the Ljung-Box Test and therefore we can determine the data is independently distributed. In addition, we see from the graphs that the lagged values are not auto-correlated with one another, and the residuals are normally distributed.

Series: x

ARIMA(0,1,2)(1,1,1)[12]

Coefficients:

	ma1	ma2	sar1	sma1
	-0.3040	-0.1908	-0.2488	-0.7001
s.e.	0.0939	0.0871	0.1580	0.1755

sigma² estimated as 113.5: log likelihood=-409.33

AIC=828.65 AICc=829.25 BIC=842.02

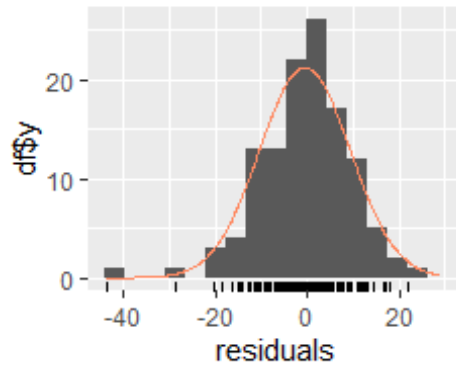
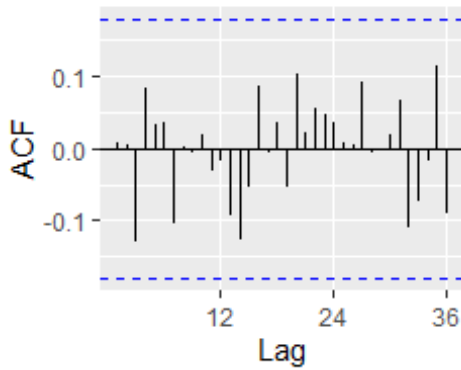
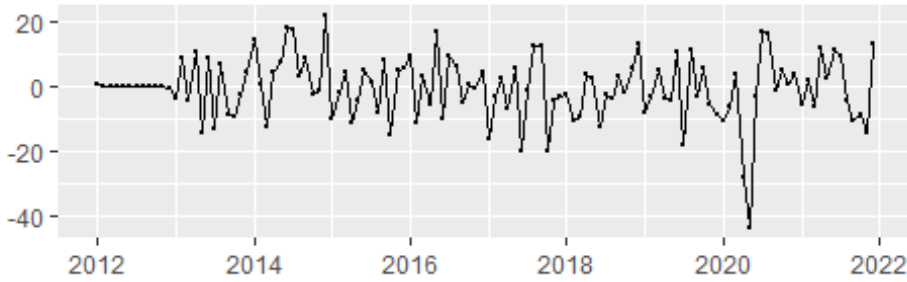
Training set error measures:

	ME	RMSE	MAE	MPE	MAPE	MASE
Training set	-0.5066976	9.86858	7.364808	-0.06322886	0.8106228	0.3883785

ACF1

Training set 0.008085022

Residuals from ARIMA(0,1,2)(1,1,1)[12]

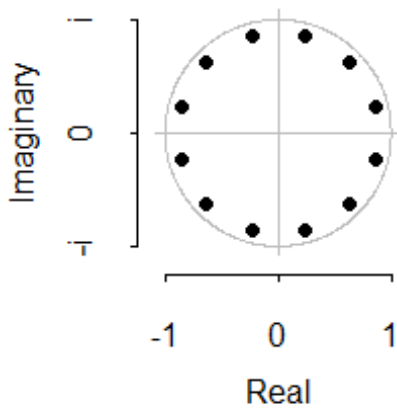


Ljung-Box test

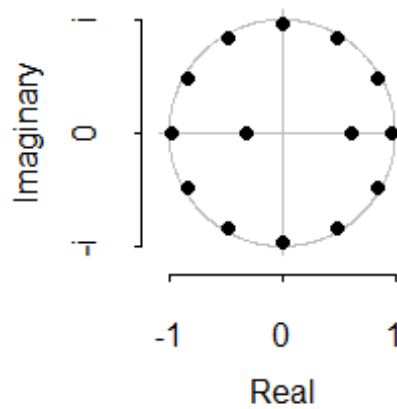
data: Residuals from ARIMA(0,1,2)(1,1,1)[12]
 $Q^* = 13.029$, $df = 20$, $p\text{-value} = 0.8761$

Model df: 4. Total lags used: 24

Inverse AR roots

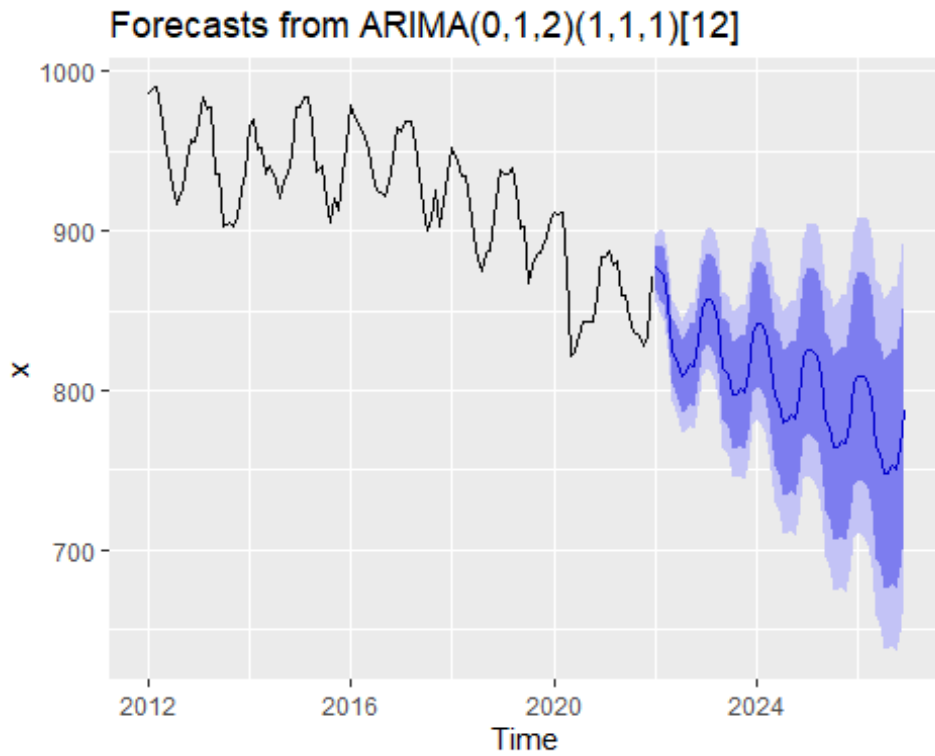


Inverse MA roots



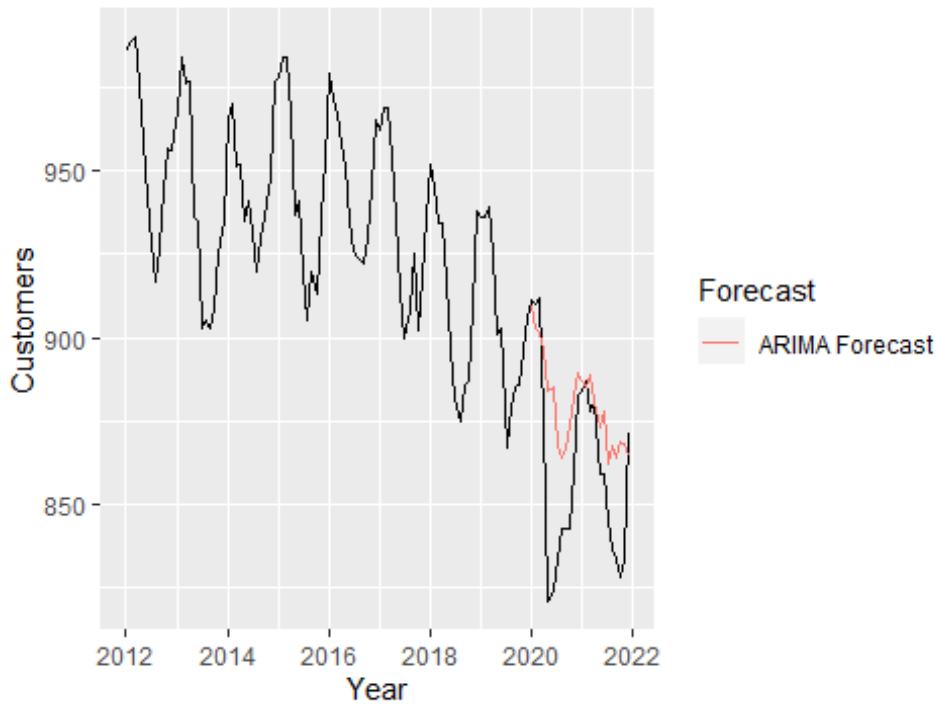
ARIMA Model: 5 Year Forecast

Below we fit & forecast 60 months into the future using an ARIMA (0,1,2)(1,1,1) model.



Back-Testing

Commercial Client Backtesting: 2020-2021



Test Results

Below we see that the model performs roughly as expected for a “normal” year of 2019, and continues to have a high degree of accuracy in 2020 and 2021.

```
[1] "24Month Mean Absolute Error (MAE): 21.28"
```

```
[1] "24Month Mean Accuracy: 97.47"
```

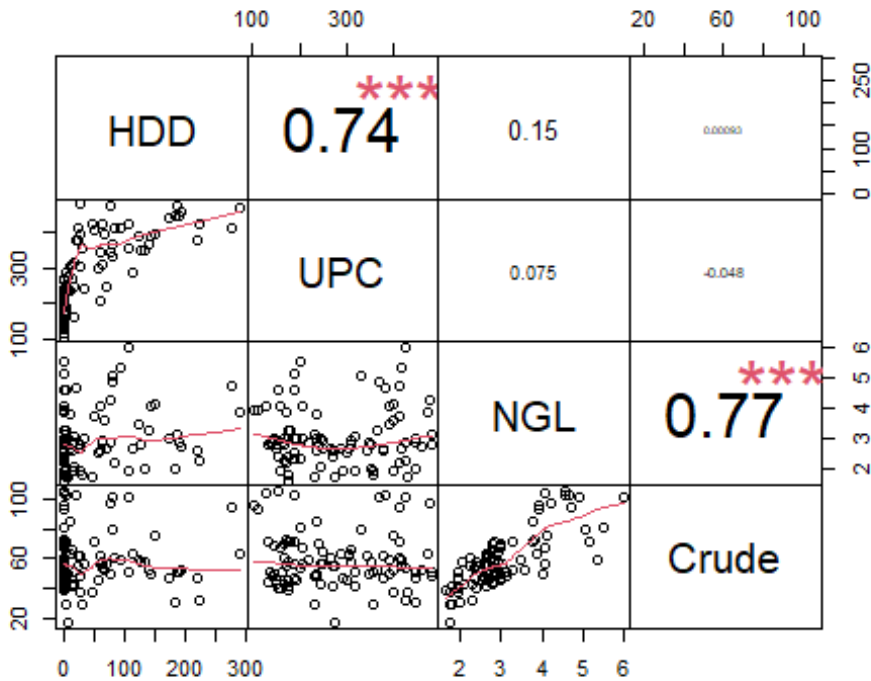
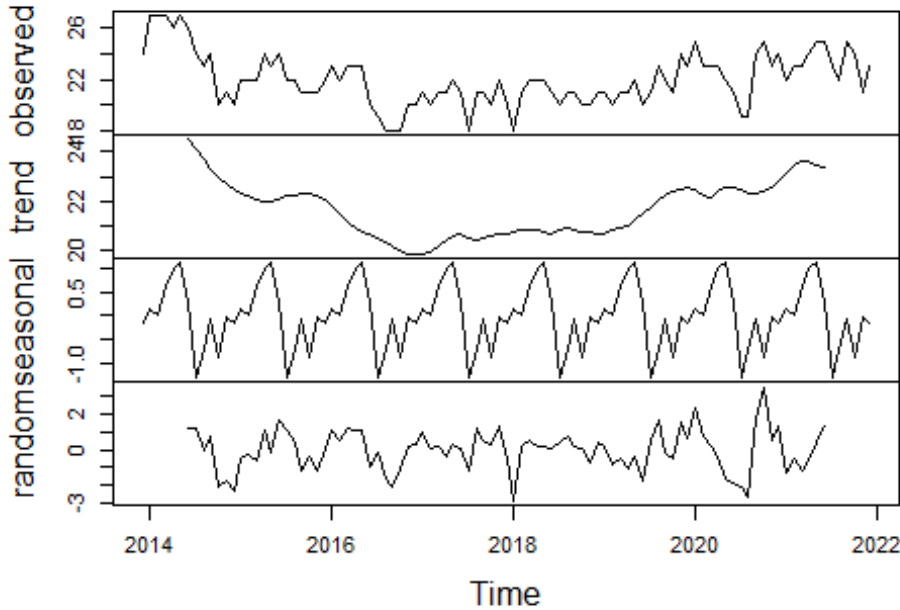
	Actual	Forecast	Absolute_Error	Accuracy
Jan 2020	911	909	1.75	99.8
Feb 2020	910	903	7.12	99.2
Mar 2020	912	902	10.38	98.9
Apr 2020	876	897	20.78	97.6
May 2020	821	884	63.10	92.3
Jun 2020	824	885	61.33	92.6
Jul 2020	834	868	33.82	95.9
Aug 2020	843	864	21.24	97.5
Sep 2020	843	867	23.83	97.2
Oct 2020	843	874	30.67	96.4
Nov 2020	860	882	21.96	97.4
Dec 2020	883	889	6.27	99.3
Jan 2021	884	887	3.31	99.6
Feb 2021	887	885	1.98	99.8
Mar 2021	878	889	10.89	98.8
Apr 2021	881	881	0.26	100.0
May 2021	859	873	14.31	98.3
Jun 2021	859	878	18.92	97.8
Jul 2021	845	862	17.01	98.0
Aug 2021	837	868	30.73	96.3
Sep 2021	834	864	29.84	96.4
Oct 2021	828	869	40.68	95.1
Nov 2021	834	868	34.17	95.9
Dec 2021	871	865	6.34	99.3

Fort Meade General Services1 (GS-1 & GSTS1)

Fort Meade customers only

Customer Time-Series Decomposition

Decomposition of additive time series



ARIMA Model: Expected Accuracy

	ME	RMSE	MAE
Forecast Horizon 1	0	2	1
Forecast Horizon 2	1	2	1
Forecast Horizon 3	1	2	1
Forecast Horizon 4	1	2	1
Forecast Horizon 5	1	2	2
Forecast Horizon 6	1	2	1
Forecast Horizon 7	1	2	2
Forecast Horizon 8	1	2	2
Forecast Horizon 9	1	2	2
Forecast Horizon 10	1	2	2
Forecast Horizon 11	1	2	2
Forecast Horizon 12	1	2	2
Forecast Horizon 13	1	2	2
Forecast Horizon 14	1	2	2
Forecast Horizon 15	1	3	2
Forecast Horizon 16	2	3	2
Forecast Horizon 17	2	3	2
Forecast Horizon 18	2	3	2
Forecast Horizon 19	2	3	2
Forecast Horizon 20	2	3	2
Forecast Horizon 21	2	3	2
Forecast Horizon 22	2	3	2
Forecast Horizon 23	2	3	2
Forecast Horizon 24	2	3	2

ARIMA Model: Diagnostics

In this section we evaluate the diagnostics of the ARIMA Model. Below we see that the model fails the Ljung-Box Test and therefore we can determine the data is independently distributed. In addition, we see from the graphs that the lagged values are not auto-correlated with one another, and the residuals are normally distributed.

Series: x

ARIMA(1,1,1)(1,0,0)[12]

Coefficients:

	ar1	ma1	sar1
	0.5450	-0.8785	0.1712
s.e.	0.1309	0.0738	0.1134

sigma² estimated as 2.043: log likelihood=-169.4

AIC=346.8 AICc=347.24 BIC=357.06

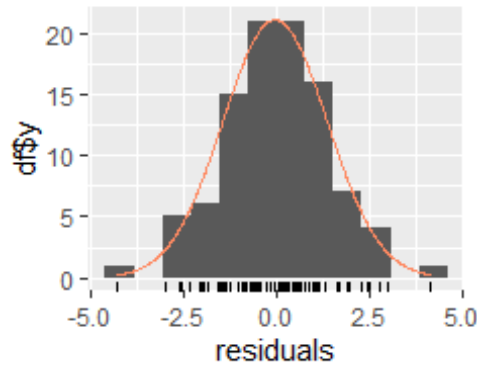
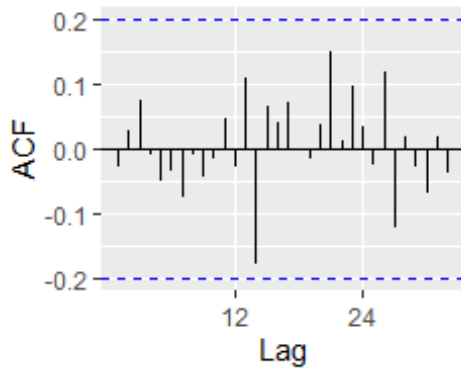
Training set error measures:

	ME	RMSE	MAE	MPE	MAPE	MASE
Training set	-0.053021	1.399699	1.095254	-0.5677927	5.052239	0.589219

ACF1

Training set -0.02706726

Residuals from ARIMA(1,1,1)(1,0,0)[12]

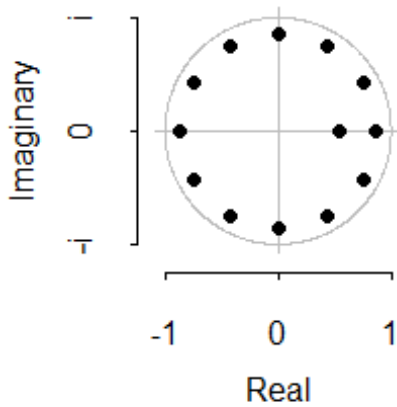


Ljung-Box test

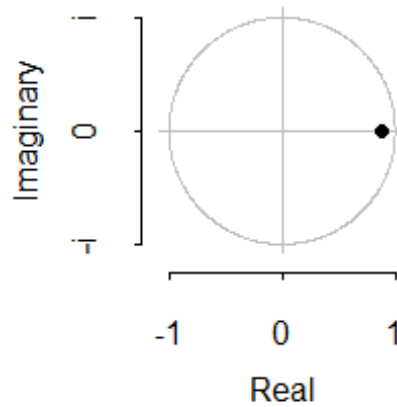
data: Residuals from ARIMA(1,1,1)(1,0,0)[12]
 $Q^* = 8.6502$, $df = 16$, $p\text{-value} = 0.9271$

Model df: 3. Total lags used: 19

Inverse AR roots



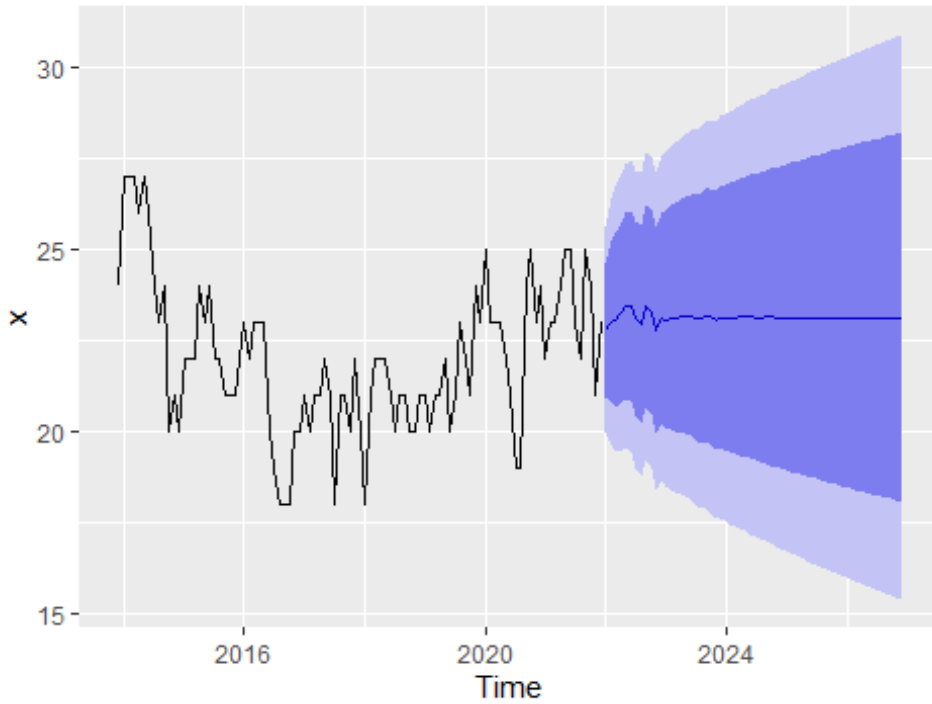
Inverse MA roots



ARIMA Model: 5 Year Forecast

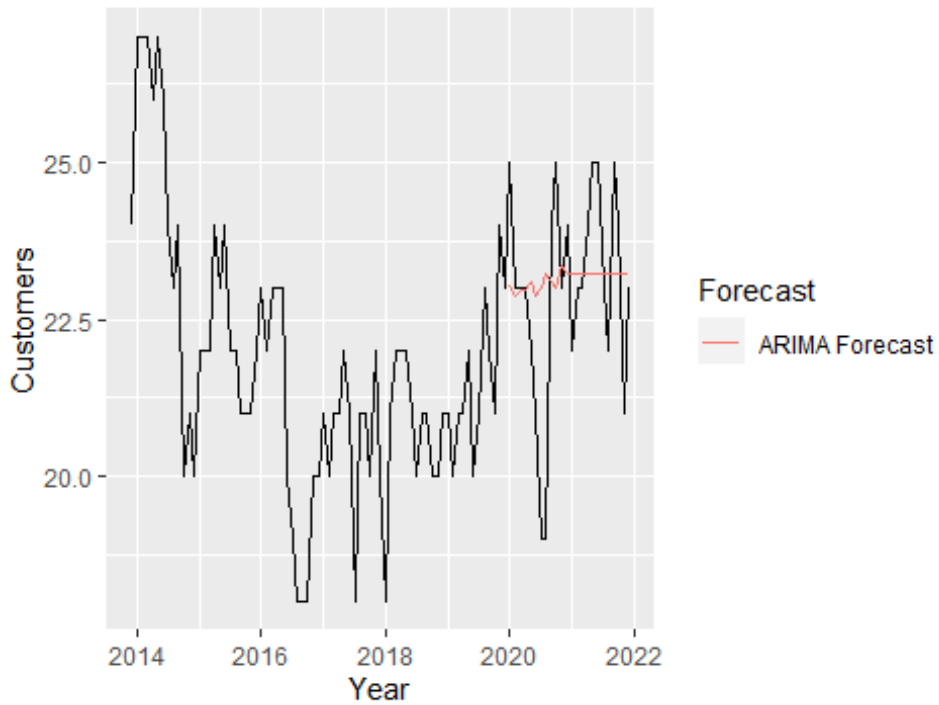
Below we fit & forecast 60 months into the future using an ARIMA (1,1,1)(1,0,0) model.

Forecasts from ARIMA(1,1,1)(1,0,0)[12]



Back-Testing

Commercial Client Backtesting: 2020-2021



Test Results

Below we see that the model performs roughly as expected for a “normal” year of 2019, and continues to have a high degree of accuracy in 2020 and 2021.

```
[1] "24Month Mean Absolute Error (MAE): 1.24"
```

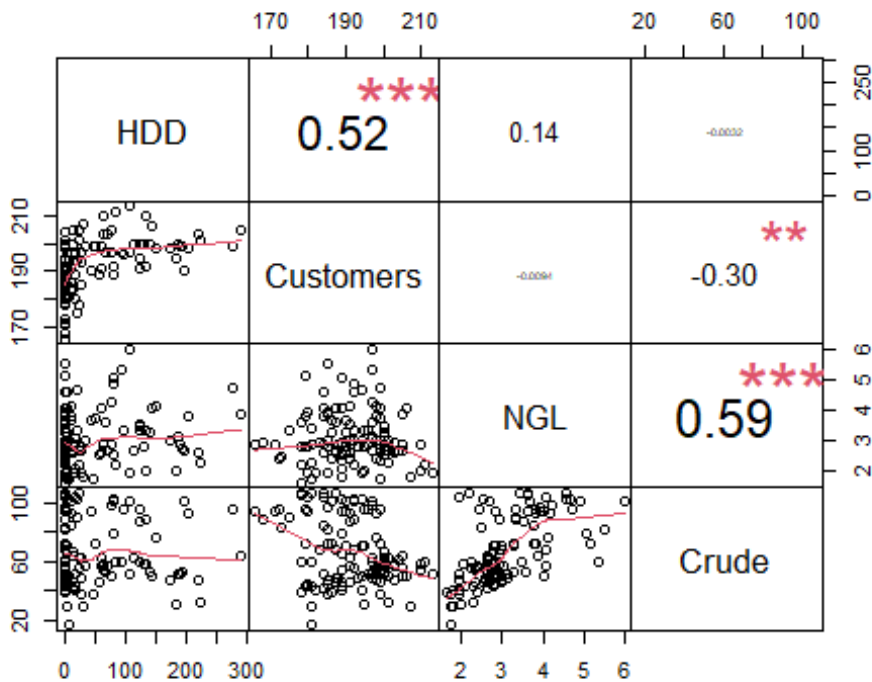
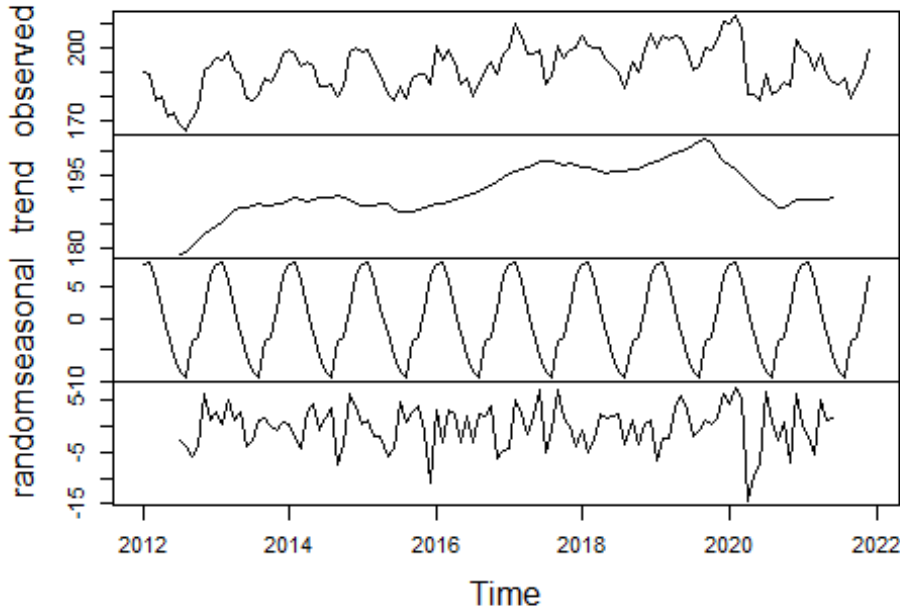
```
[1] "24Month Mean Accuracy: 94.34"
```

	Actual	Forecast	Absolute_Error	Accuracy
Jan 2020	25	23	1.97	92.1
Feb 2020	23	23	0.13	99.4
Mar 2020	23	23	0.02	99.9
Apr 2020	23	23	0.02	99.9
May 2020	22	23	1.09	95.0
Jun 2020	21	23	1.88	91.0
Jul 2020	19	23	4.00	78.9
Aug 2020	19	23	4.22	77.8
Sep 2020	24	23	0.90	96.2
Oct 2020	25	23	2.00	92.0
Nov 2020	23	23	0.34	98.5
Dec 2020	24	23	0.79	96.7
Jan 2021	22	23	1.21	94.5
Feb 2021	23	23	0.21	99.1
Mar 2021	23	23	0.21	99.1
Apr 2021	24	23	0.79	96.7
May 2021	25	23	1.79	92.8
Jun 2021	25	23	1.79	92.8
Jul 2021	23	23	0.21	99.1
Aug 2021	22	23	1.21	94.5
Sep 2021	25	23	1.79	92.8
Oct 2021	24	23	0.79	96.7
Nov 2021	21	23	2.21	89.5
Dec 2021	23	23	0.21	99.1

CFG Firm Transportation Services (FTS-1)

Customer Time-Series Decomposition

Decomposition of additive time series



ARIMA Model: Expected Accuracy

In this section we evaluate the expected accuracy of a Seasonal ARIMA Model using cross-validation. ARIMA is an acronym for 'Autoregressive Integrated Moving Average' which is a widely used Time-Series forecasting model that utilizes the recent values to predict outward.

Here we evaluate model accuracy by using cross-validation and rolling forecasts throughout the time-series to determine our expected accuracy over a 24 Month period.

	ME	RMSE	MAE
Forecast Horizon 1	0	5	4
Forecast Horizon 2	1	5	4
Forecast Horizon 3	0	4	4
Forecast Horizon 4	0	6	4
Forecast Horizon 5	-1	7	5
Forecast Horizon 6	-1	8	5
Forecast Horizon 7	-2	8	5
Forecast Horizon 8	-2	8	5
Forecast Horizon 9	-3	9	6
Forecast Horizon 10	-3	9	6
Forecast Horizon 11	-4	9	7
Forecast Horizon 12	-4	9	7
Forecast Horizon 13	-4	10	7
Forecast Horizon 14	-5	10	7
Forecast Horizon 15	-5	10	8
Forecast Horizon 16	-5	10	8
Forecast Horizon 17	-6	10	8
Forecast Horizon 18	-6	10	8
Forecast Horizon 19	-6	10	8
Forecast Horizon 20	-7	10	8
Forecast Horizon 21	-7	11	9
Forecast Horizon 22	-7	11	9
Forecast Horizon 23	-8	12	9
Forecast Horizon 24	-8	12	9

ARIMA Model: Diagnostics

In this section we evaluate the diagnostics of the ARIMA Model. Below we see that the model fails the Ljung-Box Test and therefore we can determine the data is independently distributed. In addition, we see from the graphs that the lagged values are not auto-correlated with one another, and the residuals are normally distributed.

```
Series: x
ARIMA(0,1,2)(2,1,0)[12]

Coefficients:
      ma1      ma2      sar1      sar2
    -0.5312 -0.1461 -0.7304 -0.2622
s.e.   0.0941  0.0932  0.0976  0.1097

sigma^2 estimated as 35.66:  log likelihood=-344.57
AIC=699.15  AICc=699.74  BIC=712.51

Training set error measures:
      ME      RMSE      MAE      MPE      MAPE      MASE
```

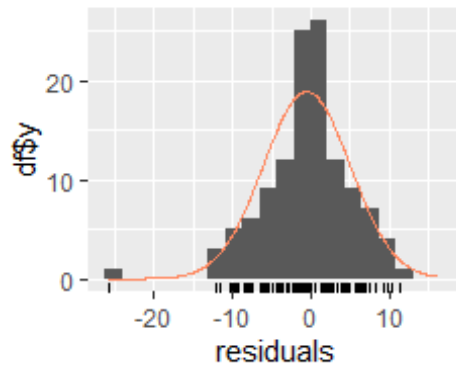
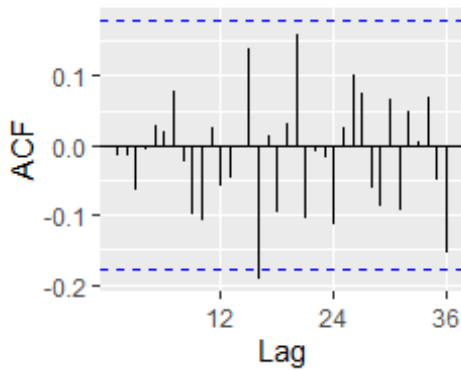
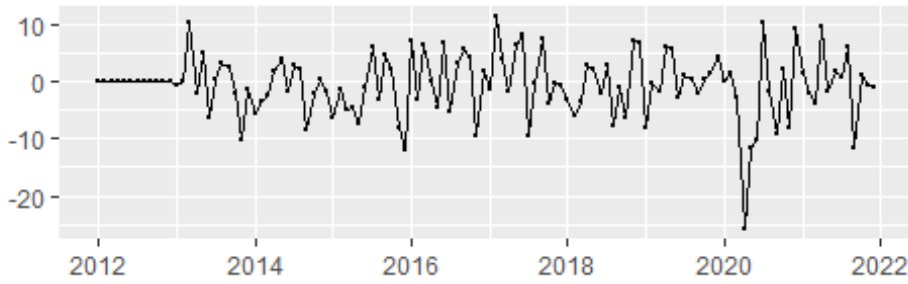
FPUC-Rate 0625460

Training set -0.5663027 5.532242 3.975449 -0.3420511 2.082338 0.5561509

ACF1

Training set -0.01412129

Residuals from ARIMA(0,1,2)(2,1,0)[12]



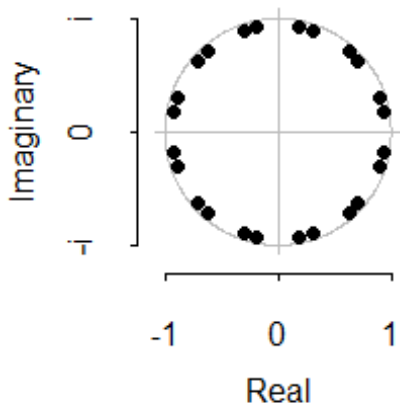
Ljung-Box test

data: Residuals from ARIMA(0,1,2)(2,1,0)[12]

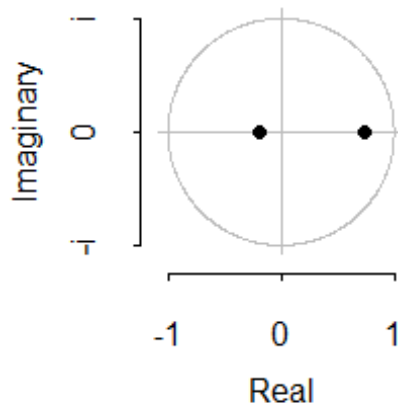
$Q^* = 22.143$, $df = 20$, $p\text{-value} = 0.3328$

Model df: 4. Total lags used: 24

Inverse AR roots



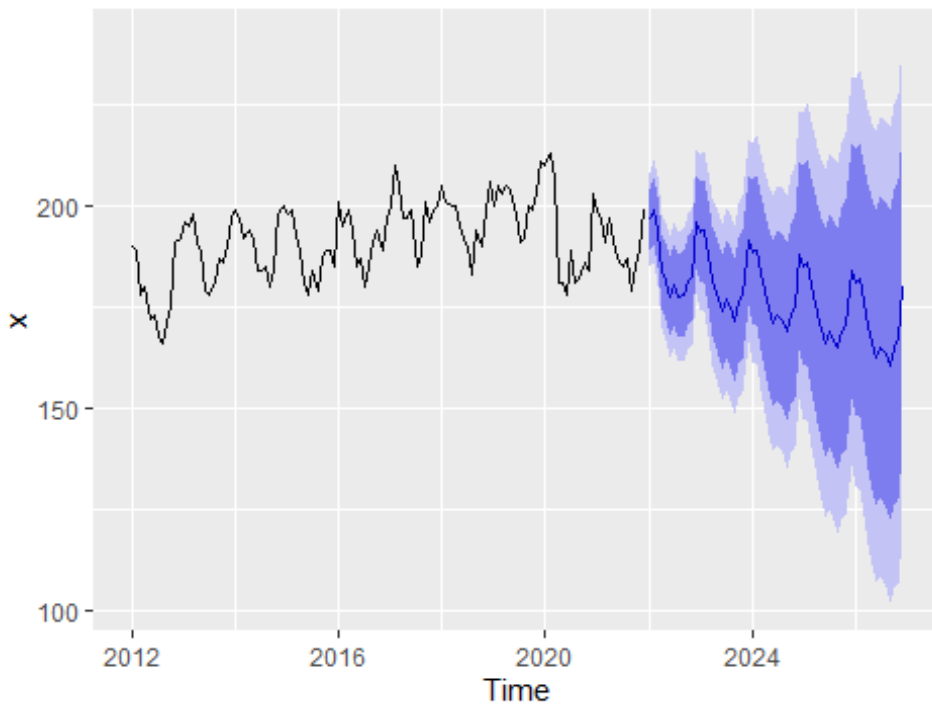
Inverse MA roots



ARIMA Model: 5 Year Forecast

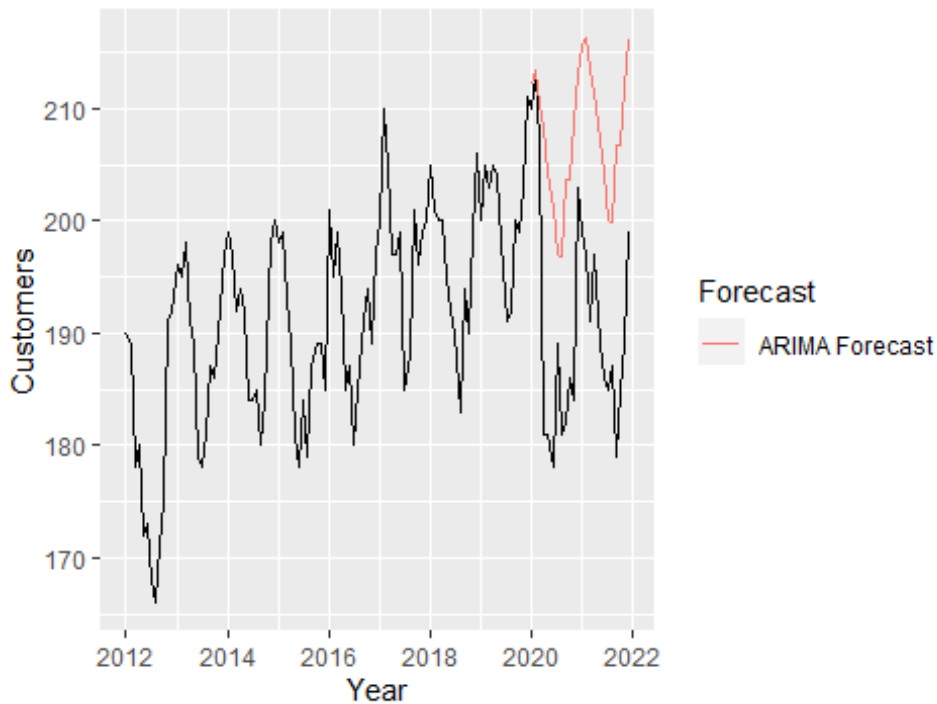
Below we fit & forecast 60 months into the future using an ARIMA (0,1,2)(2,1,0) model. In the graph below we see the 80% and 95% Prediction Intervals bounding our forecast.

Forecasts from ARIMA(0,1,2)(2,1,0)[12]



Back-Testing

Commercial Client Backtesting: 2020-2021



Test Results

Below we see that the model performs roughly as expected for a “normal” year of 2019, and continues to have a high degree of accuracy in 2020 and 2021.

```
[1] "24Month Mean Absolute Error (MAE): 16.84"
```

```
[1] "24Month Mean Accuracy: 90.99"
```

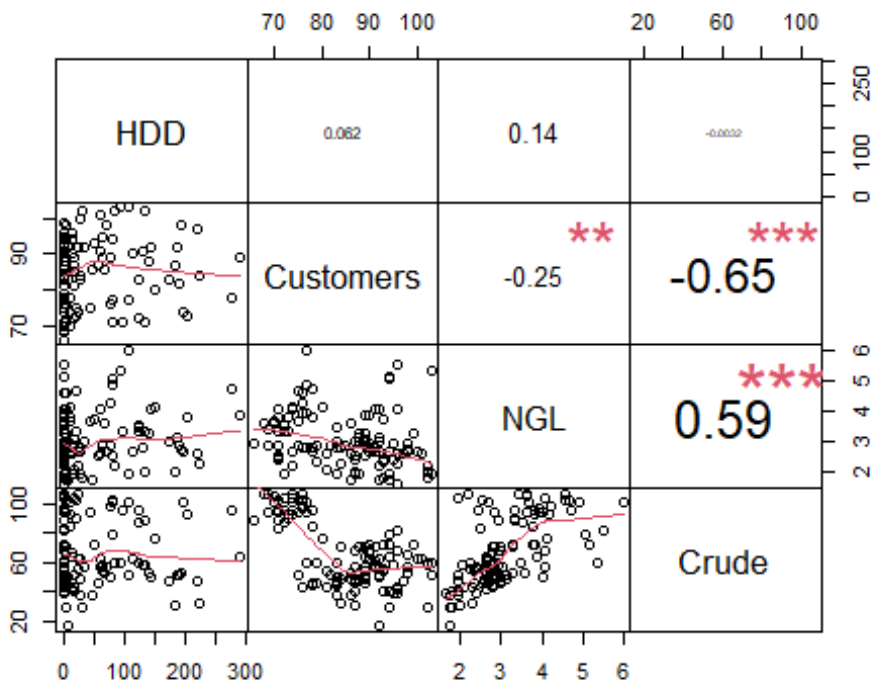
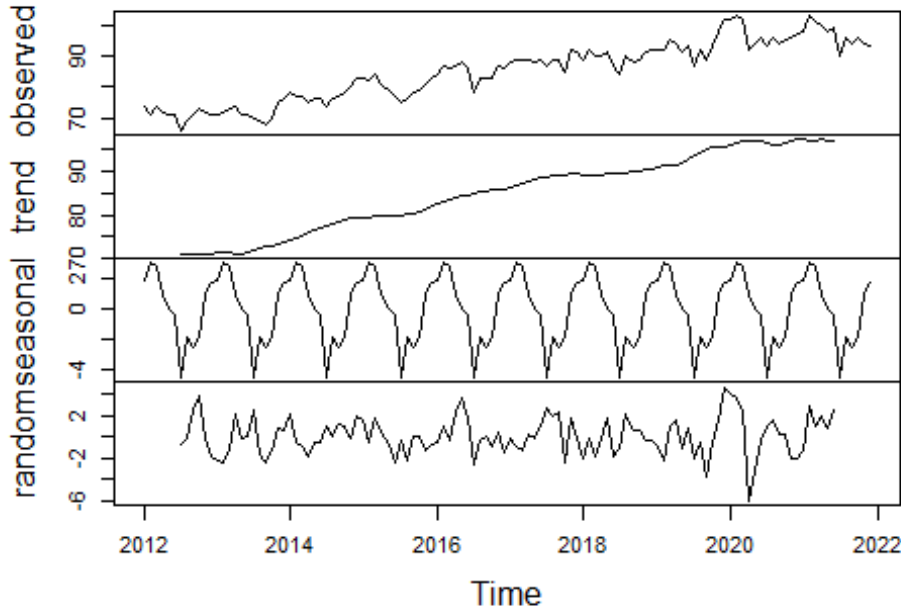
	Actual	Forecast	Absolute_Error	Accuracy
Jan 2020	210	212	2.13	99.0
Feb 2020	213	213	0.32	99.8
Mar 2020	207	210	3.39	98.4
Apr 2020	181	208	27.36	84.9
May 2020	181	204	23.16	87.2
Jun 2020	178	201	23.10	87.0
Jul 2020	189	197	7.96	95.8
Aug 2020	181	197	15.75	91.3
Sep 2020	182	204	21.71	88.1
Oct 2020	186	204	17.61	90.5
Nov 2020	184	209	24.95	86.4
Dec 2020	203	213	10.01	95.1
Jan 2021	199	216	16.62	91.6
Feb 2021	197	216	19.26	90.2
Mar 2021	191	214	22.53	88.2
Apr 2021	197	211	14.42	92.7
May 2021	189	207	18.25	90.3
Jun 2021	186	204	18.18	90.2
Jul 2021	185	200	15.05	91.9
Aug 2021	187	200	12.83	93.1
Sep 2021	179	207	27.80	84.5

Oct 2021	185	207	21.69	88.3
Nov 2021	189	212	23.03	87.8
Dec 2021	199	216	17.10	91.4

CFG Firm Transportation Services (FTS-2)

Customer Time-Series Decomposition

Decomposition of additive time series



ARIMA Model: Expected Accuracy

In this section we evaluate the expected accuracy of a Seasonal ARIMA Model using cross-validation. ARIMA is an acronym for 'Autoregressive Integrated Moving Average' which is a widely used Time-Series forecasting model that utilizes the recent values to predict outward.

Here we evaluate model accuracy by using cross-validation and rolling forecasts throughout the time-series to determine our expected accuracy over a 24 Month period.

	ME	RMSE	MAE
Forecast Horizon 1	0	2	2
Forecast Horizon 2	0	3	2
Forecast Horizon 3	0	3	3
Forecast Horizon 4	0	4	3
Forecast Horizon 5	0	4	3
Forecast Horizon 6	0	4	3
Forecast Horizon 7	-1	4	3
Forecast Horizon 8	-1	4	3
Forecast Horizon 9	-1	4	3
Forecast Horizon 10	-1	4	3
Forecast Horizon 11	-1	4	3
Forecast Horizon 12	-1	4	3
Forecast Horizon 13	-1	4	3
Forecast Horizon 14	-1	3	3
Forecast Horizon 15	-1	3	3
Forecast Horizon 16	-1	3	3
Forecast Horizon 17	-1	3	3
Forecast Horizon 18	-1	3	3
Forecast Horizon 19	-1	3	3
Forecast Horizon 20	-1	4	3
Forecast Horizon 21	-2	4	3
Forecast Horizon 22	-2	3	3
Forecast Horizon 23	-2	4	3
Forecast Horizon 24	-2	4	3

ARIMA Model: Diagnostics

In this section we evaluate the diagnostics of the ARIMA Model. Below we see that the model fails the Ljung-Box Test and therefore we can determine the data is independently distributed. In addition, we see from the graphs that the lagged values are not auto-correlated with one another, and the residuals are normally distributed.

```
Series: x
ARIMA(1,1,1)(2,0,0)[12]

Coefficients:
      ar1      ma1      sar1      sar2
    0.5954 -0.8705  0.2882  0.3367
s.e.  0.1236  0.0741  0.0912  0.0980

sigma^2 estimated as 5.481:  log likelihood=-270.87
AIC=551.74  AICc=552.27  BIC=565.63

Training set error measures:
      ME      RMSE      MAE      MPE      MAPE      MASE
```

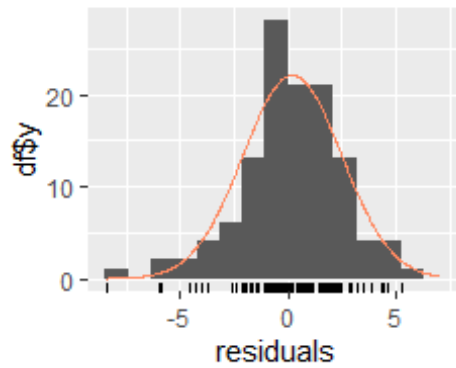
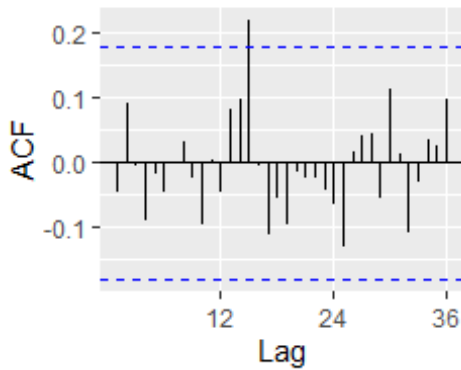
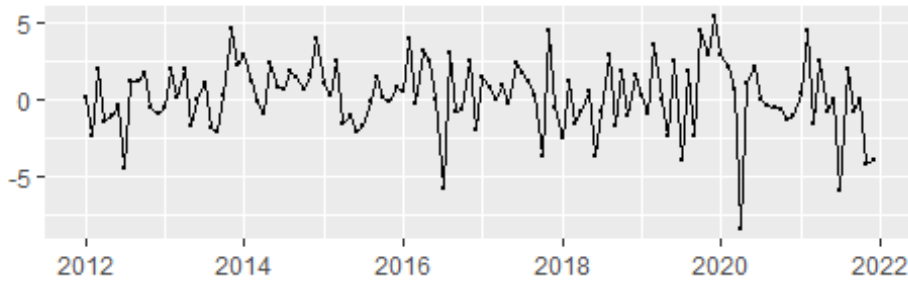

FPUC-Rate 0625465

Training set 0.1866313 2.291785 1.736264 0.1824327 2.041302 0.4845389

ACF1

Training set -0.04640503

Residuals from ARIMA(1,1,1)(2,0,0)[12]



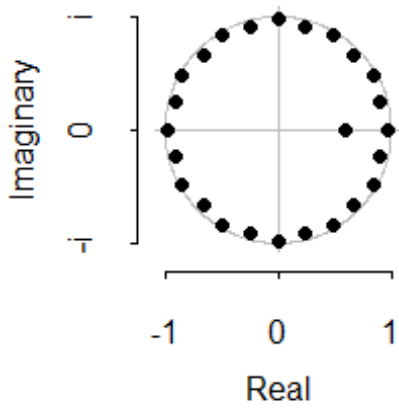
Ljung-Box test

data: Residuals from ARIMA(1,1,1)(2,0,0)[12]

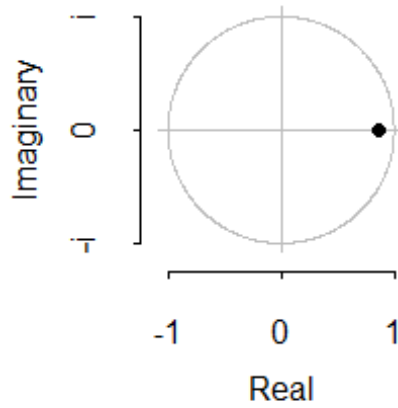
$Q^* = 17.899$, $df = 20$, $p\text{-value} = 0.594$

Model df: 4. Total lags used: 24

Inverse AR roots



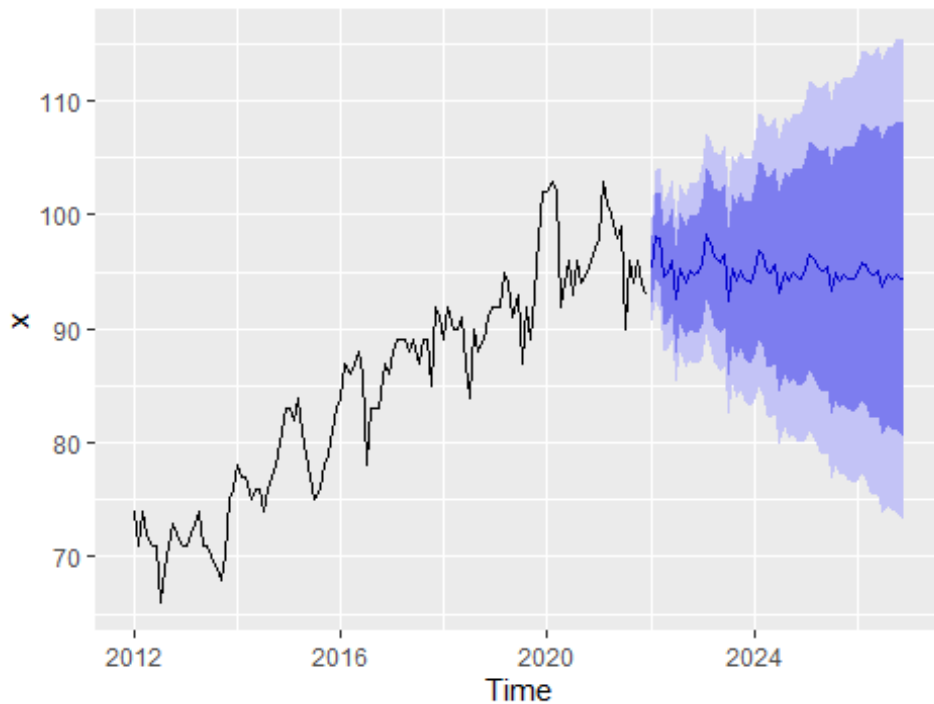
Inverse MA roots



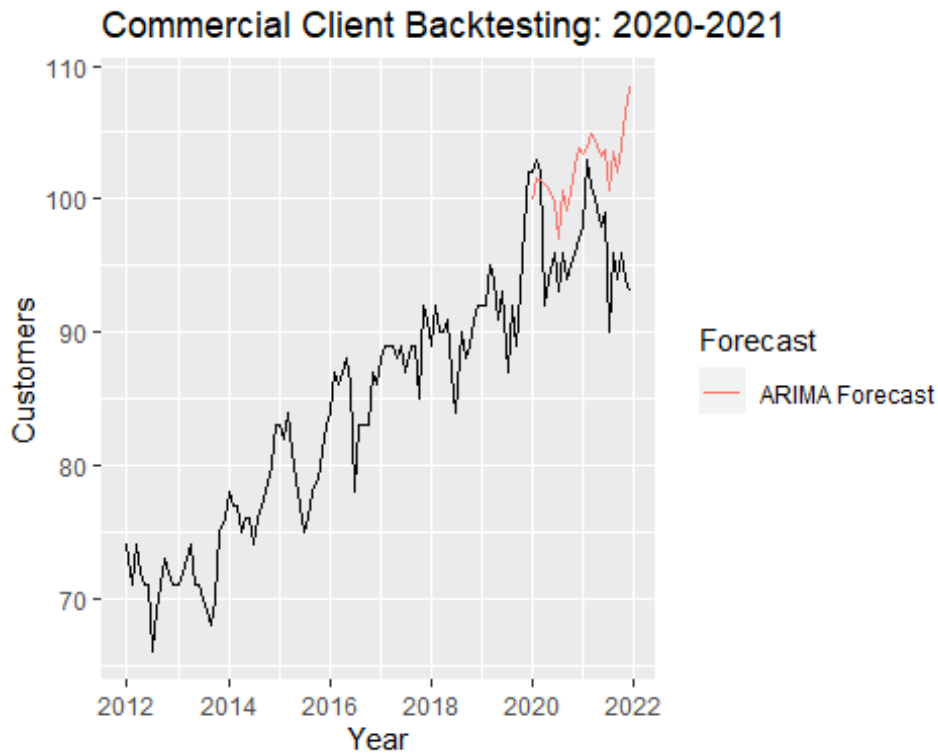
ARIMA Model: 5 Year Forecast

Below we fit & forecast 60 months into the future using an ARIMA (1,1,1)(2,0,0) model. In the graph below we see the 80% and 95% Prediction Intervals bounding our forecast.

Forecasts from ARIMA(1,1,1)(2,0,0)[12]



Back-Testing



Test Results

Below we see that the model performs roughly as expected for a “normal” year of 2019, and continues to have a high degree of accuracy in 2020 and 2021.

[1] "24Month Mean Absolute Error (MAE): 5.96"

[1] "24Month Mean Accuracy: 93.74"

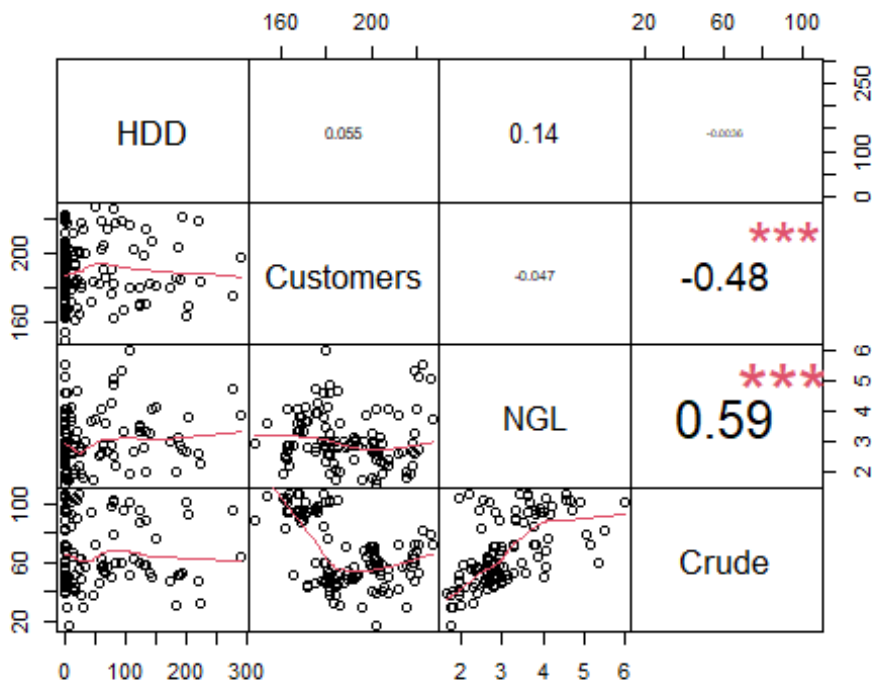
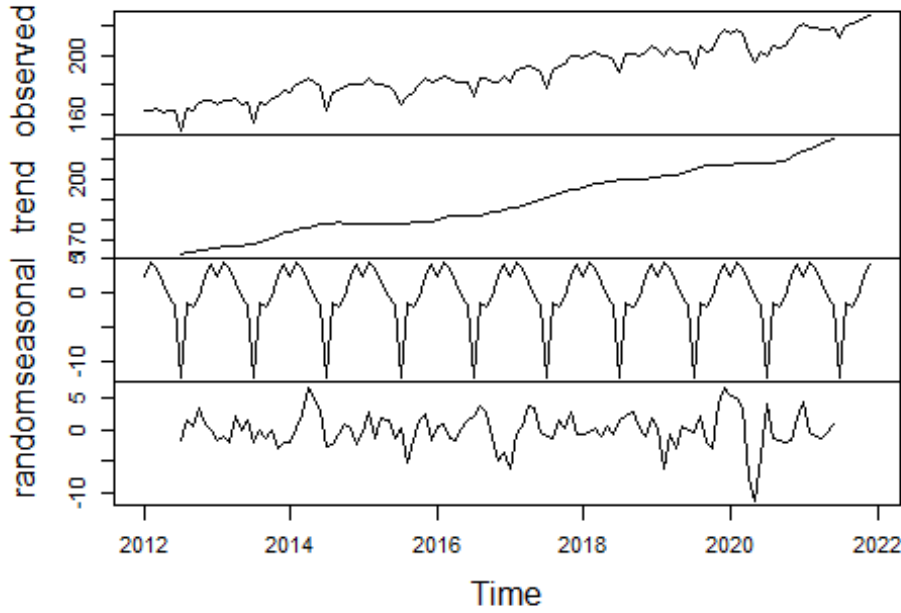
	Actual	Forecast	Absolute_Error	Accuracy
Jan 2020	102	100	2.03	98.0
Feb 2020	103	102	1.46	98.6
Mar 2020	102	101	0.64	99.4
Apr 2020	92	101	9.15	90.1
May 2020	94	101	6.81	92.8
Jun 2020	96	100	3.68	96.2
Jul 2020	93	97	4.01	95.7
Aug 2020	96	101	4.65	95.2
Sep 2020	94	99	5.11	94.6
Oct 2020	95	100	5.49	94.2
Nov 2020	96	103	6.52	93.2
Dec 2020	97	104	6.90	92.9
Jan 2021	98	103	5.40	94.5
Feb 2021	103	104	0.79	99.2
Mar 2021	101	105	3.96	96.1
Apr 2021	100	105	4.50	95.5
May 2021	98	103	5.20	94.7
Jun 2021	99	104	4.74	95.2
Jul 2021	90	101	10.66	88.2
Aug 2021	96	104	7.57	92.1
Sep 2021	94	102	7.98	91.5

Oct 2021	96	104	7.94	91.7
Nov 2021	94	106	12.46	86.7
Dec 2021	93	108	15.41	83.4

CFG Firm Transportation Services 2.1 (FTS-2.1)

Customer Time-Series Decomposition

Decomposition of additive time series



ARIMA Model: Expected Accuracy

In this section we evaluate the expected accuracy of a Seasonal ARIMA Model using cross-validation. ARIMA is an acronym for 'Autoregressive Integrated Moving Average' which is a widely used Time-Series forecasting model that utilizes the recent values to predict outward.

Here we evaluate model accuracy by using cross-validation and rolling forecasts throughout the time-series to determine our expected accuracy over a 24 Month period.

	ME	RMSE	MAE
Forecast Horizon 1	1	3	2
Forecast Horizon 2	1	4	3
Forecast Horizon 3	2	5	4
Forecast Horizon 4	2	5	4
Forecast Horizon 5	1	6	5
Forecast Horizon 6	1	6	5
Forecast Horizon 7	1	6	5
Forecast Horizon 8	1	6	6
Forecast Horizon 9	1	7	6
Forecast Horizon 10	1	7	6
Forecast Horizon 11	1	7	6
Forecast Horizon 12	0	6	5
Forecast Horizon 13	1	6	5
Forecast Horizon 14	1	7	6
Forecast Horizon 15	1	7	6
Forecast Horizon 16	1	8	5
Forecast Horizon 17	1	8	6
Forecast Horizon 18	1	8	6
Forecast Horizon 19	1	8	6
Forecast Horizon 20	1	8	6
Forecast Horizon 21	1	8	6
Forecast Horizon 22	1	8	6
Forecast Horizon 23	1	8	7
Forecast Horizon 24	1	8	6

ARIMA Model: Diagnostics

In this section we evaluate the diagnostics of the ARIMA Model. Below we see that the model fails the Ljung-Box Test and therefore we can determine the data is independently distributed. In addition, we see from the graphs that the lagged values are not auto-correlated with one another, and the residuals are normally distributed.

```
Series: x
ARIMA(1,0,0)(0,1,1)[12] with drift
```

```
Coefficients:
      ar1      sma1  drift
      0.7114 -0.6852  0.5050
s.e.  0.0671  0.0977  0.0353
```

```
sigma^2 estimated as 9.806: log likelihood=-279.13
AIC=566.26  AICc=566.65  BIC=576.99
```

```
Training set error measures:
```

```
ME      RMSE      MAE      MPE      MAPE      MASE
```

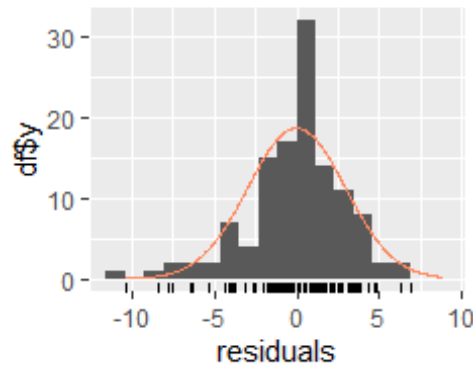
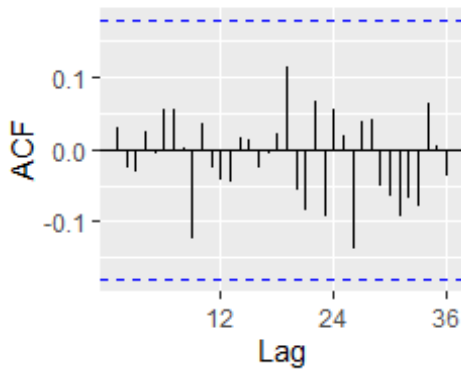
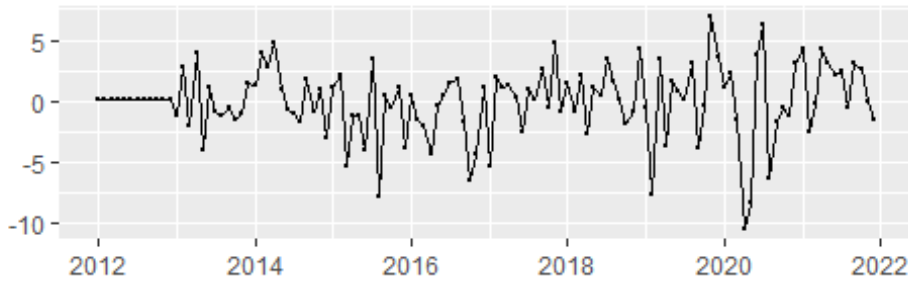
FPUC-Rate 0625470

Training set -0.02500651 2.929146 2.142987 -0.03690567 1.116374 0.3098294

ACF1

Training set 0.03029662

Residuals from ARIMA(1,0,0)(0,1,1)[12] with drift



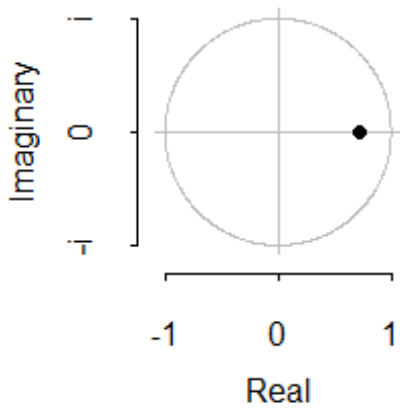
Ljung-Box test

data: Residuals from ARIMA(1,0,0)(0,1,1)[12] with drift

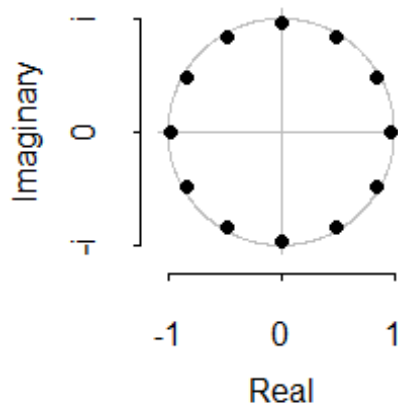
$Q^* = 10.142$, $df = 21$, $p\text{-value} = 0.977$

Model $df: 3$. Total lags used: 24

Inverse AR roots



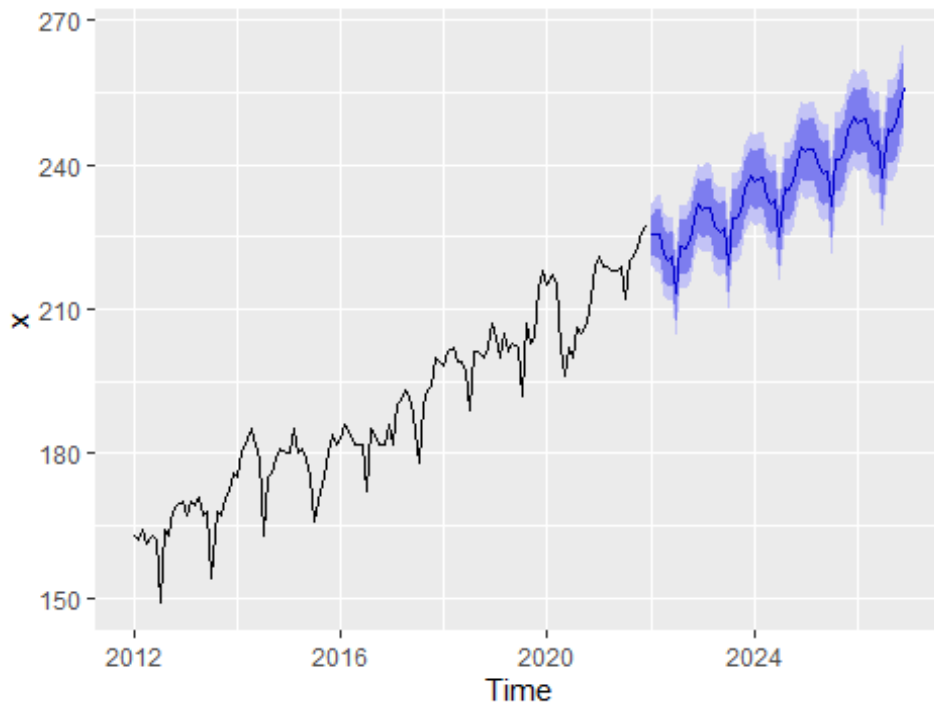
Inverse MA roots



ARIMA Model: 5 Year Forecast

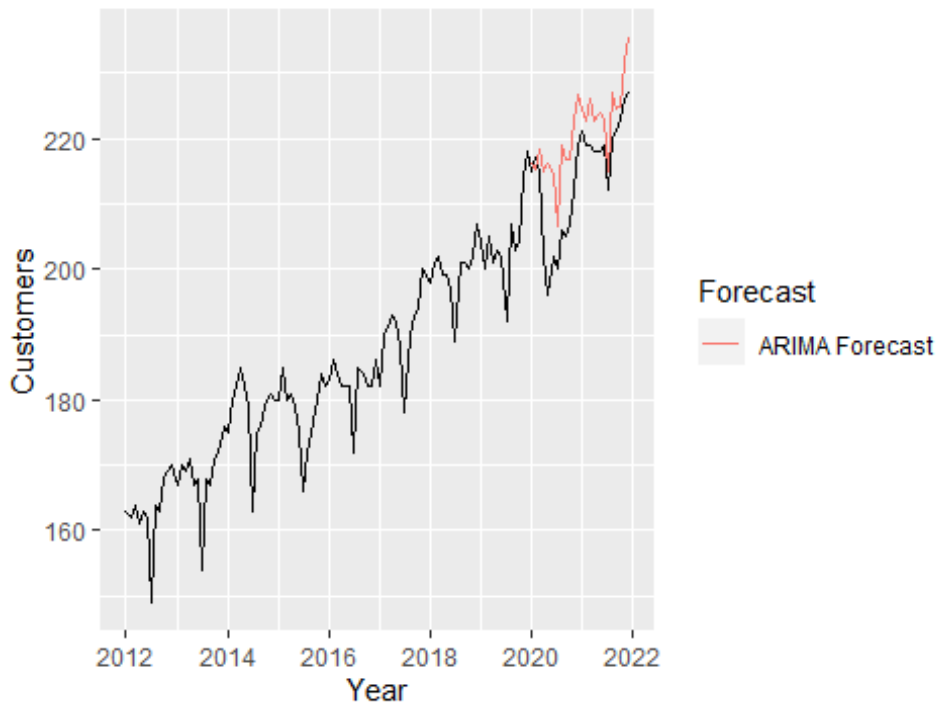
Below we fit & forecast 60 months into the future using an ARIMA (1,0,0)(0,1,1) model. In the graph below we see the 80% and 95% Prediction Intervals bounding our forecast.

Forecasts from ARIMA(1,0,0)(0,1,1)[12] with drift



Back-Testing

Commercial Client Backtesting: 2020-2021



Test Results

Below we see that the model performs roughly as expected for a “normal” year of 2019, and continues to have a high degree of accuracy in 2020 and 2021.

[1] "24Month Mean Absolute Error (MAE): 7.07"

[1] "24Month Mean Accuracy: 96.63"

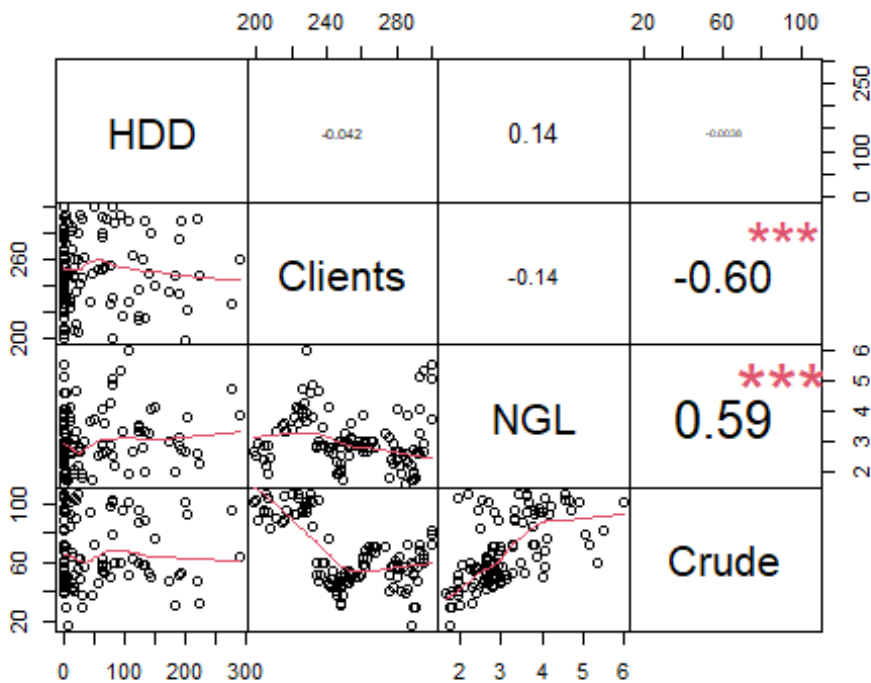
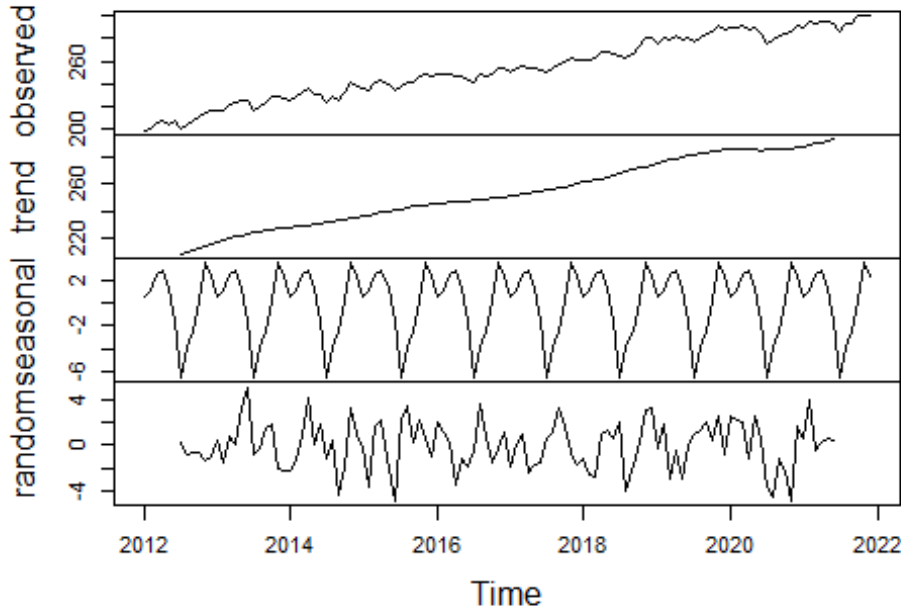
	Actual	Forecast	Absolute_Error	Accuracy
Jan 2020	215	216	1.12	99.5
Feb 2020	217	215	1.64	99.2
Mar 2020	215	218	3.23	98.5
Apr 2020	202	215	13.05	93.5
May 2020	196	216	20.03	89.8
Jun 2020	202	215	12.73	93.7
Jul 2020	200	207	6.58	96.7
Aug 2020	206	219	12.81	93.8
Sep 2020	205	217	11.84	94.2
Oct 2020	207	217	9.93	95.2
Nov 2020	212	223	10.66	95.0
Dec 2020	219	227	7.64	96.5
Jan 2021	221	225	3.51	98.4
Feb 2021	219	223	3.52	98.4
Mar 2021	219	226	6.95	96.8
Apr 2021	218	223	4.77	97.8
May 2021	218	224	6.06	97.2
Jun 2021	219	223	4.02	98.2
Jul 2021	212	215	2.97	98.6
Aug 2021	220	227	7.04	96.8
Sep 2021	221	224	3.46	98.4

Oct 2021	223	225	1.90	99.1
Nov 2021	226	232	5.76	97.5
Dec 2021	227	235	8.34	96.3

CFG Firm Transportation Services 3 (FTS-3)

Customer Time-Series Decomposition

Decomposition of additive time series



ARIMA Model: Expected Accuracy

In this section we evaluate the expected accuracy of a Seasonal ARIMA Model using cross-validation. ARIMA is an acronym for 'Autoregressive Integrated Moving Average' which is a widely used Time-Series forecasting model that utilizes the recent values to predict outward.

Here we evaluate model accuracy by using cross-validation and rolling forecasts throughout the time-series to determine our expected accuracy over a 24 Month period.

	ME	RMSE	MAE
Forecast Horizon 1	1	3	3
Forecast Horizon 2	2	4	2
Forecast Horizon 3	2	4	3
Forecast Horizon 4	2	4	3
Forecast Horizon 5	2	4	3
Forecast Horizon 6	2	5	4
Forecast Horizon 7	2	5	4
Forecast Horizon 8	2	6	5
Forecast Horizon 9	2	6	5
Forecast Horizon 10	2	7	6
Forecast Horizon 11	1	8	6
Forecast Horizon 12	1	8	7
Forecast Horizon 13	2	9	8
Forecast Horizon 14	2	9	8
Forecast Horizon 15	2	9	9
Forecast Horizon 16	2	10	9
Forecast Horizon 17	2	10	9
Forecast Horizon 18	2	10	9
Forecast Horizon 19	2	10	9
Forecast Horizon 20	1	10	9
Forecast Horizon 21	1	10	9
Forecast Horizon 22	1	10	9
Forecast Horizon 23	1	10	9
Forecast Horizon 24	1	10	9

ARIMA Model: Diagnostics

In this section we evaluate the diagnostics of the ARIMA Model. Below we see that the model fails the Ljung-Box Test and therefore we can determine the data is independently distributed. In addition, we see from the graphs that the lagged values are not auto-correlated with one another, and the residuals are normally distributed.

```
Series: x
ARIMA(1,0,1)(2,1,0)[12] with drift

Coefficients:
      ar1      ma1      sar1      sar2      drift
    0.9156 -0.3765 -0.5894 -0.2462  0.8140
s.e.  0.0534  0.1190  0.0944  0.1056  0.0951

sigma^2 estimated as 9.539:  log likelihood=-275.07
AIC=562.15  AICc=562.98  BIC=578.24

Training set error measures:
```

ME	RMSE	MAE	MPE	MAPE	MASE
----	------	-----	-----	------	------

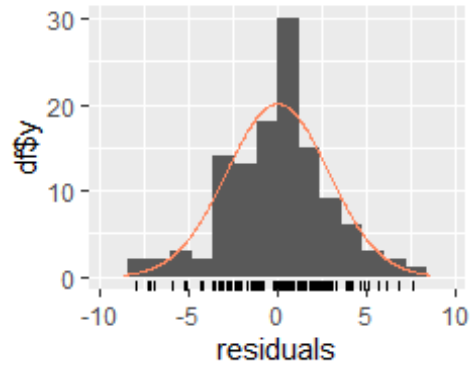
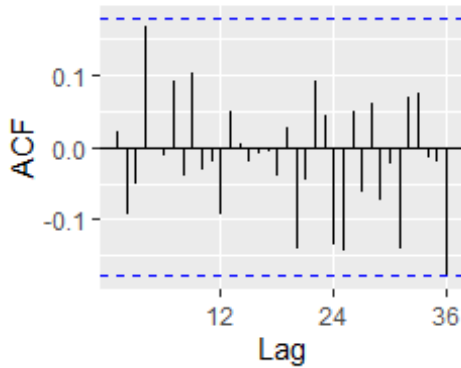
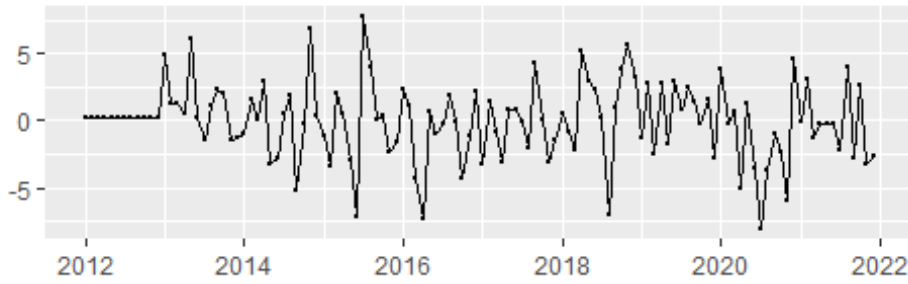
FPUC-Rate 0625475

Training set -0.01527597 2.861378 2.119481 -3.072475e-05 0.8255929 0.2119481

ACF1

Training set 0.02237732

Residuals from ARIMA(1,0,1)(2,1,0)[12] with drift



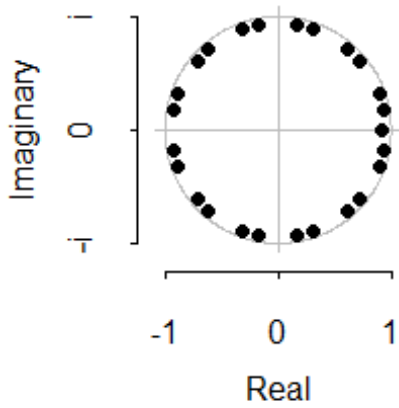
Ljung-Box test

data: Residuals from ARIMA(1,0,1)(2,1,0)[12] with drift

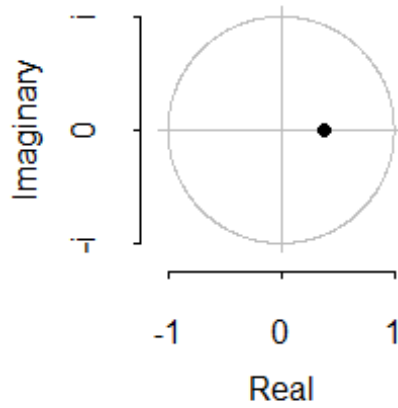
$Q^* = 17.588$, $df = 19$, $p\text{-value} = 0.5501$

Model $df: 5$. Total lags used: 24

Inverse AR roots



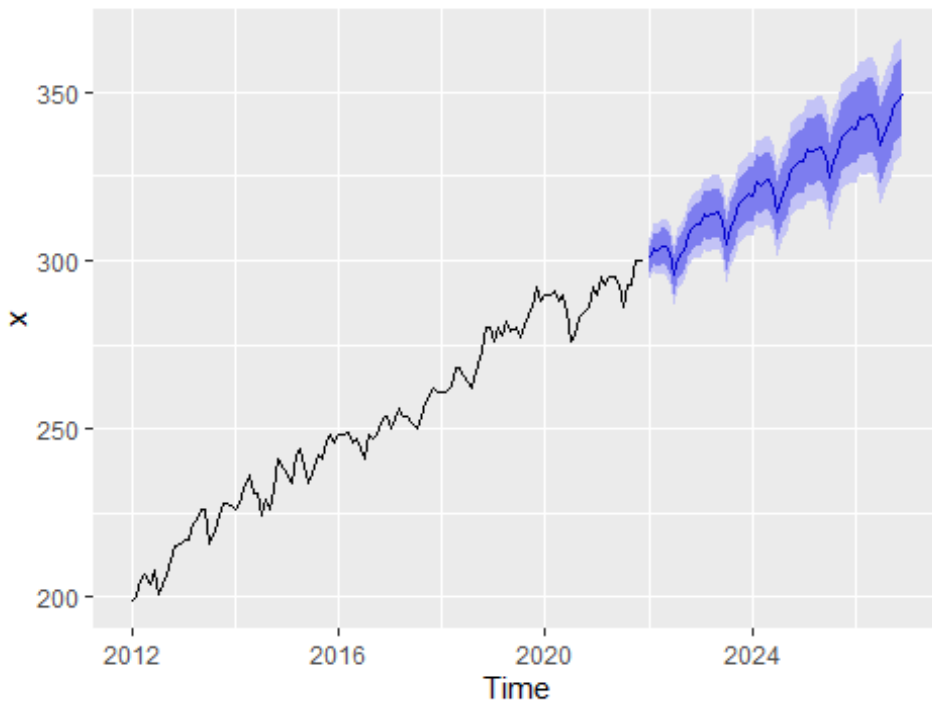
Inverse MA roots



ARIMA Model: 5 Year Forecast

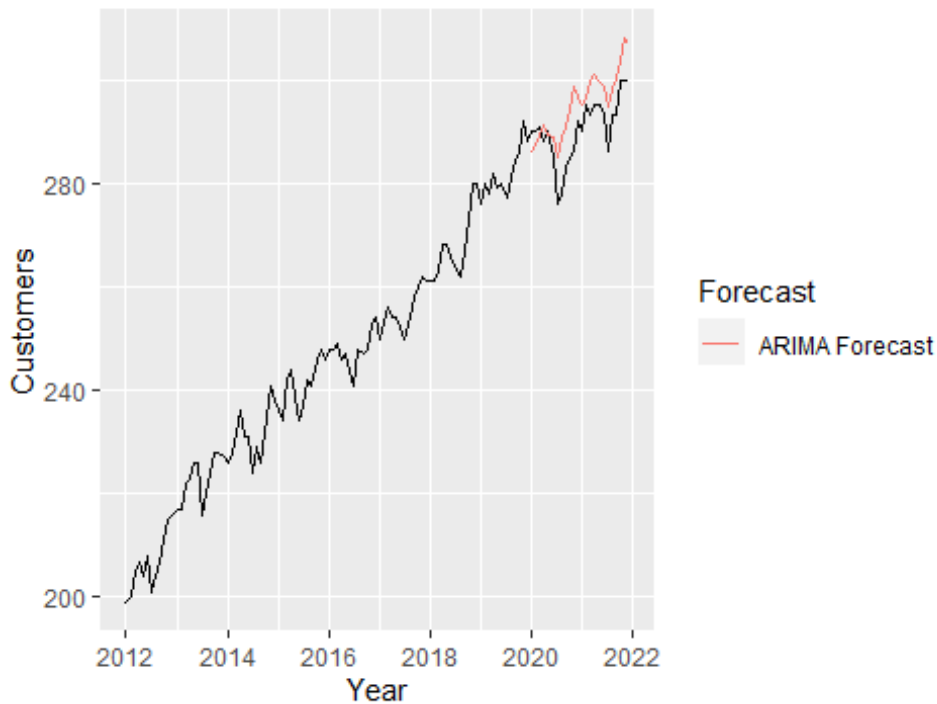
Below we fit & forecast 60 months into the future using an ARIMA (1,0,1)(2,1,0) model. In the graph below we see the 80% and 95% Prediction Intervals bounding our forecast.

Forecasts from ARIMA(1,0,1)(2,1,0)[12] with drift



Back-Testing

Commercial Client Backtesting: 2020-2021



Test Results

Below we see that the model performs roughly as expected for a “normal” year of 2019, and continues to have a high degree of accuracy in 2020 and 2021.

[1] "24Month Mean Absolute Error (MAE): 5.76"

[1] "24Month Mean Accuracy: 98.01"

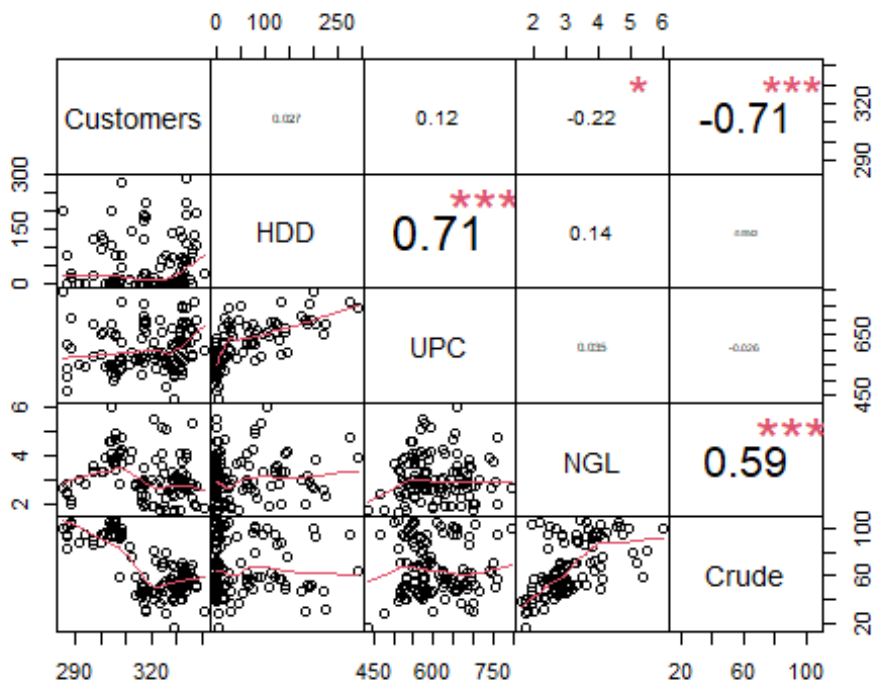
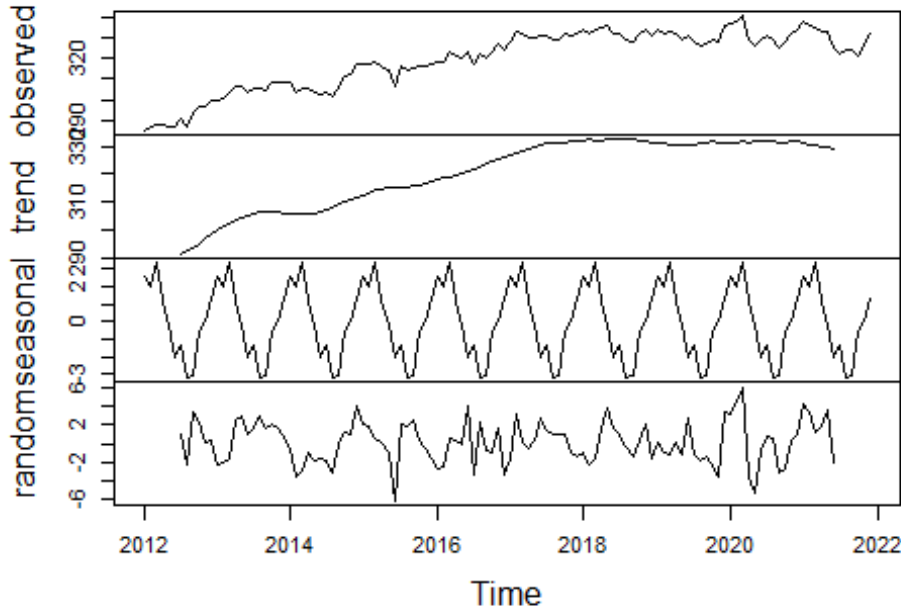
	Actual	Forecast	Absolute_Error	Accuracy
Jan 2020	290	286	4.17	98.6
Feb 2020	290	287	2.80	99.0
Mar 2020	291	289	1.63	99.4
Apr 2020	288	291	3.26	98.9
May 2020	290	289	0.68	99.8
Jun 2020	285	289	3.83	98.7
Jul 2020	276	285	8.98	96.7
Aug 2020	278	289	10.83	96.1
Sep 2020	283	291	7.69	97.3
Oct 2020	285	294	8.99	96.8
Nov 2020	286	299	12.51	95.6
Dec 2020	292	297	4.73	98.4
Jan 2021	290	295	5.21	98.2
Feb 2021	295	296	1.24	99.6
Mar 2021	293	299	6.32	97.8
Apr 2021	295	301	5.96	98.0
May 2021	295	299	4.33	98.5
Jun 2021	293	299	5.58	98.1
Jul 2021	286	295	8.64	97.0
Aug 2021	293	298	5.37	98.2
Sep 2021	293	300	7.10	97.6

Oct 2021	300	304	3.70	98.8
Nov 2021	300	308	8.01	97.3
Dec 2021	300	307	6.68	97.8

CFG Firm Transportation Services 3.1 (FTS-3.1)

Customer Time-Series Decomposition

Decomposition of additive time series



ARIMA Model: Expected Accuracy

In this section we evaluate the expected accuracy of a Seasonal ARIMA Model using cross-validation. ARIMA is an acronym for 'Autoregressive Integrated Moving Average' which is a widely used Time-Series forecasting model that utilizes the recent values to predict outward.

Here we evaluate model accuracy by using cross-validation and rolling forecasts throughout the time-series to determine our expected accuracy over a 24 Month period.

		ME	RMSE	MAE
Forecast Horizon	1	0	3	2
Forecast Horizon	2	0	4	3
Forecast Horizon	3	0	4	4
Forecast Horizon	4	-1	5	4
Forecast Horizon	5	-1	6	5
Forecast Horizon	6	-2	6	5
Forecast Horizon	7	-2	6	5
Forecast Horizon	8	-3	5	4
Forecast Horizon	9	-3	5	4
Forecast Horizon	10	-4	6	5
Forecast Horizon	11	-4	6	5
Forecast Horizon	12	-5	6	5
Forecast Horizon	13	-5	7	6
Forecast Horizon	14	-5	8	7
Forecast Horizon	15	-6	9	8
Forecast Horizon	16	-6	10	9
Forecast Horizon	17	-6	11	10
Forecast Horizon	18	-7	11	10
Forecast Horizon	19	-8	11	10
Forecast Horizon	20	-9	11	9
Forecast Horizon	21	-9	11	9
Forecast Horizon	22	-10	11	10
Forecast Horizon	23	-10	12	10
Forecast Horizon	24	-11	13	11

ARIMA Model: Diagnostics

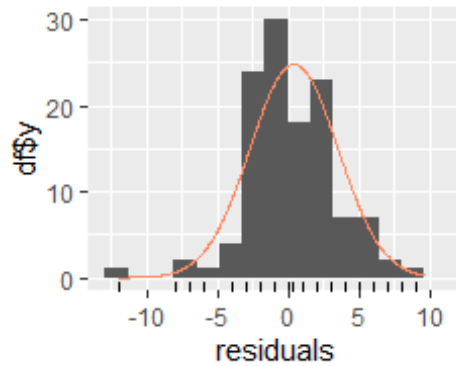
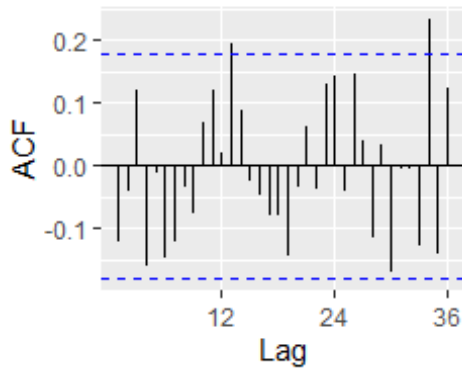
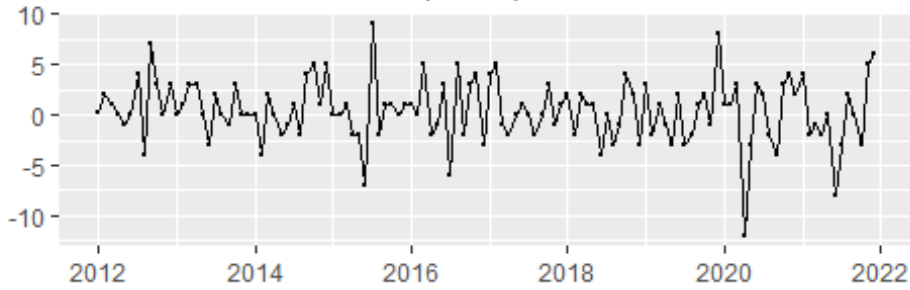
In this section we evaluate the diagnostics of the ARIMA Model. Below we see that the model fails the Ljung-Box Test and therefore we can determine the data is independently distributed. In addition, we see from the graphs that the lagged values are not auto-correlated with one another, and the residuals are normally distributed.

```
Series: x
ARIMA(0,1,0)

sigma^2 estimated as 9.824:  log likelihood=-304.8
AIC=611.6  AICc=611.63  BIC=614.38

Training set error measures:
              ME          RMSE          MAE          MPE          MAPE          MASE
Training set 0.3940417  3.121273  2.327375  0.1232868  0.7268457  0.3825822
              ACF1
Training set -0.1205972
```

Residuals from ARIMA(0,1,0)



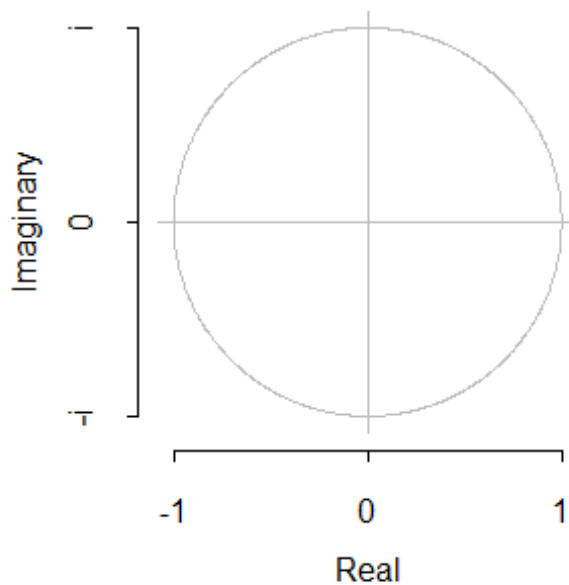
Ljung-Box test

data: Residuals from ARIMA(0,1,0)
 $Q^* = 33.497$, $df = 24$, $p\text{-value} = 0.09401$

Model df: 0. Total lags used: 24

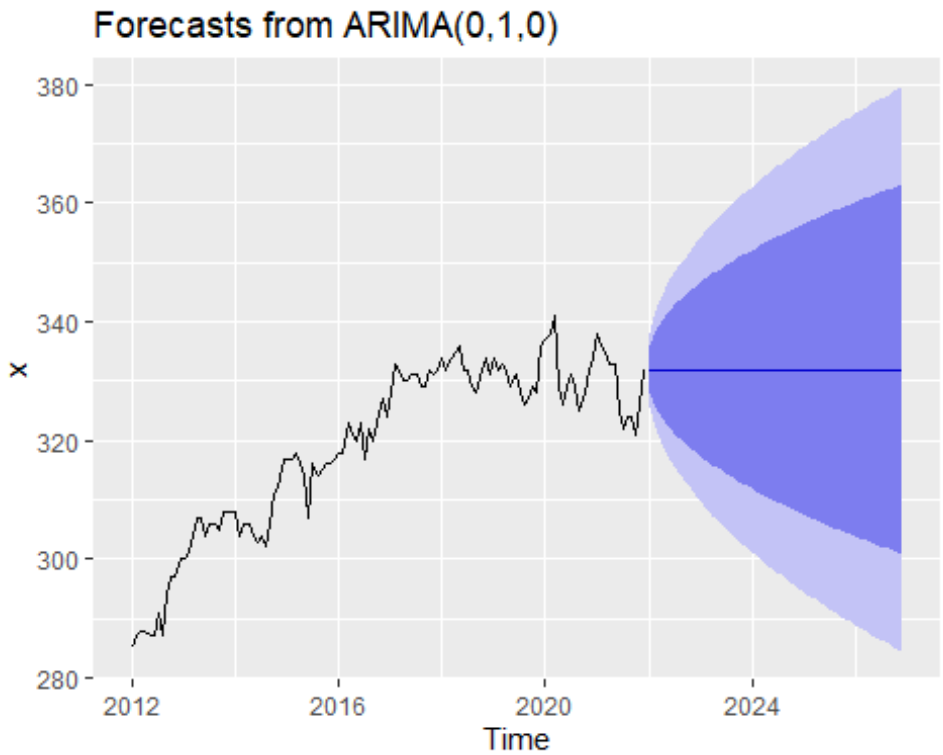
Warning in plot.Arima(arima_fit): No roots to plot

No AR or MA roots

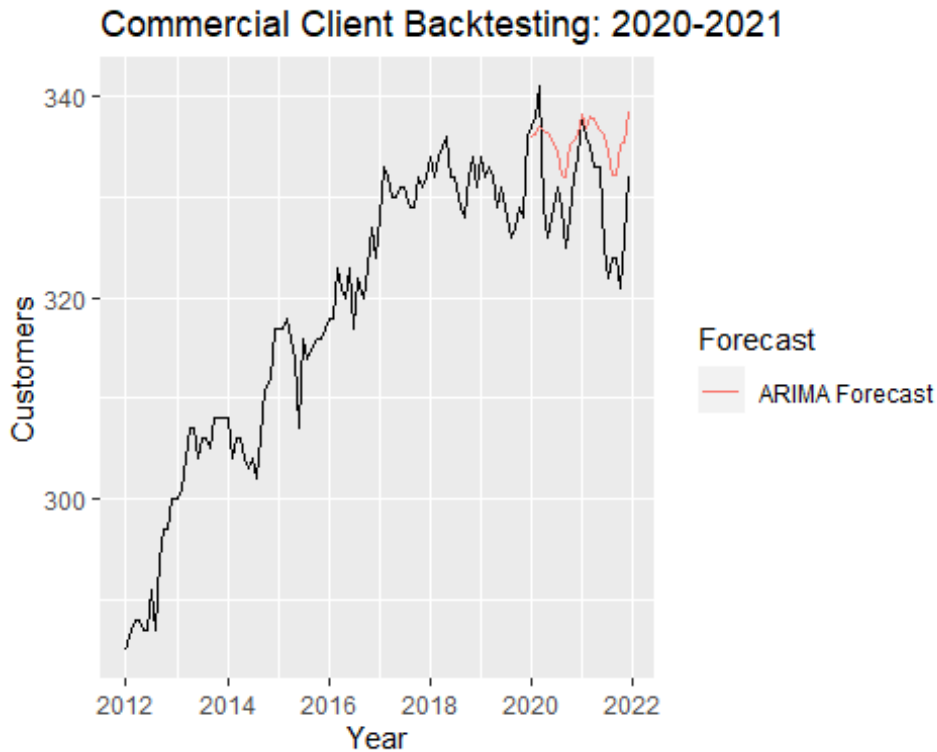


ARIMA Model: 5 Year Forecast

Below we fit & forecast 60 months into the future using an ARIMA (0,1,0) model. In the graph below we see the 80% and 95% Prediction Intervals bounding our forecast.



Back-Testing



Test Results

Below we see that the model performs roughly as expected for a “normal” year of 2019, and continues to have a high degree of accuracy in 2020 and 2021.

```
[1] "24Month Mean Absolute Error (MAE): 5.86"
```

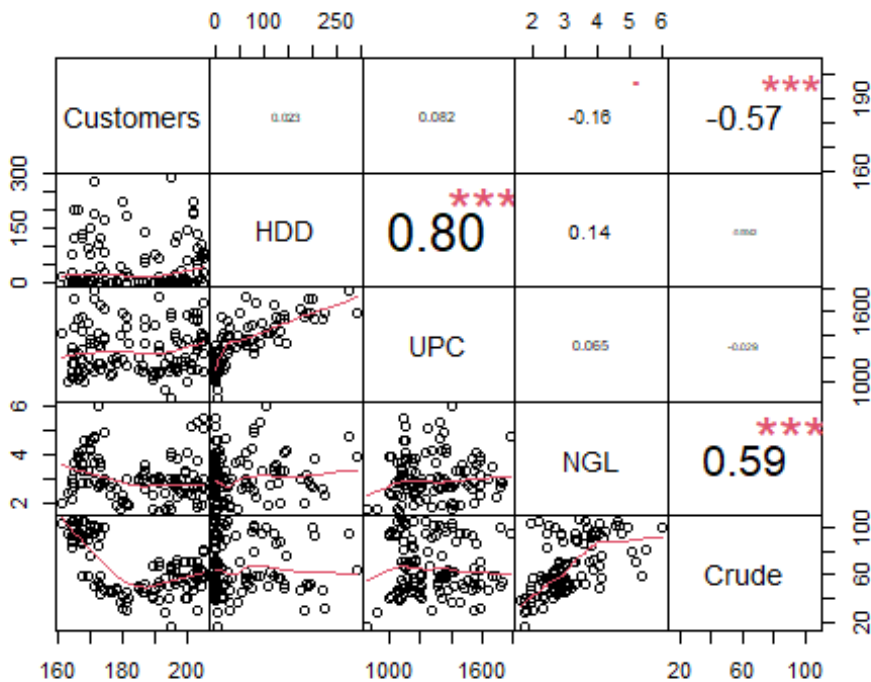
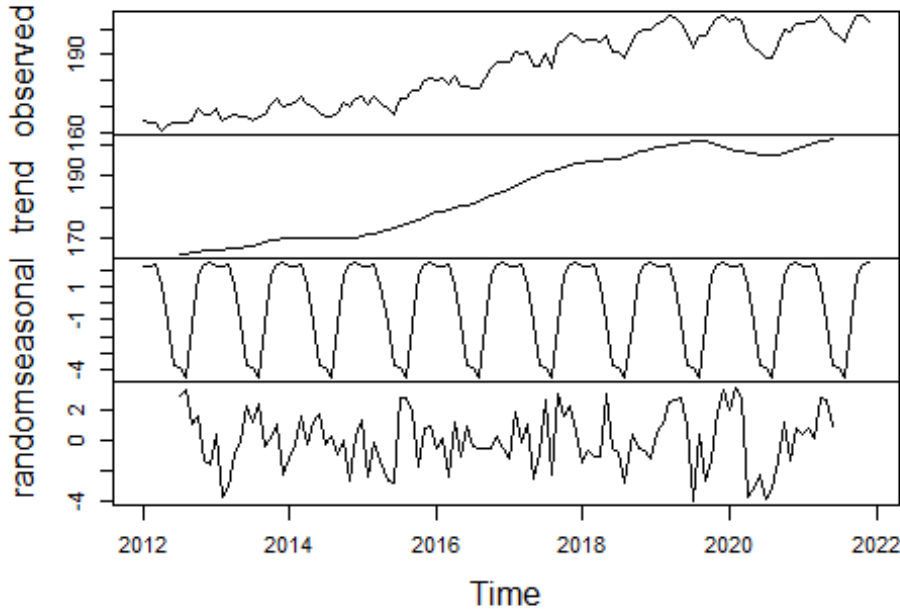
```
[1] "24Month Mean Accuracy: 98.22"
```

	Actual	Forecast	Absolute_Error	Accuracy
Jan 2020	337	336	1.03	99.7
Feb 2020	338	336	1.84	99.5
Mar 2020	341	337	4.00	98.8
Apr 2020	329	337	7.62	97.7
May 2020	326	336	10.42	96.8
Jun 2020	329	335	6.31	98.1
Jul 2020	331	335	3.65	98.9
Aug 2020	329	332	3.18	99.0
Sep 2020	325	332	6.94	97.9
Oct 2020	328	335	7.18	97.8
Nov 2020	332	336	3.58	98.9
Dec 2020	334	336	2.27	99.3
Jan 2021	338	338	0.28	99.9
Feb 2021	336	337	0.77	99.8
Mar 2021	335	338	3.05	99.1
Apr 2021	333	338	4.81	98.6
May 2021	333	337	3.68	98.9
Jun 2021	325	336	11.12	96.6
Jul 2021	322	335	12.57	96.1
Aug 2021	324	332	8.16	97.5
Sep 2021	324	332	8.25	97.5
Oct 2021	321	335	14.16	95.6
Nov 2021	326	335	9.40	97.1
Dec 2021	332	338	6.34	98.1

CFG Firm Transportation Services 4 (FTS-4)

Customer Time-Series Decomposition

Decomposition of additive time series



ARIMA Model: Expected Accuracy

In this section we evaluate the expected accuracy of a Seasonal ARIMA Model using cross-validation. ARIMA is an acronym for 'Autoregressive Integrated Moving Average' which is a widely used Time-Series forecasting model that utilizes the recent values to predict outward.

Here we evaluate model accuracy by using cross-validation and rolling forecasts throughout the time-series to determine our expected accuracy over a 24 Month period.

		ME	RMSE	MAE
Forecast Horizon	1	0	3	2
Forecast Horizon	2	-1	3	2
Forecast Horizon	3	-1	3	3
Forecast Horizon	4	-1	4	3
Forecast Horizon	5	-2	5	4
Forecast Horizon	6	-2	5	4
Forecast Horizon	7	-3	5	4
Forecast Horizon	8	-3	6	5
Forecast Horizon	9	-3	6	5
Forecast Horizon	10	-4	7	5
Forecast Horizon	11	-4	7	5
Forecast Horizon	12	-5	7	6
Forecast Horizon	13	-5	8	6
Forecast Horizon	14	-6	8	6
Forecast Horizon	15	-6	8	7
Forecast Horizon	16	-6	9	7
Forecast Horizon	17	-7	9	7
Forecast Horizon	18	-7	9	7
Forecast Horizon	19	-7	9	7
Forecast Horizon	20	-8	9	8
Forecast Horizon	21	-8	10	9
Forecast Horizon	22	-8	10	9
Forecast Horizon	23	-9	11	10
Forecast Horizon	24	-9	11	10

ARIMA Model: Diagnostics

In this section we evaluate the diagnostics of the ARIMA Model. Below we see that the model fails the Ljung-Box Test and therefore we can determine the data is independently distributed. In addition, we see from the graphs that the lagged values are not auto-correlated with one another, and the residuals are normally distributed.

```
Series: x
ARIMA(1,0,1)(0,1,1)[12] with drift
```

Coefficients:

```
      ar1      ma1      sma1      drift
      0.9423  -0.3365  -0.7736  0.3495
s.e.  0.0388   0.0996   0.1133  0.0650
```

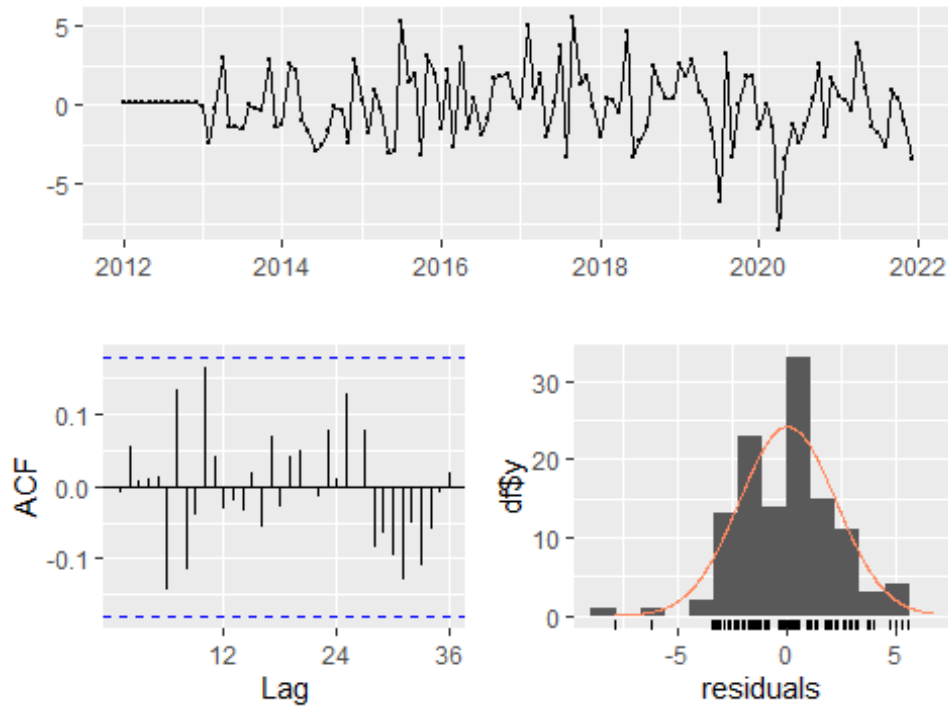
```
sigma^2 estimated as 5.605:  log likelihood=-250
AIC=509.99  AICc=510.58  BIC=523.4
```

Training set error measures:

```
              ME      RMSE      MAE      MPE      MAPE      MASE
Training set 0.01367694 2.204091 1.668164 -0.003418302 0.898286 0.3205725
              ACF1
Training set -0.008318769
```

FPUC-Rate 0625485

Residuals from ARIMA(1,0,1)(0,1,1)[12] with drift

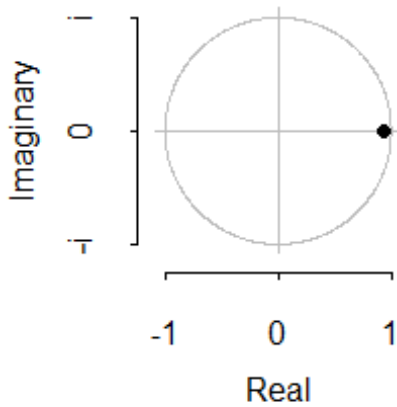


Ljung-Box test

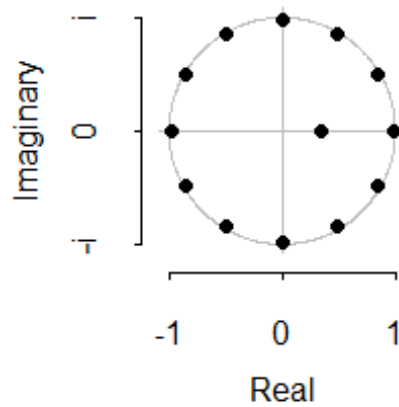
data: Residuals from ARIMA(1,0,1)(0,1,1)[12] with drift
 $Q^* = 14.616$, $df = 20$, $p\text{-value} = 0.7979$

Model df: 4. Total lags used: 24

Inverse AR roots

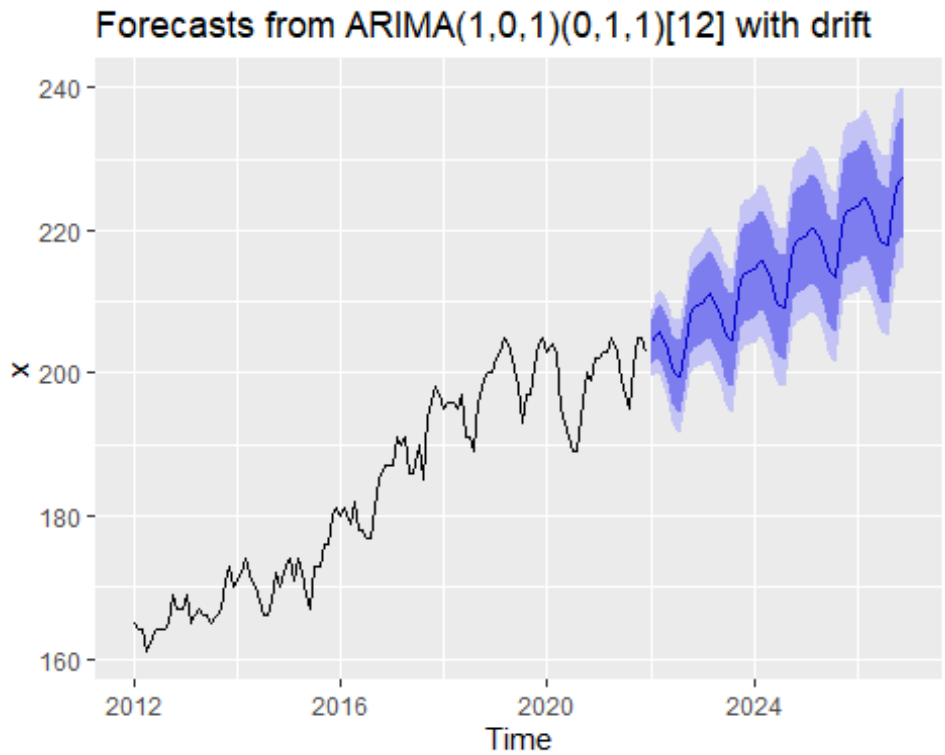


Inverse MA roots

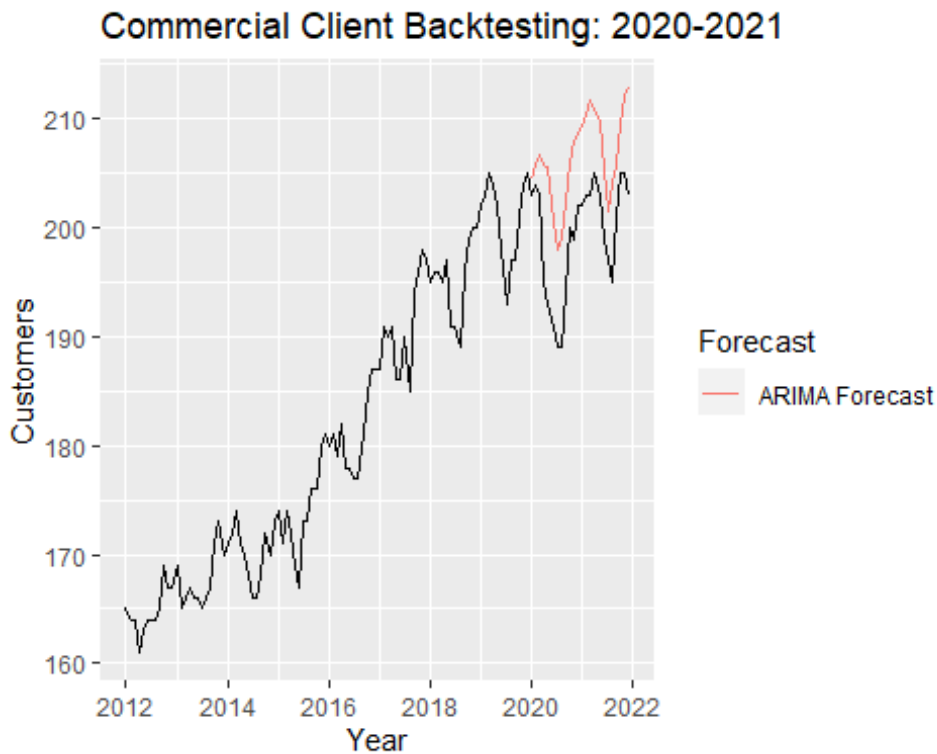


ARIMA Model: 5 Year Forecast

Below we fit & forecast 60 months into the future using an ARIMA (1,0,1)(0,1,1) model. In the graph below we see the 80% and 95% Prediction Intervals bounding our forecast.



Back-Testing



Test Results

Below we see that the model performs roughly as expected for a “normal” year of 2019, and continues to have a high degree of accuracy in 2020 and 2021.

```
[1] "24Month Mean Absolute Error (MAE): 7.15"
```

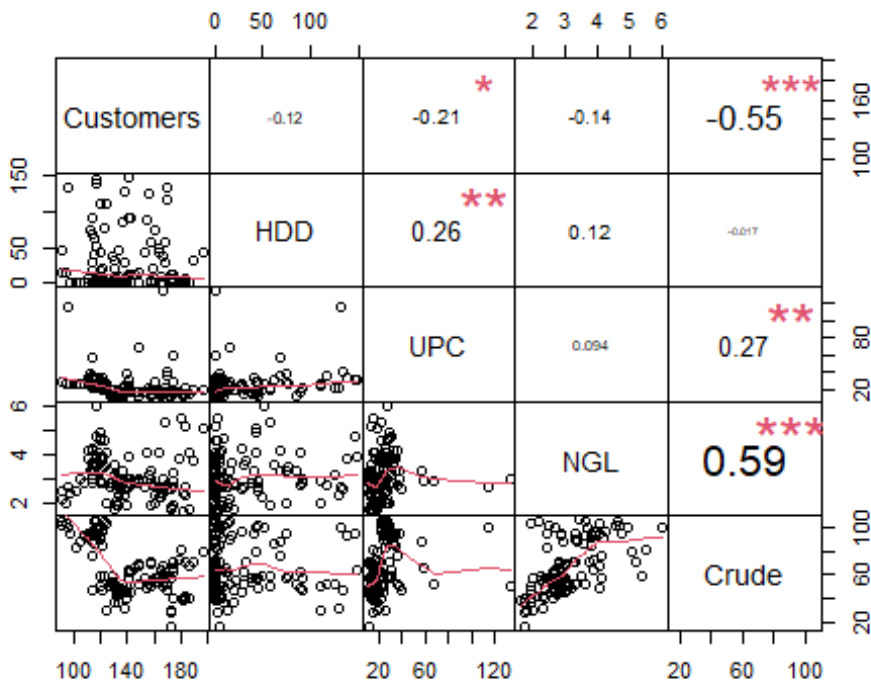
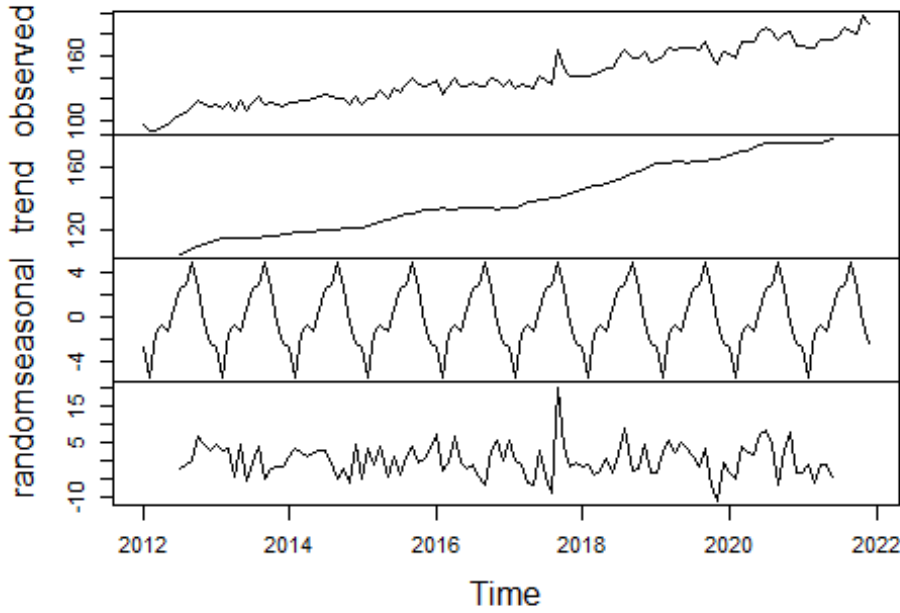
```
[1] "24Month Mean Accuracy: 96.38"
```

	Actual	Forecast	Absolute_Error	Accuracy
Jan 2020	203	204	1.43	99.3
Feb 2020	204	206	1.74	99.1
Mar 2020	203	207	3.65	98.2
Apr 2020	195	206	10.72	94.5
May 2020	193	206	12.58	93.5
Jun 2020	191	201	9.65	94.9
Jul 2020	189	198	9.00	95.2
Aug 2020	189	199	10.17	94.6
Sep 2020	194	202	8.48	95.6
Oct 2020	200	206	6.01	97.0
Nov 2020	199	208	9.06	95.4
Dec 2020	202	209	6.59	96.7
Jan 2021	202	209	7.23	96.4
Feb 2021	203	210	7.40	96.4
Mar 2021	203	212	8.82	95.7
Apr 2021	205	211	5.86	97.1
May 2021	203	210	6.84	96.6
Jun 2021	199	205	6.35	96.8
Jul 2021	197	202	4.59	97.7
Aug 2021	195	204	9.10	95.3
Sep 2021	201	206	4.84	97.6
Oct 2021	205	210	4.59	97.8
Nov 2021	205	212	7.09	96.5
Dec 2021	203	213	9.84	95.2

Commercial Standby Generator Service (CS-GS)

Customer Time-Series Decomposition

Decomposition of additive time series



ARIMA Model: Expected Accuracy

In this section we evaluate the expected accuracy of a Seasonal ARIMA Model using cross-validation. ARIMA is an acronym for 'Autoregressive Integrated Moving Average' which is a widely used Time-Series forecasting model that utilizes the recent values to predict outward.

Here we evaluate model accuracy by using cross-validation and rolling forecasts throughout the time-series to determine our expected accuracy over a 24 Month period.

	ME	RMSE	MAE
Forecast Horizon 1	1	8	5
Forecast Horizon 2	0	9	7
Forecast Horizon 3	1	9	7
Forecast Horizon 4	2	10	8
Forecast Horizon 5	2	11	8
Forecast Horizon 6	3	11	8
Forecast Horizon 7	4	11	9
Forecast Horizon 8	5	11	9
Forecast Horizon 9	5	11	8
Forecast Horizon 10	5	10	8
Forecast Horizon 11	5	11	9
Forecast Horizon 12	6	12	9
Forecast Horizon 13	6	12	9
Forecast Horizon 14	6	13	11
Forecast Horizon 15	6	14	11
Forecast Horizon 16	7	14	11
Forecast Horizon 17	7	14	11
Forecast Horizon 18	7	14	12
Forecast Horizon 19	8	14	12
Forecast Horizon 20	8	14	12
Forecast Horizon 21	8	14	12
Forecast Horizon 22	8	14	12
Forecast Horizon 23	8	15	13
Forecast Horizon 24	9	16	14

ARIMA Model: Diagnostics

In this section we evaluate the diagnostics of the ARIMA Model. Below we see that the model fails the Ljung-Box Test and therefore we can determine the data is independently distributed. In addition, we see from the graphs that the lagged values are not auto-correlated with one another, and the residuals are normally distributed.

```
Series: x
ARIMA(0,1,1) with drift
```

```
Coefficients:
      ma1  drift
-0.4687  0.8146
s.e.    0.0859  0.2893
```

```
sigma^2 estimated as 35.37:  log likelihood=-380.14
AIC=766.27  AICc=766.48  BIC=774.61
```

```
Training set error measures:
```

```
ME      RMSE      MAE      MPE      MAPE      MASE
```

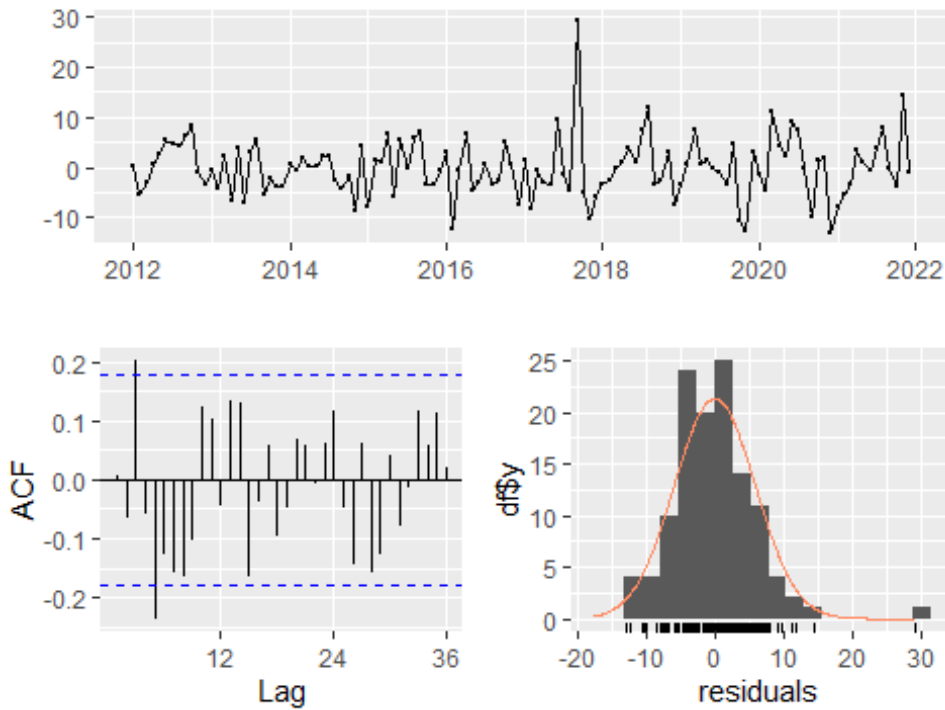
FPUC-Rate 0625490

Training set -0.0239026 5.872354 4.328385 -0.1464874 3.084861 0.4512216

ACF1

Training set 0.006491761

Residuals from ARIMA(0,1,1) with drift



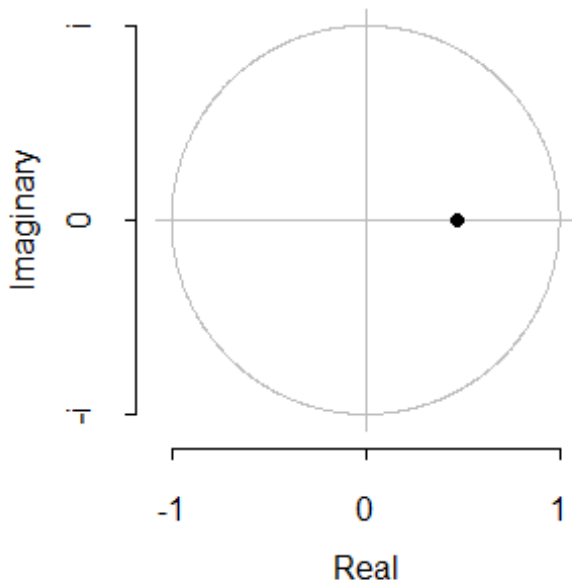
Ljung-Box test

data: Residuals from ARIMA(0,1,1) with drift

$Q^* = 41.998$, $df = 22$, $p\text{-value} = 0.006254$

Model $df: 2$. Total lags used: 24

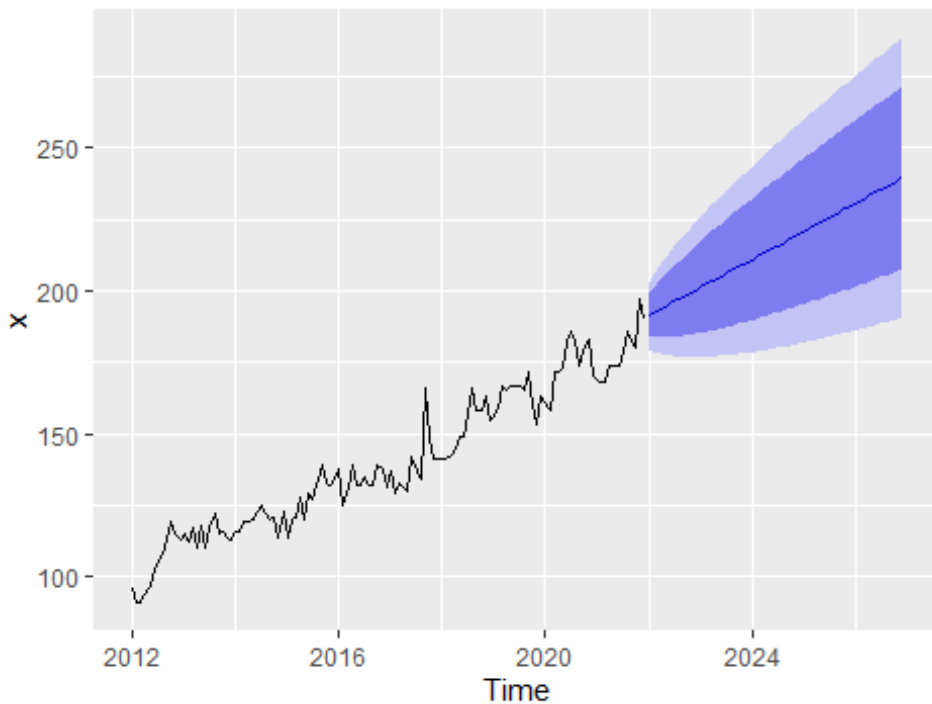
Inverse MA roots



ARIMA Model: 5 Year Forecast

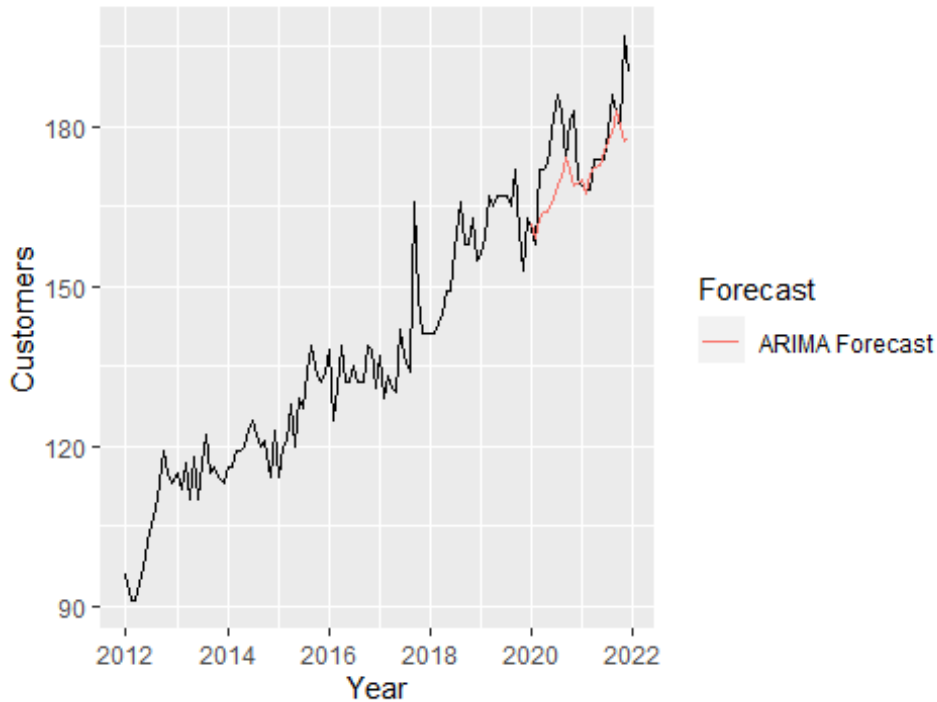
Below we fit & forecast 60 months into the future using an ARIMA (0,1,1) model. In the graph below we see the 80% and 95% Prediction Intervals bounding our forecast.

Forecasts from ARIMA(0,1,1) with drift



Back-Testing

Commercial Client Backtesting: 2020-2021



Test Results

Below we see that the model performs roughly as expected for a “normal” year of 2019, and continues to have a high degree of accuracy in 2020 and 2021.

[1] "24Month Mean Absolute Error (MAE): 6.18"

[1] "24Month Mean Accuracy: 96.6"

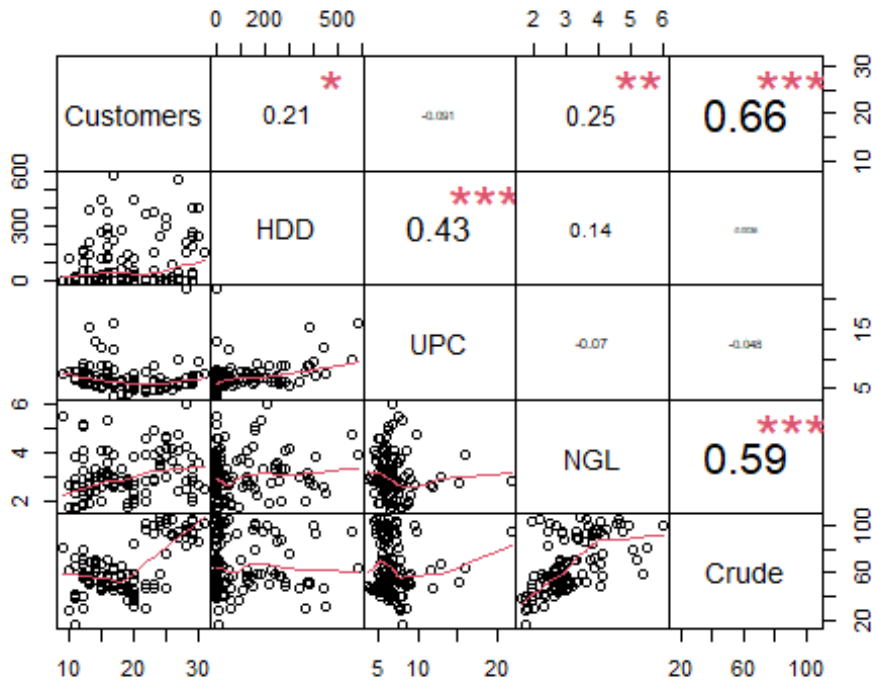
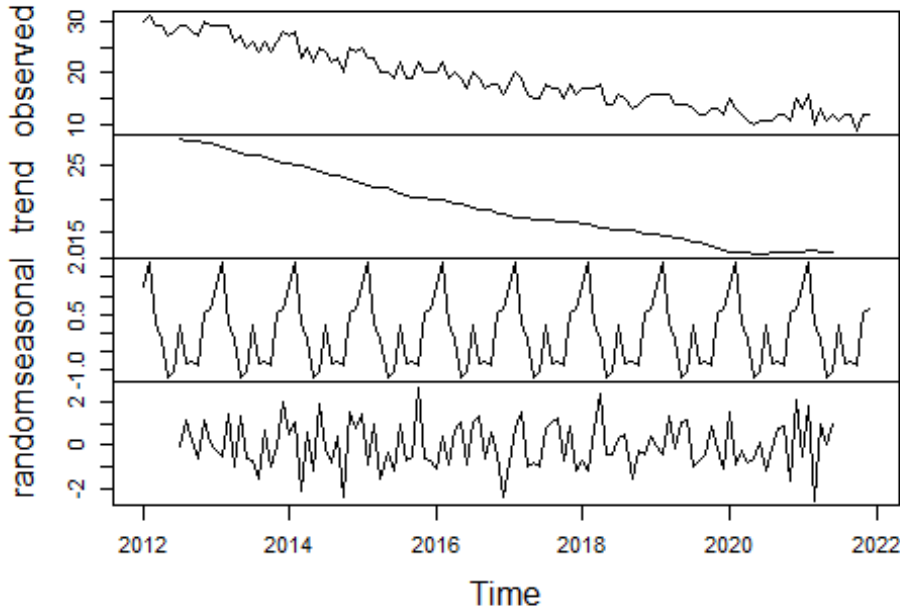
	Actual	Forecast	Absolute_Error	Accuracy
Jan 2020	161	162	0.65	99.6
Feb 2020	158	159	1.15	99.3
Mar 2020	172	163	9.23	94.6
Apr 2020	172	164	8.10	95.3
May 2020	173	164	8.85	94.9
Jun 2020	182	167	15.23	91.6
Jul 2020	186	169	17.23	90.7
Aug 2020	183	170	12.60	93.1
Sep 2020	174	174	0.40	99.8
Oct 2020	181	172	9.23	94.9
Nov 2020	183	169	14.23	92.2
Dec 2020	170	169	0.85	99.5
Jan 2021	169	170	1.07	99.4
Feb 2021	168	168	0.43	99.7
Mar 2021	168	171	3.19	98.1
Apr 2021	174	172	1.68	99.0
May 2021	174	173	1.43	99.2
Jun 2021	174	175	1.19	99.3
Jul 2021	179	177	1.81	99.0
Aug 2021	186	179	7.18	96.1
Sep 2021	183	183	0.18	99.9

Oct 2021	180	180	0.19	99.9
Nov 2021	197	177	19.81	89.9
Dec 2021	190	178	12.43	93.5

Firm Transportation Service (FTS-A & FTS-B)

Customer Time-Series Decomposition

Decomposition of additive time series



ARIMA Model: Expected Accuracy

In this section we evaluate the expected accuracy of a Seasonal ARIMA Model using cross-validation. ARIMA is an acronym for 'Autoregressive Integrated Moving Average' which is a widely used Time-Series forecasting model that utilizes the recent values to predict outward.

Here we evaluate model accuracy by using cross-validation and rolling forecasts throughout the time-series to determine our expected accuracy over a 24 Month period.

	ME	RMSE	MAE
Forecast Horizon 1	0	1	1
Forecast Horizon 2	0	1	1
Forecast Horizon 3	0	1	1
Forecast Horizon 4	0	1	1
Forecast Horizon 5	0	1	1
Forecast Horizon 6	0	1	1
Forecast Horizon 7	0	1	1
Forecast Horizon 8	0	2	1
Forecast Horizon 9	0	1	1
Forecast Horizon 10	0	2	1
Forecast Horizon 11	-1	2	1
Forecast Horizon 12	0	2	1
Forecast Horizon 13	0	2	1
Forecast Horizon 14	0	2	2
Forecast Horizon 15	-1	2	2
Forecast Horizon 16	-1	2	2
Forecast Horizon 17	-1	2	2
Forecast Horizon 18	-1	2	2
Forecast Horizon 19	-1	2	2
Forecast Horizon 20	-1	2	2
Forecast Horizon 21	-1	2	2
Forecast Horizon 22	-1	2	2
Forecast Horizon 23	-1	2	2
Forecast Horizon 24	-1	2	2

ARIMA Model: Diagnostics

In this section we evaluate the diagnostics of the ARIMA Model. Below we see that the model fails the Ljung-Box Test and therefore we can determine the data is independently distributed. In addition, we see from the graphs that the lagged values are not auto-correlated with one another, and the residuals are normally distributed.

```
Series: x
ARIMA(0,1,1)(0,0,2)[12] with drift
```

```
Coefficients:
      ma1      sma1      sma2      drift
-0.8361  0.2333  0.2618 -0.1511
s.e.    0.0572  0.0956  0.0907  0.0325
```

```
sigma^2 estimated as 2.184: log likelihood=-214.92
AIC=439.83  AICc=440.37  BIC=453.73
```

```
Training set error measures:
```

```
ME      RMSE      MAE      MPE      MAPE      MASE
```

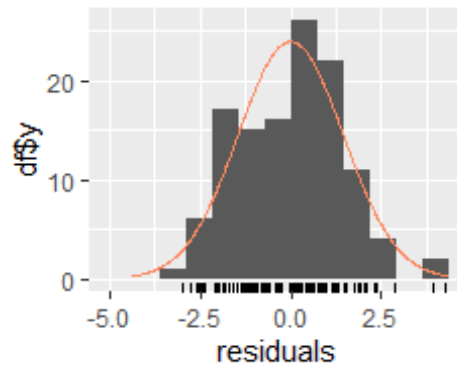
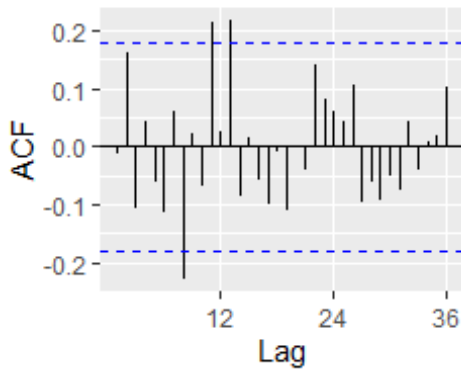
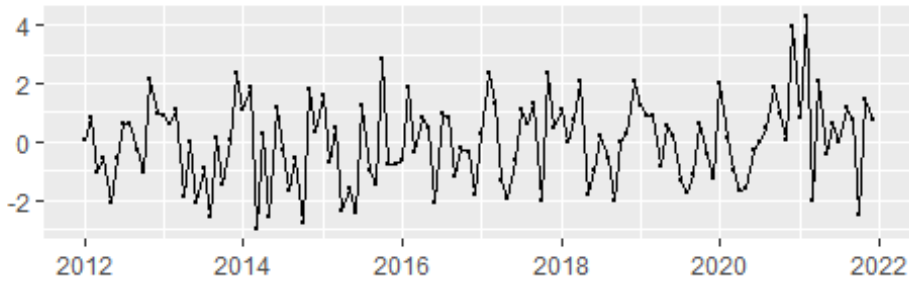
FPUC-Rate 0625495

Training set -0.01183897 1.446572 1.176106 -0.3366003 6.840653 0.5405083

ACF1

Training set -0.01405601

Residuals from ARIMA(0,1,1)(0,0,2)[12] with drift



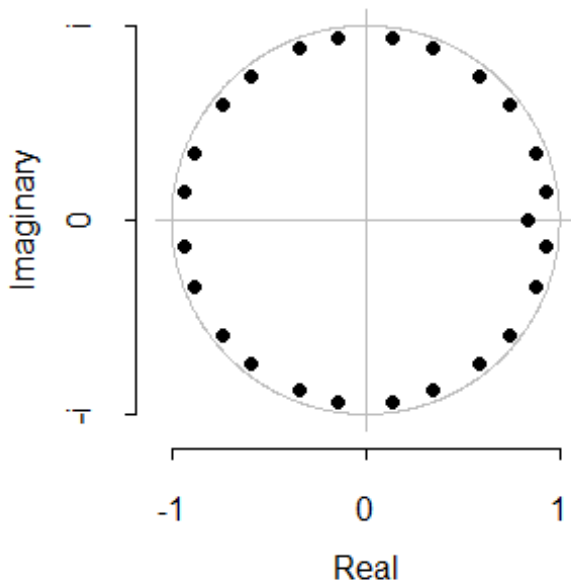
Ljung-Box test

data: Residuals from ARIMA(0,1,1)(0,0,2)[12] with drift

$Q^* = 37.008$, $df = 20$, $p\text{-value} = 0.01168$

Model $df: 4$. Total lags used: 24

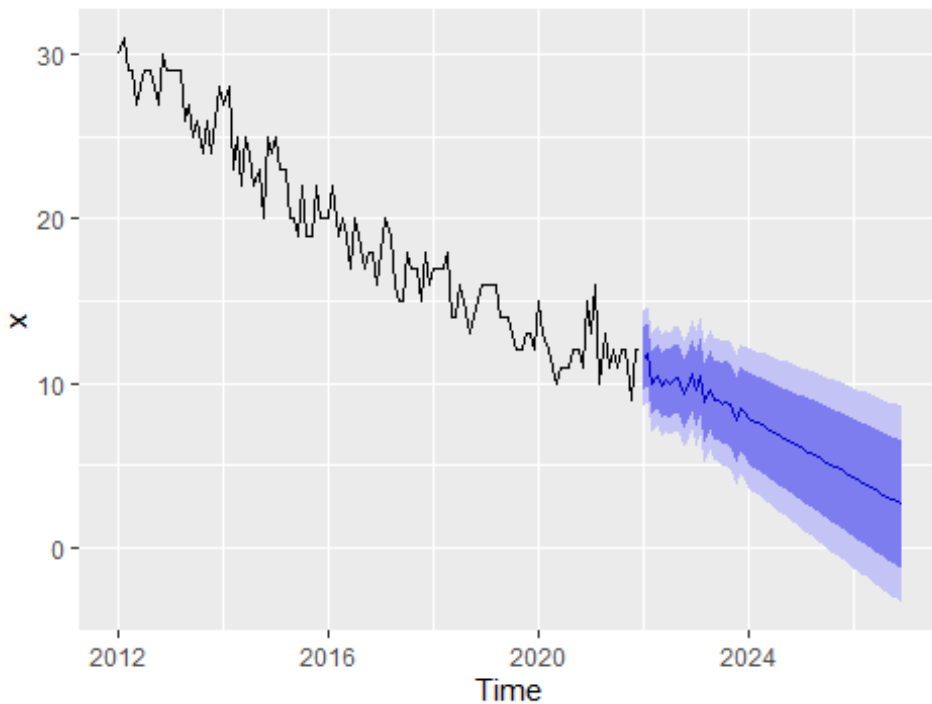
Inverse MA roots



ARIMA Model: 5 Year Forecast

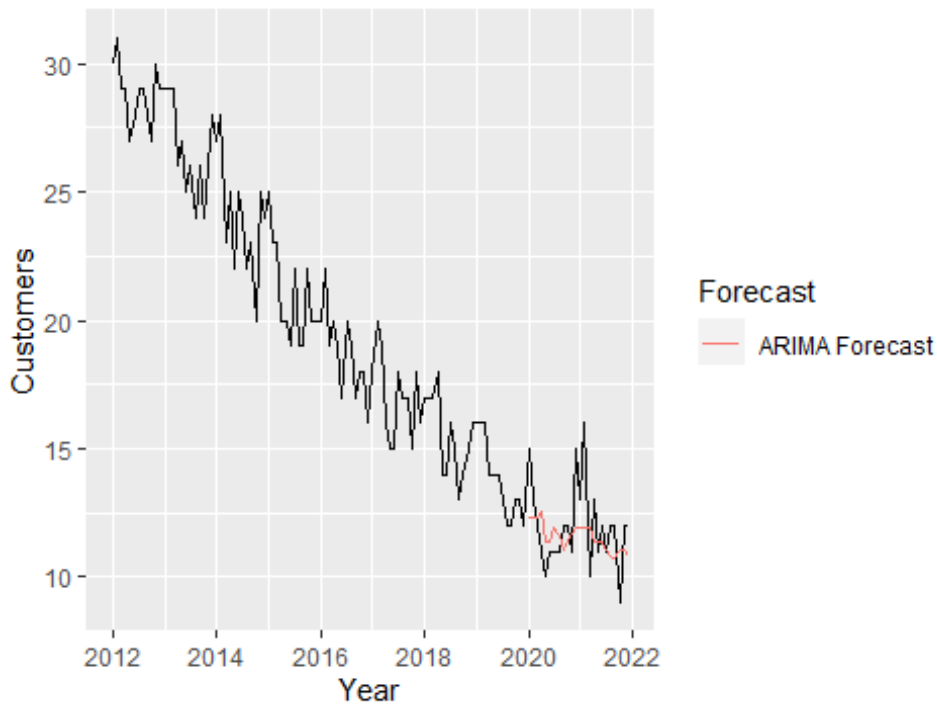
Below we fit & forecast 60 months into the future using an ARIMA (0,1,1)(0,0,2) model. In the graph below we see the 80% and 95% Prediction Intervals bounding our forecast.

Forecasts from ARIMA(0,1,1)(0,0,2)[12] with drift



Back-Testing

Commercial Client Backtesting: 2020-2021



Test Results

Below we see that the model performs roughly as expected for a “normal” year of 2019, and continues to have a high degree of accuracy in 2020 and 2021.

```
[1] "24Month Mean Absolute Error (MAE): 1.26"
```

```
[1] "24Month Mean Accuracy: 89.71"
```

	Actual	Forecast	Absolute_Error	Accuracy
Jan 2020	15	12	2.72	81.9
Feb 2020	13	12	0.72	94.5
Mar 2020	12	12	0.28	97.7
Apr 2020	11	13	1.53	86.1
May 2020	10	11	1.39	86.1
Jun 2020	11	11	0.39	96.5
Jul 2020	11	12	0.94	91.5
Aug 2020	11	12	0.64	94.2
Sep 2020	12	11	0.93	92.2
Oct 2020	12	11	0.63	94.8
Nov 2020	11	12	0.66	94.0
Dec 2020	15	12	3.07	79.5
Jan 2021	13	12	1.07	91.8
Feb 2021	16	12	4.07	74.6
Mar 2021	10	12	1.93	80.7
Apr 2021	13	11	1.63	87.5
May 2021	11	11	0.34	96.9
Jun 2021	12	11	0.66	94.5
Jul 2021	11	11	0.07	99.4
Aug 2021	12	11	1.22	89.8
Sep 2021	12	11	1.23	89.8

FPUC-Rate 0625498

Oct 2021	9	11	2.06	77.1
Nov 2021	12	11	0.94	92.2
Dec 2021	12	11	1.22	89.8